**NATIONAL
SENIOR CERTIFICATE**

GRADE 12

JUNE 2018

MATHEMATICS P1

MARKS: 150

TIME: 3 hours

JMATHE1

This question paper consists of 11 pages, including an information sheet.

INSTRUCTIONS AND INFORMATION

Read the following instructions carefully before answering the questions.

1.   This question paper consists of 10 questions. Answer ALL the questions.

2.   Clearly show ALL calculations, diagrams, graphs, et cetera that you have used in determining your answers.

3.   Answers only will not necessarily be awarded full marks.

4.   You may use an approved scientific calculator (non-programmable and non-graphical), unless stated otherwise.

5.   If necessary, round off answers to TWO decimal places, unless stated otherwise.

6.   Diagrams are NOT necessarily drawn to scale.

7.   An information sheet, with formulae, is included at the end of the question paper.

8.   Number the answers correctly according to the numbering system used in this question paper.

9.   Write neatly and legibly.

QUESTION 1

1.1   Solve for x, in each of the following:

    1.1.1 $(x - 2)(3x - 1) = 0$ (2)

    1.1.2 $2x^2 + 3x - 7 = 0$ (correct to TWO decimal places)   (3)

    1.1.3 $-x^2 - 2x + 15 < 0$ (4)

    1.1.4 $\dfrac{3^{x+1} - 3^x}{3^{x-1}} = 2\left(\dfrac{1}{9}\right)^{x-1}$ (5)

1.2   Solve simultaneously for x and y in the following equations:

    $x - 3y = 1$ and $y^2 + 2xy - x^2 = -7$ (6)

1.3   The solution(s) of a quadratic equation is given by: $x = \dfrac{n \pm \sqrt{n^2 + 4mn}}{2m}$

    Determine the value(s) of x if the roots are equal.   (5)

    [25]

QUESTION 2

2.1   The following quadratic pattern is given, $15 ; 10 ; 7 ; x ; 7 ; \ldots$

     2.1.1   Calculate the value of x.   (3)

     2.1.2   Determine the nth term of the above pattern.   (4)

     2.1.3   Calculate the value of the 50th term of the pattern.   (2)

2.2   In an arithmetic series the seventh term is 34 and the fifteenth term is 74.

     2.2.1   Determine the common difference of the series.   (3)

     2.2.2   Determine the sum of the first 40 terms of the series.   (3)

     2.2.3   Write the sum to 40 terms in sigma notation.   (2)

2.3   A geometric series has a general term, $T_k = \dfrac{3^k}{15}$

     2.3.1   Write the general term in the form $T_k = a.r^{k-1}$ (2)

     2.3.2   Determine the value of n, if $\displaystyle\sum_{k=1}^{n}\left(\frac{3^k}{15}\right) = 24\frac{1}{5}$ (4)

     2.3.3   Is this a convergent series? Give a reason.   (2)

2.4   Prove, without the use of a calculator, that $P = 9^{\frac{1}{3}} \times 9^{\frac{1}{9}} \times 9^{\frac{1}{27}} \times \ldots$ to infinity is equal to 3.   (4)

                                                [29]

QUESTION 3

3.1   The diagram below represents the graphs of $f(x) = a(x-2)^2 + 4$ and $g(x) = b^x$
        The graphs intersect at P, the turning point of f and at Q, the y-intercept of both f and g.
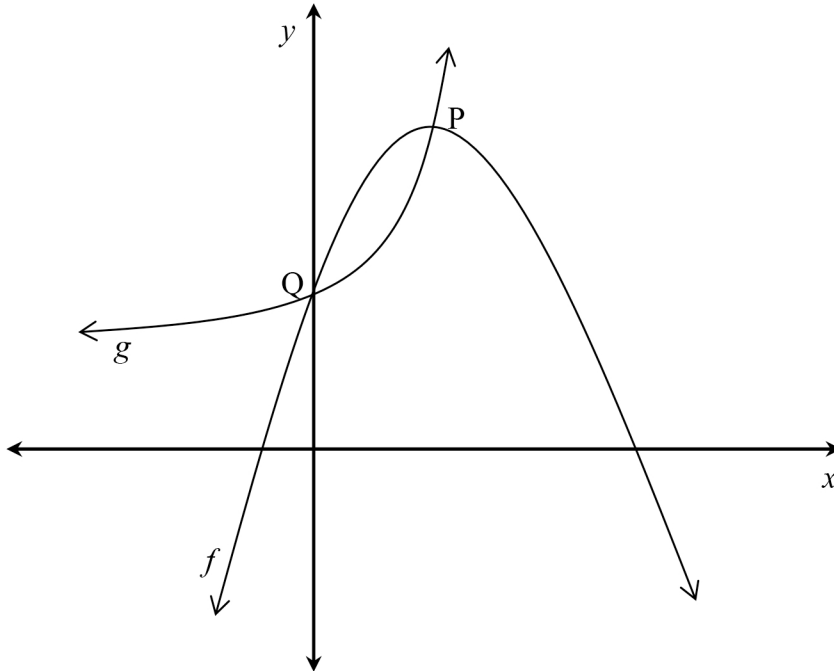
3.1.1   Write down the coordinates of P and Q.   (2)

3.1.2   Determine the values of a and b.   (4)

3.1.3   How can the domain of f be restricted such that f^{-1} may be a function?   (2)

3.1.4   Determine the maximum value of $h(x) = g[f(x)]$.   (2)

3.2   Consider the following two functions: $p(x) = x^2 + 1$ and $r(x) = x^2 + 2x$

3.2.1   Write down the range of p.   (1)

3.2.2   Describe the transformation from p to r.   (3)

[14]

QUESTION 4

Given the equation of f, a hyperbola, $f(x) = \dfrac{-3}{x+1} + 5$, answer the questions that follow.

