



basic education

Department:
Basic Education
REPUBLIC OF SOUTH AFRICA

NATIONAL SENIOR CERTIFICATE

GRADE 12

MATHEMATICS P2

NOVEMBER 2017

MARKS: 150

TIME: 3 hours

**This question paper consists of 14 pages, 1 information sheet
and an answer book of 28 pages.**

INSTRUCTIONS AND INFORMATION

Read the following instructions carefully before answering the questions.

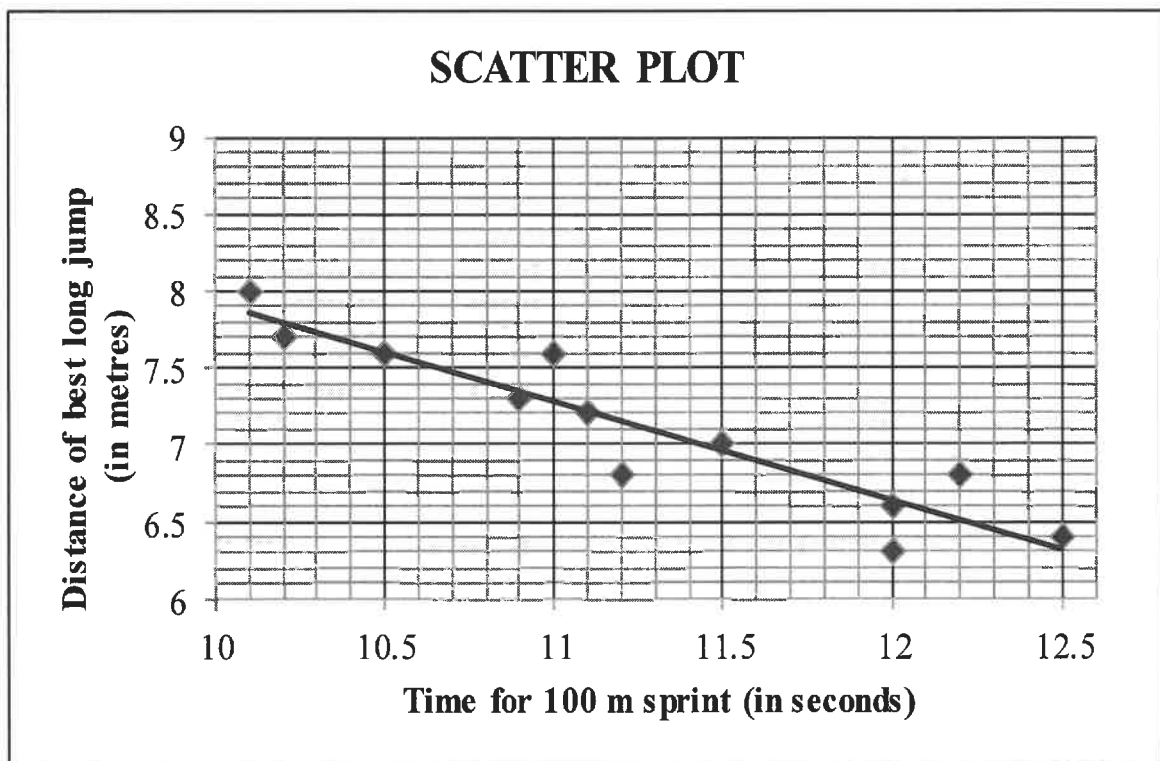
1. This question paper consists of 11 questions.
2. Answer ALL the questions in the ANSWER BOOK provided.
3. Clearly show ALL calculations, diagrams, graphs, et cetera that you have used in determining your answers.
4. Answers only will NOT necessarily be awarded full marks.
5. You may use an approved scientific calculator (non-programmable and non-graphical), unless stated otherwise.
6. If necessary, round off answers to TWO decimal places, unless stated otherwise.
7. Diagrams are NOT necessarily drawn to scale.
8. An information sheet with formulae is included at the end of the question paper.
9. Write neatly and legibly.

QUESTION 1

The table below shows the time (in seconds, rounded to ONE decimal place) taken by 12 athletes to run the 100 metre sprint and the distance (in metres, rounded to ONE decimal place) of their best long jump.

| | | | | | | | | | | | | |
|---|------|------|------|------|-----|------|------|------|-----|-----|------|------|
| Time for 100 m sprint (in seconds) | 10,1 | 10,2 | 10,5 | 10,9 | 11 | 11,1 | 11,2 | 11,5 | 12 | 12 | 12,2 | 12,5 |
| Distance of best long jump (in metres) | 8 | 7,7 | 7,6 | 7,3 | 7,6 | 7,2 | 6,8 | 7 | 6,6 | 6,3 | 6,8 | 6,4 |

The scatter plot representing the data above is given below.