4.1 Calculate the y-intercept of f. (1)

4.2 Calculate the x-intercept(s) of f. (2)

4.3 Sketch the graph of f, clearly indicating the asymptotes and intercepts with the axes. (3)

4.4 Write down the equation of the graph formed if the graph of f is shifted 3 units to the right and then reflected across the x-axis. (3)

[9]

QUESTION 5

The diagram represents a sketch graph of the function, $f(x) = \log_3 x$, with P(k ; -2) a point on the curve.
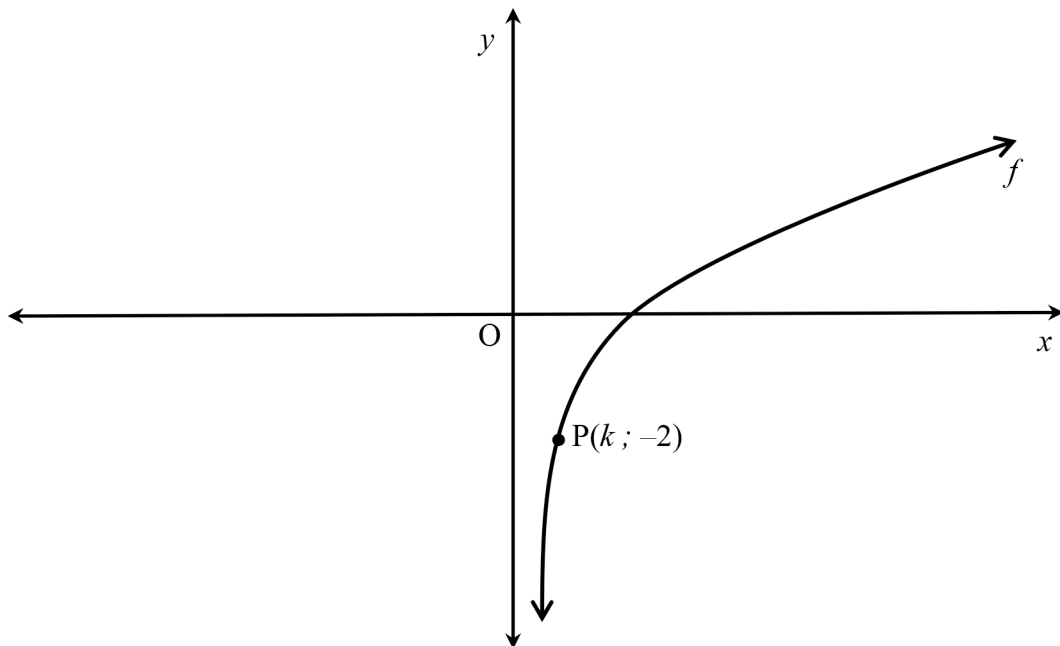
5.1 Determine the equation of f^{-1} in the form $f^{-1}(x) = ...$ (2)

5.2 Explain how you would use the graph of f to sketch the graph of f^{-1}. (2)

5.3 Find the value of k. (2)

5.4 Hence, or otherwise, solve for x, if $\log_3 x < -2$ (2)

5.5 For which value(s) of x, will $f(x) \cdot f'(x) \geq 0$? (2)

[10]

QUESTION 6

6.1   Interest on a credit card is quoted as 23% p.a. compounded monthly. What is the effective
       annual interest rate? Give your answer correct to two decimal places.   (3)

6.2   Mary has just been to the bank to withdraw all her savings, and to her delight she discovers
       she has saved R15 768,39 over the last 10 years. If the interest was calculated at 4,38% per
       annum, compounded quarterly, how much money did Mary originally invest at the bank?   (3)

6.3   A company purchased a new vehicle for R200 000. The vehicle's value depreciated to
       R50 710,00 at a rate of 24% p.a. on a reducing balance. The company wants to replace the
       vehicle with a new one. The replacement cost of the vehicle increased by 18% p.a.
       compounded annually, calculate:

       6.3.1   How long it took for the vehicle's value to depreciate to R50 710,00   (4)

       6.3.2   The cost of a new vehicle to replace the old one   (2)

       6.3.3   The total amount required, if the old vehicle is sold and the proceeds contribute
                towards the new vehicle   (1)
                                                                                                          [13]

QUESTION 7

7.1   Determine the derivative of $f(x) = 1 - 3x^2$ from first principles.   (4)

7.2   Determine $\dfrac{dy}{dx}$ if $y = \left(\sqrt{x} + \dfrac{1}{\sqrt{x}}\right)^2$ (3)

7.3   Determine the coordinates of the point on the graph of $y = 3x^2 - 2x + 1$ where the gradient
   is 4.   (4)
                                                                                                          [11]

QUESTION 8

8.1 The function, $f(x) = ax^3 + bx^2 + cx + d$, represents a cubic graph. The x-intercepts of the graph are $(-2;0)$, $\left(\dfrac{2}{3};0\right)$ and $(3;0)$. The points $P(x;y)$ and $Q(2;-16)$ are the turning points of f.

    8.1.1 Show that the equation of f is given by $f(x) = 3x^3 - 5x^2 - 16x + 12$. (5)

    8.1.2 Determine the coordinates of P, the local maximum of f. (4)

    8.1.3 Draw the graph of f, clearly indicating the turning points and the intercepts with the axes. (4)

8.2 Given: $f(x) = ax^3 + bx^2 + 3x + 3$ and $g(x) = f''(x)$ where $g(x) = 12x + 4$
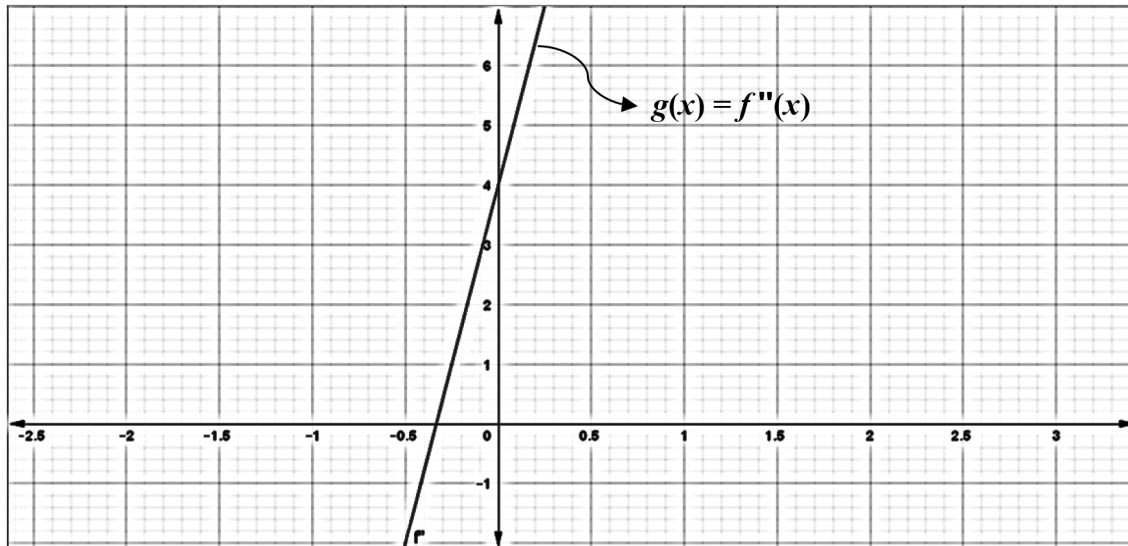
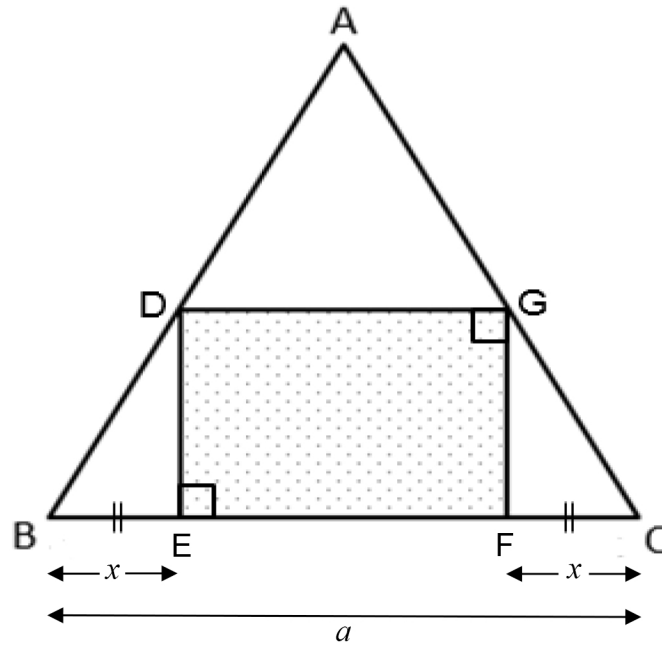   8.2.1 Determine the values of a and b. (2)

    8.2.2 For which value(s) of x, will $f'(x)$ be increasing? (2)

    8.2.3 Describe the concavity of f for all $x \in R$ (2)

[19]

QUESTION 9

In the sketch Δ ABC is an equilateral triangle with BC = *a* units.
DEFG is a rectangle. BE = FC = *x* units.

9.1   Prove that the area of the rectangle, $A = \sqrt{3}ax - 2\sqrt{3}x^2$ (4)

9.2   Determine, in terms of *a*, the maximum area of the rectangle.   (5)

[9]

QUESTION 10

10.1 The sport teacher at a school analysed data to determine how many learners play sport, as well as the gender of each learner. The data is presented in the following table.

	Do not play sport (not S)	Play sport (S)	Total
Male (M)	51	69	120
Female (F)	49	67	116
Total	100	136	236

    10.1.1 Determine the probability that a learner selected at random is female and plays sport. (1)

    10.1.2 Are the events "male" and "do not play sport" independent? Show ALL calculations to support your answer. (4)

10.2 In a bag, there are x blue balls and 2 red balls. A ball is selected at random, the colour is recorded and then replaced. Another ball is then selected at random, the colour is recorded and then replaced. The probability that the two balls are different colours is 0,375.

    10.2.1 Draw a tree diagram of the above scenario. (3)

    10.2.2 Hence, determine the value of x. (3)

[11]

TOTAL: 150

INFORMATION SHEET: MATHEMATICS

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$A = P(1 + ni) \qquad A = P(1 - ni) \qquad A = P(1 - i)^n \qquad A = P(1 + i)^n$$

$$T_n = a + (n-1)d \qquad S_n = \frac{n}{2}(2a + (n-1)d)$$

$$T_n = ar^{n-1} \qquad S_n = \frac{a(r^n - 1)}{r - 1} \quad ; \qquad r \neq 1 \qquad S_\infty = \frac{a}{1-r} \; ; \; -1 < r < 1$$

$$F = \frac{x\left[(1+i)^n - 1\right]}{i} \qquad\qquad P = \frac{x[1 - (1+i)^{-n}]}{i}$$

$$f'(x) = \lim_{h \to 0} \frac{f(x+h) - f(x)}{h}$$

$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2} \qquad M\left(\frac{x_1 + x_2}{2} ; \frac{y_1 + y_2}{2}\right)$$

$$y = mx + c \qquad y - y_1 = m(x - x_1) \qquad m = \frac{y_2 - y_1}{x_2 - x_1} \qquad\qquad m = \tan\theta$$

$$(x - a)^2 + (y - b)^2 = r^2$$

In ΔABC:

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C} \qquad a^2 = b^2 + c^2 - 2bc.\cos A \qquad area\,\Delta ABC = \frac{1}{2}ab.\sin C$$

$$\sin(\alpha + \beta) = \sin\alpha.\cos\beta + \cos\alpha.\sin\beta \qquad \sin(\alpha - \beta) = \sin\alpha.\cos\beta - \cos\alpha.\sin\beta$$

$$\cos(\alpha + \beta) = \cos\alpha.\cos\beta - \sin\alpha.\sin\beta \qquad \cos(\alpha - \beta) = \cos\alpha.\cos\beta + \sin\alpha.\sin\beta$$

$$\cos 2\alpha = \begin{cases} \cos^2\alpha - \sin^2\alpha \\ 1 - 2\sin^2\alpha \\ 2\cos^2\alpha - 1 \end{cases} \qquad\qquad \sin 2\alpha = 2\sin\alpha.\cos\alpha$$

$$\bar{x} = \frac{\sum x}{n} \qquad \partial^2 = \frac{\sum_{i=1}^{n}(x_i - \bar{x})^2}{n} \qquad P(A) = \frac{n(A)}{n(S)} \quad P(A \text{ or } B) = P(A) + P(B) - P$$

(A and B)

$$\hat{y} = a + bx \qquad b = \frac{\sum(x - \bar{x})(y - \bar{y})}{\sum(x - \bar{x})^2}$$

**NATIONAL
SENIOR CERTIFICATE**
*NASIONALE
SENIOR SERTIFIKAAT*

GRADE/*GRAAD* 12

JUNE/*JUNIE* 2018
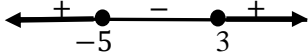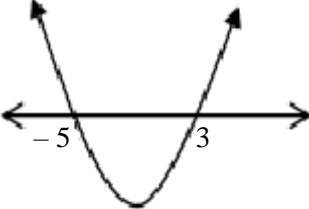
**MATHEMATICS P1/*WISKUNDE V1*
MARKING GUIDELINE/*NASIENRIGLYN***

MARKS/*PUNTE*: **150**

NOTE/LET OP:

- If a candidate answered a question TWICE, mark the FIRST attempt ONLY.
  Indien 'n kandidaat 'n vraag TWEE keer beantwoord het, merk SLEGS die EERSTE poging.
- Consistent accuracy(CA) applies in ALL aspects of the memorandum.
  Volgehoue akkuraatheid geld deurgaans in ALLE aspekte van die memorandum.
- If a candidate crossed out an attempt of a question and did not redo the question, mark the crossed-out attempt.
  Indien 'n kandidaat 'n poging vir 'n vraag deurgetrek het en nie die vraag weer beantwoord het nie, merk die poging wat deurgetrek is.
- The mark for substitution is awarded for substitution into the correct formula.
  Die punt vir substitusie word toegeken vir substitusie in die korrekte formule.

QUESTION 1/*VRAAG 1*

1.1.1	$(x-2)(3x-1)=0$ $x-2=0$ or/of $3x-1=0$ $\quad x=2$ or/of $x=\frac{1}{3}$	✓✓ x-values / *waardes* (2)
1.1.2	$2x^2+3x-7=0$ $\boxed{\text{Penalise 1 mark for incorrect rounding off./ \textit{Penaliseer 1 punt vir verkeerde afronding}.}}$ $x=\dfrac{-b\pm\sqrt{b^2-4ac}}{2a}$ $x=\dfrac{-(3)\pm\sqrt{(3)^2-4(2)(-7)}}{2(2)}$ $x=\dfrac{-3\pm\sqrt{65}}{4}$ $\therefore x=1,27$ *or / of* $x=-2,77$	✓ substitution / *vervanging* ✓✓ x-values / *waardes* (3)
1.1.3	$-x^2-2x+15<0$ $\;x^2+2x-15>0$ $(x+5)(x-3)>0$ $\therefore x<-5$ *or/of* $x>3$	✓ factors / *faktore* ✓ critical values with method/ *kritieke waardes met metode* ✓✓ answer (accuracy) / *antwoord (akkuraatheid)* (4)

1.1.4	$\dfrac{3^{x+1}-3^x}{3^{x-1}}=2\left(\dfrac{1}{9}\right)^{x-1}$	
	$\dfrac{3^x(3-1)}{3^x\left(\dfrac{1}{3}\right)}=2\left(3^{-2}\right)^{x-1}$	✓ simplifying LHS / *vereenvoudiging LK* ✓ simplifying RHS / *vereenvoudiging RK*
	$6=2\times3^{-2x+2}$ $3^{-2x+2}=3^1$	✓ same base / *dieselfde basis*
	$-2x+2=1$ $-2x=-1$	✓ equating exponents / *gelykstel van eksponente*
	$x=\dfrac{1}{2}$	✓ answer / *antwoord* (5)

1.2	$x-3y=1....................(1)$ $y^2+2xy-x^2=-7......(2)$	
	from / vanaf $(1):x=3y+1.....(3)$	✓ x subject of the formula / *x onderwerp van die formule*
	(3) *in* $(2):$ $\quad y^2+2y(3y+1)-(3y+1)^2=-7$	✓ substitution / *vervanging*
	$\qquad\qquad y^2+6y^2+2y-9y^2-6y-1+7=0$	✓ removing brackets / *verwyder hakies*
	$\qquad\qquad\qquad -2y^2-4y+6=0$ $\qquad\qquad\qquad\quad y^2+2y-3=0$	✓ standard form / *standaardvorm*
	$\qquad\qquad\qquad\quad (y+3)(y-1)=0$ $\qquad\qquad\qquad\qquad y=-3\ or/of\ \ y=1$	✓ y-values / *waardes*
	$\qquad\qquad\qquad\quad x=-8\ or/of\ \ x=4$	✓ x-values / *waardes* (6)

1.3	*For equal roots / Vir gelyke wortels :* $$n^2 + 4mn = 0$$ $$n(n + 4m) = 0$$ $$\therefore n = 0 \ or / of \ n = -4m$$ $$n = 0 \ \Rightarrow \ x = \frac{0 \pm \sqrt{(0)^2 - 4m(0)}}{2m}$$ $$x = 0$$ $$n = -4m \ \Rightarrow \ x = \frac{(-4m) \pm \sqrt{(-4m)^2 + 4m(-4m)}}{2m}$$ $$x = -2$$	$\checkmark \ \Delta = 0$ $\checkmark$ both *n*-values / *beide n-waardes* $\checkmark$ substitution / *vervanging* $\checkmark \ x = 0$ $\checkmark \ x = -2$ (5)
		[25]