The equation of the least squares regression line is $\hat{y} = a + bx$.

- 1.1 Determine the values of a and b . (3)
- 1.2 An athlete runs the 100 metre sprint in 11,7 seconds. Use $\hat{y} = a + bx$ to predict the distance of the best long jump of this athlete. (2)
- 1.3 Another athlete completes the 100 metre sprint in 12,3 seconds and the distance of his best long jump is 7,6 metres. If this is included in the data, will the gradient of the least squares regression line increase or decrease? Motivate your answer without any further calculations. (2)

[7]

QUESTION 2

In an experiment, a group of 23 girls were presented with a page containing 30 coloured rectangles. They were asked to name the colours of the rectangles correctly as quickly as possible. The time, in seconds, taken by each of the girls is given in the table below.

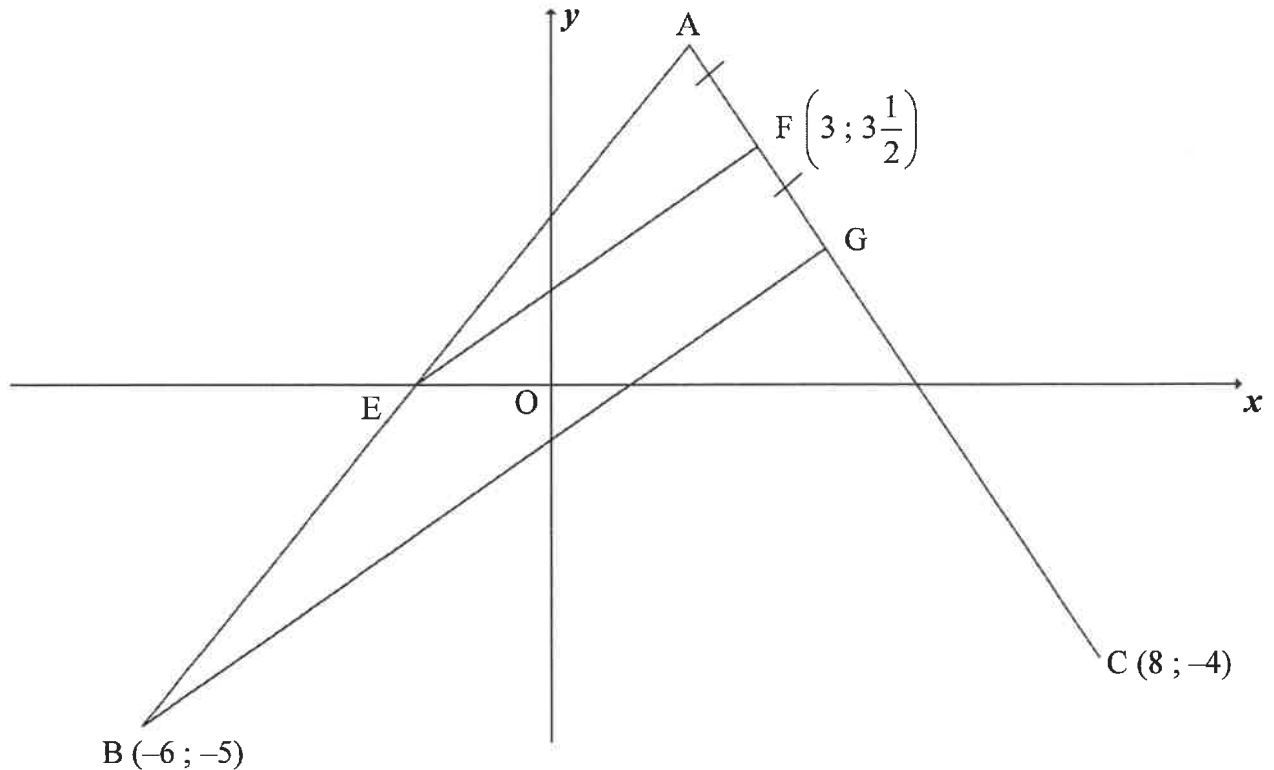
| | | | | | | | | | | | |
|----|----|----|----|----|----|----|----|----|----|----|----|
| 12 | 13 | 13 | 14 | 14 | 16 | 17 | 18 | 18 | 18 | 19 | 20 |
| 21 | 21 | 22 | 22 | 23 | 24 | 25 | 27 | 29 | 30 | 36 | |