QUESTION 2/VRAAG 2
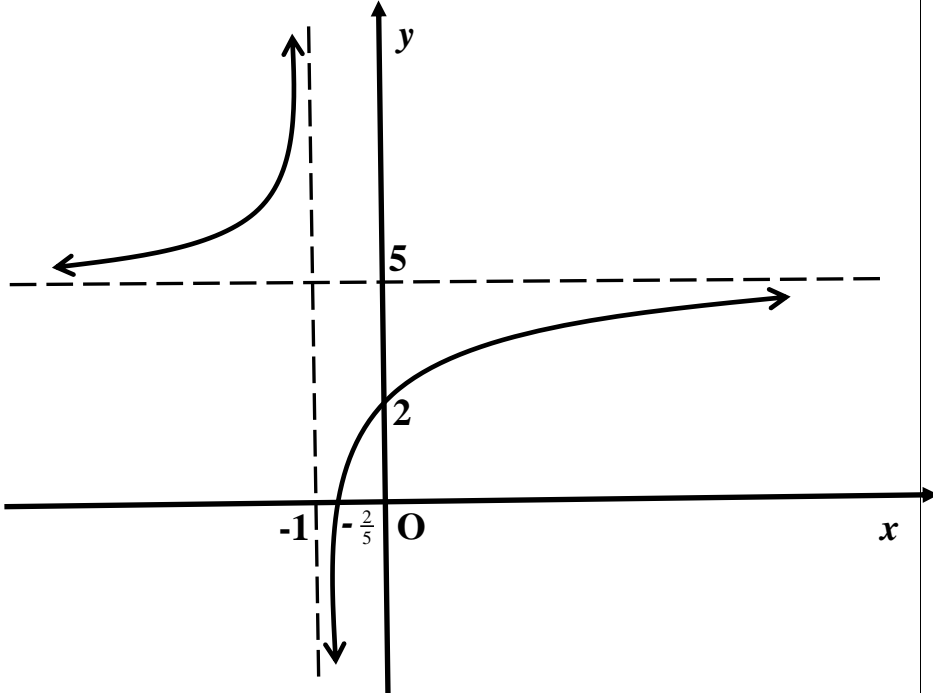
2.1.1	$15 \quad ; \quad 10 \quad ; \quad 7 \quad ; \quad x \quad ; \quad 7$ $\quad -5 \quad -3 \quad (x-7) \quad (7-x)$ - 1st differences/1ste verskille $\quad\quad 2 \quad (x-4) \quad (-2x+14)$ - 2nd differences/2de verskille $x-4=2 \quad\quad or/of \quad\quad -2x+14=x-4$ $\quad x=6 \quad\quad or/of \quad\quad\quad -3x=-18$ $\quad\quad\quad\quad\quad\quad\quad\quad\quad\quad\quad x=6$	✓ 2nd differences / 2de verskille ✓ equating / gelyk stel ✓ answer / antwoord (3)
2.1.2	$2a=2 \quad\quad 3a+b=-5 \quad\quad a+b+c=1$ $\ a=1 \quad\quad\ 3(1)+b=-5 \quad\quad 1-8+c=15$ $\quad\quad\quad\quad\quad\quad b=-8 \quad\quad\quad\quad\quad c=22$ $\therefore T_n = n^2 - 8n + 22$	✓ $a=1$ ✓ $b=-8$ ✓ $c=22$ ✓ answer / antwoord (4)
2.1.3	$T_{50} = (50)^2 - 8(50) + 22$ $\quad\ = 2122$	✓ substitution / vervanging ✓ answer / antwoord (2)
2.2.1	$a+14d=74$ $a+6d=34$ $\therefore \ 8d=40$ $\quad\ d=5$	✓ setting up 2 equations / opstel van 2 vergelykings ✓ method / metode ✓ answer / antwoord (3)
2.2.2	$a+6(5)=34$ $\quad\quad a=4$ $S_{40} = \dfrac{40}{2}\big[2(4)+(40-1)(5)\big]$ $\quad\ = 4060$	✓ value of a / waarde van a ✓ substitution into correct formula / vervanging in korrekte formule ✓ answer / antwoord (3)
2.2.3	$\displaystyle\sum_{n=1}^{40}(5n-1)$	✓✓ answer / antwoord (accuracy as one unit) (2)

2.3.1	$T_k = \dfrac{3^k}{15}$ $= \dfrac{3^k}{5 \times 3}$ $= \dfrac{1}{5} \times 3^{k-1}$	✓ factors of 15 / *faktore van* 15 ✓ answer / *antwoord* (2)
2.3.2	$S_n = \dfrac{a\left(r^n - 1\right)}{r - 1}$ $24\dfrac{1}{5} = \dfrac{\frac{1}{5}\left(3^n - 1\right)}{3 - 1}$ $48\dfrac{2}{5} = \dfrac{1}{5}\left(3^n - 1\right)$ $242 = 3^n - 1$ $243 = 3^n$ $3^5 = 3^n$ $\therefore n = 5$	✓ a and/en r ✓ substitution into correct formula / *vervanging in korrekte formule* ✓ exponential equation / *eksponensiële vergelyking* ✓ answer / *antwoord* (4)
2.3.3	NO / NEE. $r = 3 > 1$ r not in the interval $-1 < r < 1, r \neq 0$ (*nie in die interval*)	✓ NO / *NEE* ✓ reason / *rede* (2)
2.4	$P = 9^{\frac{1}{3}} \times 9^{\frac{1}{9}} \times 9^{\frac{1}{27}} \times ...$ to infinity / *tot oneindigend* $= 9^{\frac{1}{3} + \frac{1}{9} + \frac{1}{27} + ...\,\text{to infinity / tot oneindigend}}$ $S_\infty = \dfrac{a}{1 - r}$ $= \dfrac{\frac{1}{3}}{1 - \frac{1}{3}}$ $= \dfrac{1}{2}$ $\therefore P = 9^{\frac{1}{2}}$ $= \sqrt{9}$ $= 3$	✓ adding exponents / *optel van eksponente* ✓ sum to infinity / *Som tot oneindiging* ✓ answer / *antwoord* ✓ $P = 9^{\frac{1}{2}} / \sqrt{9}$ (4)
		[29]

QUESTION 3/*VRAAG 3*

3.1.1	$P(2;4)$ $Q(0;1)$	✓ coordinates of P / *koördinate van* P ✓ coordinates of Q / *koördinate van* Q (2)
3.1.2	$y = a(x-2)^2 + 4$ $1 = a(0-2)^2 + 4$ $-3 = 4a$ $\therefore a = -\dfrac{3}{4}$ $y = b^x$ $4 = b^2$ $\therefore b = 2$	✓ substitution / *vervanging* ✓ answer / *antwoord* ✓ substitution / *vervanging* ✓ answer / *antwoord* (4)
3.1.3	$x \geq 2$ / $x \leq 2$	✓✓ answer / *antwoord* (2)
3.1.4	$h(x) = 2^{f(x)}$ is a maximum when $f(x)$ is a maximum $\quad\quad\quad$ (*is 'n maksimum wanneer* $f(x)$ *'n maksimum is*) max *value of* $f(x) = 4$ / *maks. waarde van* $f(x) = 4$ $\therefore$ max *of* $h(x) = 2^4 = 16$ / *maks van* $h(x) = 2^4 = 16$	✓ max. value of *f(x)* / *maks. waarde van f(x)* ✓ answer / *antwoord* (2)
3.2.1	$y \geq 1, y \in R$ **OR/OF** $y \in (1; \infty)$	✓ answer / *antwoord* (1)
3.2.2	$p(x) = x^2 + 1$ / $r(x) = x^2 + 2x$ $p(x+1) - 2 = (x+1)^2 + 1 - 2$ $\quad\quad\quad\quad\quad = x^2 + 2x + 1 + 1 - 2$ $\quad\quad\quad\quad\quad = x^2 + 2x$ *Shift* 1 *unit to the left and* 2 *units down* *Skuif* 1 *eenheid na links en* 2 *eenhede af* **OR/OF** Turning Point of p(*x*) / *Draaipunt van* p(*x*) = (0 ; 1) Turning Point of r(*x*) / *Draaipunt van* r(*x*) = (-1 ; -1) $\therefore$ Shift 1 unit to the left and 2 units down / *Skuif 1 eenheid na links en 2 eenhede af*	✓ calculation / *berekening* ✓ 1 unit to the left / *1 eenheid na links* ✓ 2 units down / *2 eenhede af* (3)
		[14]

QUESTION 4/*VRAAG 4*

4.1	$y = \dfrac{-3}{0+1} + 5$ $\quad = 2$	✓ *y*-intercept / y-afsnit (1)
4.2	$\dfrac{-3}{x+1} + 5 = 0$ $\quad \dfrac{-3}{x+1} = -5$ $-5x - 5 = -3$ $\quad -5x = 2$ $\qquad x = -\dfrac{2}{5}$	✓ simplification / *vereenvoudiging* ✓ answer / *antwoord* (2)
4.3		✓ asymptotes / *asimptote* ✓ *x*- and *y-intercepts* *x*- en *y-afsnitte* ✓ shape / *vorm* (3)
4.4	$f(x) = \dfrac{-3}{x+1} + 5$ $f(x-3) = \dfrac{-3}{(x-3)+1} + 5$ $\qquad = \dfrac{-3}{x-2} + 5$ $f(x) = \dfrac{3}{x-2} - 5$	✓ substitution / *vervanging* ✓ simplification / *vereenvoudiging* ✓ reflection / *refleksie* (3)
		[9]

QUESTION 5/*VRAAG 5*

5.1	$f(x) = \log_3 x$ $x = \log_3 y$ $f^{-1}(x) = 3^x$	✓ interchanging x and y / *omruil van x en y* ✓ answer / *antwoord* (2)
5.2	f^{-1} is a reflection of f in the line $y = x$ / f^{-1} *is 'n refleksie van f in die lyn y = x*	✓✓ answer / *antwoord* (2)
5.3	$y = \log_3 x$ $-2 = \log_3 k$ $\therefore k = 3^{-2}$ $\quad = \dfrac{1}{9}$	✓ substitution / *vervanging* ✓ answer / *antwoord* (2)
5.4	$0 < x < \dfrac{1}{9}$ **OR / OF** $\log_3 x < -2 \;\; and / en \;\; x > 0$ $x < \dfrac{1}{9} \;\; and / en \;\; x > 0$ $0 < x < \dfrac{1}{9}$	✓✓ answer / *antwoord* (2)
5.5	$x \geq 1$	✓✓ answer / *antwoord* (2)
		[10]

QUESTION 6/*VRAAG 6*

6.1	$1 + i_{eff} = \left(1 + \dfrac{i_{nom}}{n}\right)^n$ $i_{eff} = \left(1 + \dfrac{23}{1200}\right)^{12} - 1$ $= 0,2558637702$ effective rate / *effektiewe koers* $=25,59\%$ p.a	✓ formula / *formule* ✓ substitution / *vervanging* ✓ answer / *antwoord* (3)
6.2	$P = \dfrac{A}{(1+i)^n}$ $= \dfrac{15768,39}{\left(1 + \dfrac{4,38}{400}\right)^{40}}$ $= R10\,200,00$	✓ i and/*en* n ✓ substitution / *vervanging* ✓ answer / *antwoord* (3)
6.3.1	$n = \dfrac{\log\left[\dfrac{A}{P}\right]}{\log\left(1-i\right)}$ $n = \dfrac{\log\left[\dfrac{50710,00}{200000,00}\right]}{\log\left(1 - \dfrac{24}{100}\right)}$ $n = 5\ years$	✓ A and/*en* P ✓ substitution / *vervanging* ✓ making n subject of the formula / *maak n die onderwerp van die formule* ✓ answer / *antwoord* (4)
6.3.2	$A = P\left(1+i\right)^n$ $= 200\,000\left(1 + \dfrac{18}{100}\right)^5$ $= R457\,551,55$	✓ substitution / *vervanging* ✓ answer / *antwoord* (2)
6.3.3	Amount/*Bedrag* = R457 551,55 – R50 710.00 = R406 841,55	✓ answer / *antwoord* (1)
		[13]