- 2.1 Calculate:
- 2.1.1 The mean of the data (2)
- 2.1.2 The interquartile range of the data (3)
- 2.2 The standard deviation of the times taken by the girls is 5,94. How many girls took longer than ONE standard deviation from the mean to name the colours? (2)
- 2.3 Draw a box and whisker diagram to represent the data on the number line provided in the ANSWER BOOK. (3)
- 2.4 The five-number summary of the times taken by a group of 23 boys in naming the colours of the rectangles correctly is (15 ; 21 ; 23,5 ; 26 ; 38).
- 2.4.1 Which of the two groups, girls or boys, had the lower median time to correctly name the colours of the rectangles? (1)
- 2.4.2 The first three learners who named the colours of all 30 rectangles correctly in the shortest time will receive a prize. How many boys will be among these three prizewinners? Motivate your answer. (2)

[13]

QUESTION 3

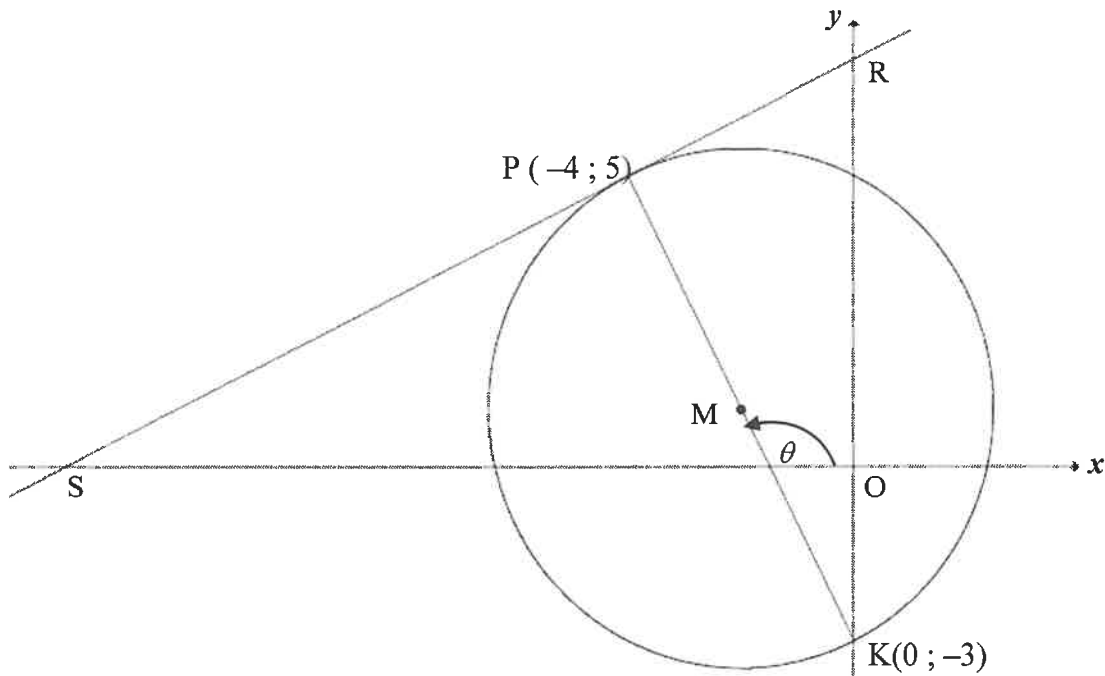
In the diagram, A, B(-6 ; -5) and C(8 ; -4) are points in the Cartesian plane. $F\left(3; 3\frac{1}{2}\right)$ and G are points on line AC such that $AF = FG$. E is the x-intercept of AB.



- 3.1 Calculate:
- 3.1.1 The equation of AC in the form $y = mx + c$ (4)
- 3.1.2 The coordinates of G if the equation of BG is $7x - 10y = 8$ (3)
- 3.2 Show by calculation that the coordinates of A is (2 ; 5). (2)
- 3.3 Prove that $EF \parallel BG$. (4)
- 3.4 ABCD is a parallelogram with D in the first quadrant. Calculate the coordinates of D. (4)
- [17]

QUESTION 4

In the diagram, $P(-4 ; 5)$ and $K(0 ; -3)$ are the end points of the diameter of a circle with centre M . S and R are respectively the x - and y -intercept of the tangent to the circle at P . θ is the inclination of PK with the positive x -axis.