QUESTION 7/VRAAG 7

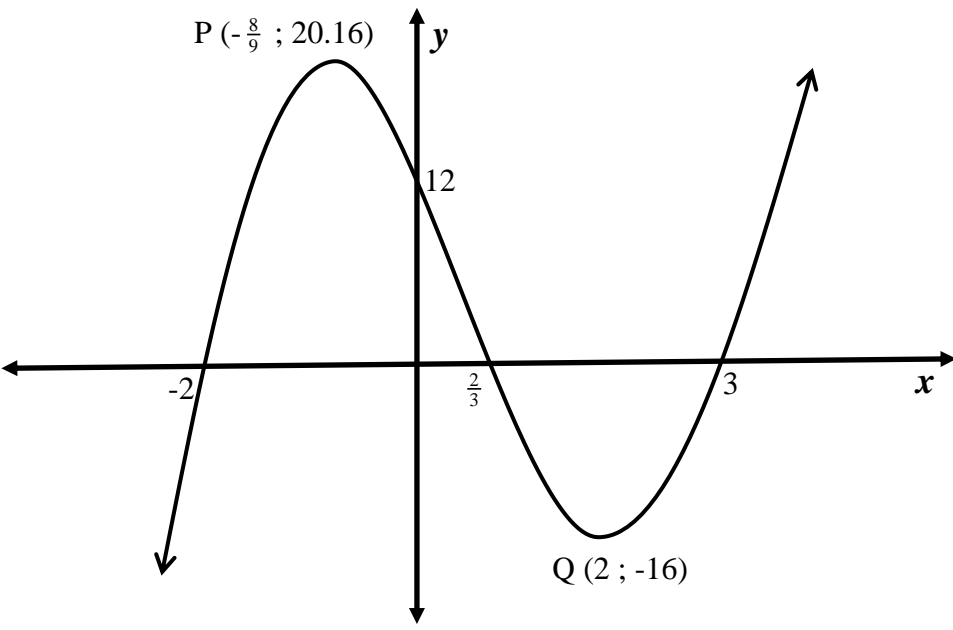|		
		Penalise 1 mark for incorrect notation in the question / *Penaliseer 1 punt vir verkeerde notasie in die vraag*
7.1	$f(x) = 1 - 3x^2$ $f(x + h) = 1 - 3(x + h)^2$ $\qquad = 1 - 3(x^2 + 2xh + h^2)$ $\qquad = 1 - 3x^2 - 6xh - 3h^2$ $f'(x) = \lim\limits_{h \to 0} \dfrac{f(x + h) - f(x)}{h}$ $\qquad = \lim\limits_{h \to 0} \dfrac{1 - 3x^2 - 6xh - 3h^2 - (1 - 3x^2)}{h}$ $\qquad = \lim\limits_{h \to 0} \dfrac{-6xh - 3h^2}{h}$ $\qquad = \lim\limits_{h \to 0} \dfrac{h(-6x - 3h)}{h}$ $\qquad = \lim\limits_{h \to 0} (-6x - 3h)$ $\qquad = -6x$ Answer ONLY: 0 marks / *SLEGS antwoord: 0 punte*	✓ $1 - 3x^2 - 6xh - 3h^2$ ✓ substitution / *vervanging* ✓ common factor / *gemene faktor* ✓ answer / *antwoord* (4)
7.2	$y = \left(\sqrt{x} - \dfrac{1}{\sqrt{x}} \right)^2$ $y = x + 2 + \dfrac{1}{x}$ $y = x + 2 + x^{-1}$ $\dfrac{dy}{dx} = 1 - x^{-2}$	✓ $y = x + 2 + x^{-1}$ ✓ 1 ✓ $-x^{-2}$ (3)
7.3	$y = 3x^2 - 2x + 1$ $y' = 6x - 2$ $6x - 2 = 4$ $6x = 6$ $x = 1$ $y = 2 \qquad (1;2)$	✓ $y' = 6x - 2$ ✓ $6x - 2 = 4$ ✓ x-coordinate / *x-koördinaat* ✓ answer / *antwoord* (4)
		[11]
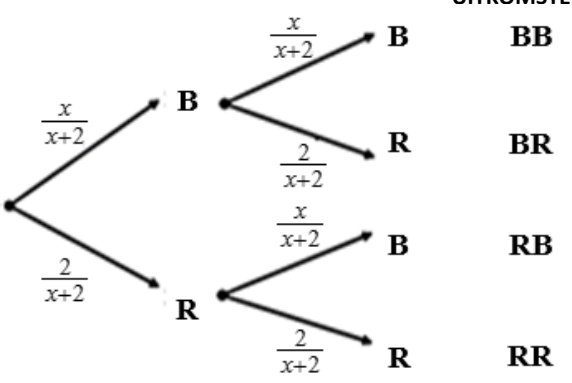
QUESTION 8/*VRAAG 8*

8.1.1	$f(x) = a(x+2)(x-\frac{2}{3})(x-3)$	✓ substitution of *x*-coordinates / *vervanging van x-koördinate*
	$-16 = a(2+2)(2-\frac{2}{3})(2-3)$	
	$-16 = -\dfrac{16}{3}a$	✓ substitution of point / *vervanging van punt*
	$a = 3$	✓ value of *a* / *waarde van a*
	$f(x) = 3(x+2)\left(x-\frac{2}{3}\right)(x-3)$	
	$\quad = 3\left(x-\frac{2}{3}\right)\left(x^2-x-6\right)$	✓ substitution / *vervanging*
	$\quad = 3\left(x^3-x^2-6x-\frac{2}{3}x^2+\frac{2}{3}x+4\right)$	✓ removing brackets / *verwyder hakies*
	$\quad = 3x^3-5x^2-16x+12$	(5)

8.1.2	$f(x) = 3x^3 - 5x^2 - 16x + 12$	
	$f'(x) = 9x^2 - 10x - 16 = 0$	✓ $f'(x) = 0$
	$\quad\quad (9x+8)(x-2) = 0$	
	$\quad\quad 9x+8 = 0 \ \ or/of \ \ x-2 = 0$	✓ factors / *faktore*
	$\quad\quad\quad x = -\dfrac{8}{9} \quad or \ /of \ \ x = 2$	✓ *x*-values / *waardes*
	$\quad\quad\quad y = \dfrac{4900}{243} \ (20,16)$	
	$B\left(-\dfrac{8}{9} \ ; \ 20,16\right)$	✓ coordinates of P / *koördinate van* P
		(4)

8.1.3		✓ *x*-intercepts / *x-afsnitte*
		✓ *y*-intercept / *y-afsnit*
		✓ turning pts / *draaipunte*
		✓ shape / *vorm*
		(4)

8.2.1	$f(x) = ax^3 + bx^2 + 3x + 3$ *and / en* $g(x) = f''(x) = 12x + 4$	
	$f'(x) = 3ax^2 + 2bx + 3$ $f''(x) = 6ax + 2b$ $6a = 12$ *and / en* $2b = 4$ $a = 2$ *and / en* $b = 2$	✓ $a = 2$ ✓ $b = 2$ (2)
8.2.2	$12x + 4 = 0$ $x = -\dfrac{1}{3}$ $\therefore x > -\dfrac{1}{3}$	✓ $x = -\frac{1}{3}$ ✓ answer / *antwoord* (2)

8.2.3	$f''(x) < 0$ *for* $x < -\dfrac{1}{3}$ $\big(\textit{concave down / konkaaf afwaarts}\big)$
	
	 $f''(x) > 0$ *for* $x > -\dfrac{1}{3}$ $\big(\textit{concave up / konkaaf opwaarts}\big)$
	
	 $x = -\dfrac{1}{3}$ is the *x*-coordinate of the point of inflection
	      where the concavity changes.
	
	 $x = -\dfrac{1}{3}$ is die *x*-koördinaat van die infleksiepunt waar die
	      konkawiteit verander.
		✓ answer / *antwoord*
		
		 ✓ answer / *antwoord*
		
		 (2)

		[19]

QUESTION 9/*VRAAG 9*

9.1	$EF = a - 2x$		✓ $EF = (a - 2x)$	
	$\dfrac{DE}{BE} = \tan 60^0$		✓ tan ratio / tan *verhouding*	
	$DE = x \tan 60^0$		✓ answer / *antwoord*	
	$\quad = \sqrt{3}x$			
	$Area = l \times b$			
	$\quad = \sqrt{3}x \times (a - 2x)$	No mark for the answer / Geen punt vir die antwoord	✓ substitution / *vervanging*	(4)
	$\quad = \sqrt{3}ax - 2\sqrt{3}x^2$			
9.2	$A(x) = \sqrt{3}ax - 2\sqrt{3}x^2$			
	$A'(x) = \sqrt{3}a - 4\sqrt{3}x = 0$		✓ derivative / *afgeleide* ✓ $f'(x) = 0$	
	$\quad x = \dfrac{-\sqrt{3}a}{-4\sqrt{3}}$			
	$\quad x = \dfrac{a}{4}$		✓ answer / *antwoord*	
	$Area = \sqrt{3}a\left(\dfrac{a}{4}\right) - 2\sqrt{3}\left(\dfrac{a}{4}\right)^2$		✓ substitution / *vervanging*	
	$\quad = \dfrac{\sqrt{3}}{4}a^2 - \dfrac{\sqrt{3}}{8}a^2$			
	$\quad = \dfrac{\sqrt{3}}{8}a^2$		✓ answer / *antwoord*	(5)
				[9]

QUESTION 10/*VRAAG 10*

10.1.1	$P(F \text{ and } S) = \dfrac{67}{236} / 0,28$	✓ answer / *antwoord* (1)
10.1.2	$P(M) \times P(not\ S)$ $= \dfrac{120}{236} \times \dfrac{100}{236}$ $= 0,22$ $P(M \cap not\ S) = \dfrac{51}{236}$ $\qquad\qquad\quad = 0,22$ $\therefore P(M) \times P(not\ S) = P(M \cap not\ S)$ $\Rightarrow events\ are\ independent\ /$ $\quad gebeurtenisse\ is\ onafhanklik$	✓ P(M) x P(not S) ✓ answer / *antwoord* ✓ answer / *antwoord* ✓ conclusion / *gevolgtrekking* (4)
10.2.1		✓ 1st branch / 1ste *tak* ✓ 2nd branch / 2de *tak* ✓ outcomes / *uitkomste* (3)
10.2.2	$\left(\dfrac{x}{x+2} \times \dfrac{2}{x+2}\right) + \left(\dfrac{2}{x+2} \times \dfrac{x}{x+2}\right) = 0,375$ $\left(\dfrac{2x}{(x+2)^2}\right) + \left(\dfrac{2x}{(x+2)^2}\right) = \dfrac{3}{8}$ $\dfrac{4x}{(x+2)^2} = \dfrac{3}{8}$ $3x^2 + 12x + 12 = 32x$ $3x^2 - 20x + 12 = 0$ $(3x-2)(x-6) = 0$ $x = \dfrac{2}{3}\ or\ /\ of\ \ x = 6$	✓ setting up equation / *opstel van vergelyking* ✓ standard form / *standaardvorm* ✓ answer / *antwoord* (3)
		[11]
		TOTAL/TOTAAL: 150