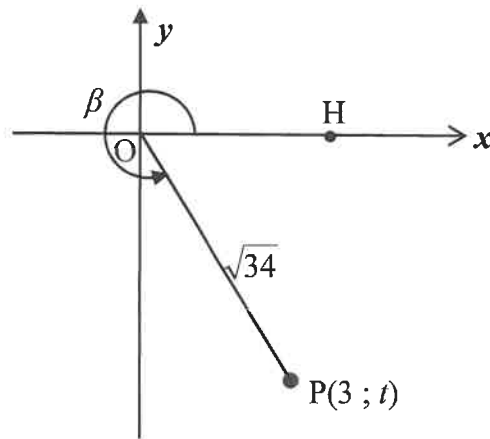
- 4.1 Determine:
- 4.1.1 The gradient of SR (4)
- 4.1.2 The equation of SR in the form $y = mx + c$ (2)
- 4.1.3 The equation of the circle in the form $(x - a)^2 + (y - b)^2 = r^2$ (4)
- 4.1.4 The size of $\hat{P}KR$ (3)
- 4.1.5 The equation of the tangent to the circle at K in the form $y = mx + c$ (2)
- 4.2 Determine the values of t such that the line $y = \frac{1}{2}x + t$ cuts the circle at two different points. (3)
- 4.3 Calculate the area of $\triangle SMK$. (5)
- [23]**

QUESTION 5

5.1 Given:
$$\frac{\sin(A - 360^\circ) \cdot \cos(90^\circ + A)}{\cos(90^\circ - A) \cdot \tan(-A)}$$

Simplify the expression to a single trigonometric ratio. (6)

5.2 In the diagram, $P(3 ; t)$ is a point in the Cartesian plane. $OP = \sqrt{34}$ and $\widehat{HOP} = \beta$ is a reflex angle.



Without using a calculator, determine the value of:

5.2.1 t (2)

5.2.2 $\tan \beta$ (1)

5.2.3 $\cos 2\beta$ (4)

5.3 Prove:

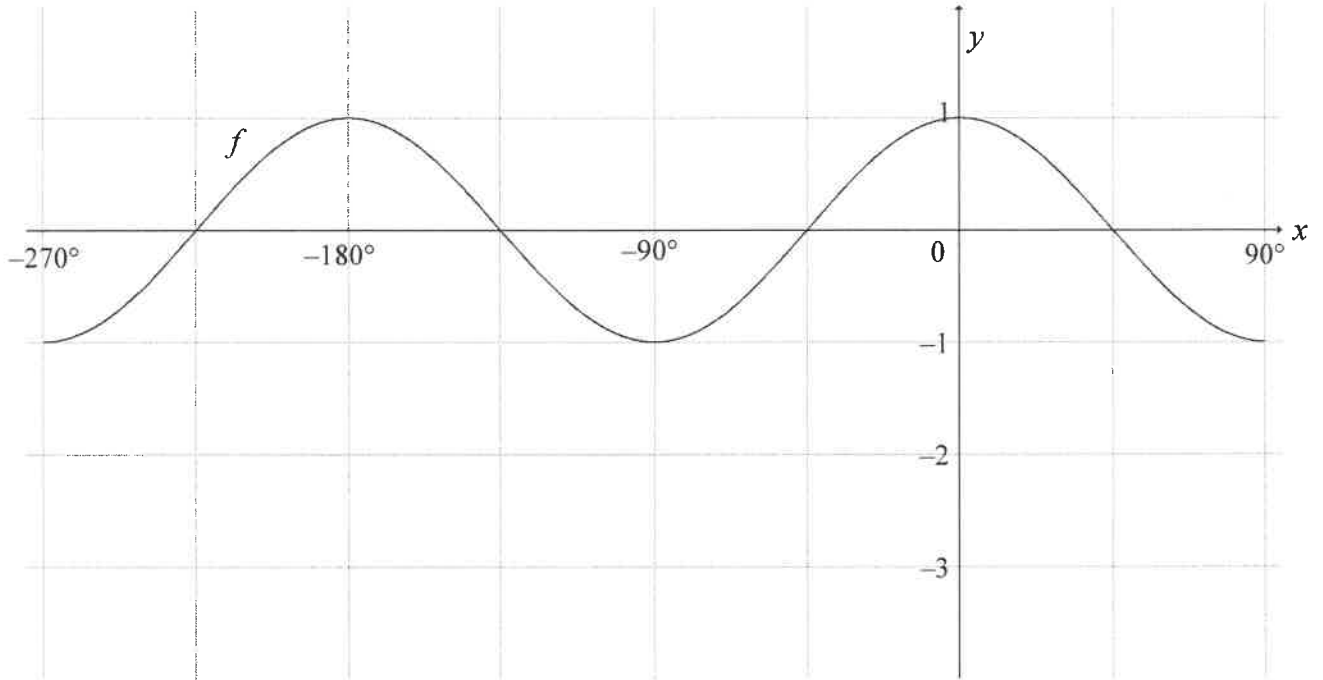
5.3.1 $\sin(A + B) - \sin(A - B) = 2 \cos A \cdot \sin B$ (2)

5.3.2 **Without using a calculator, that** $\sin 77^\circ - \sin 43^\circ = \sin 17^\circ$ (4)

[19]

QUESTION 6

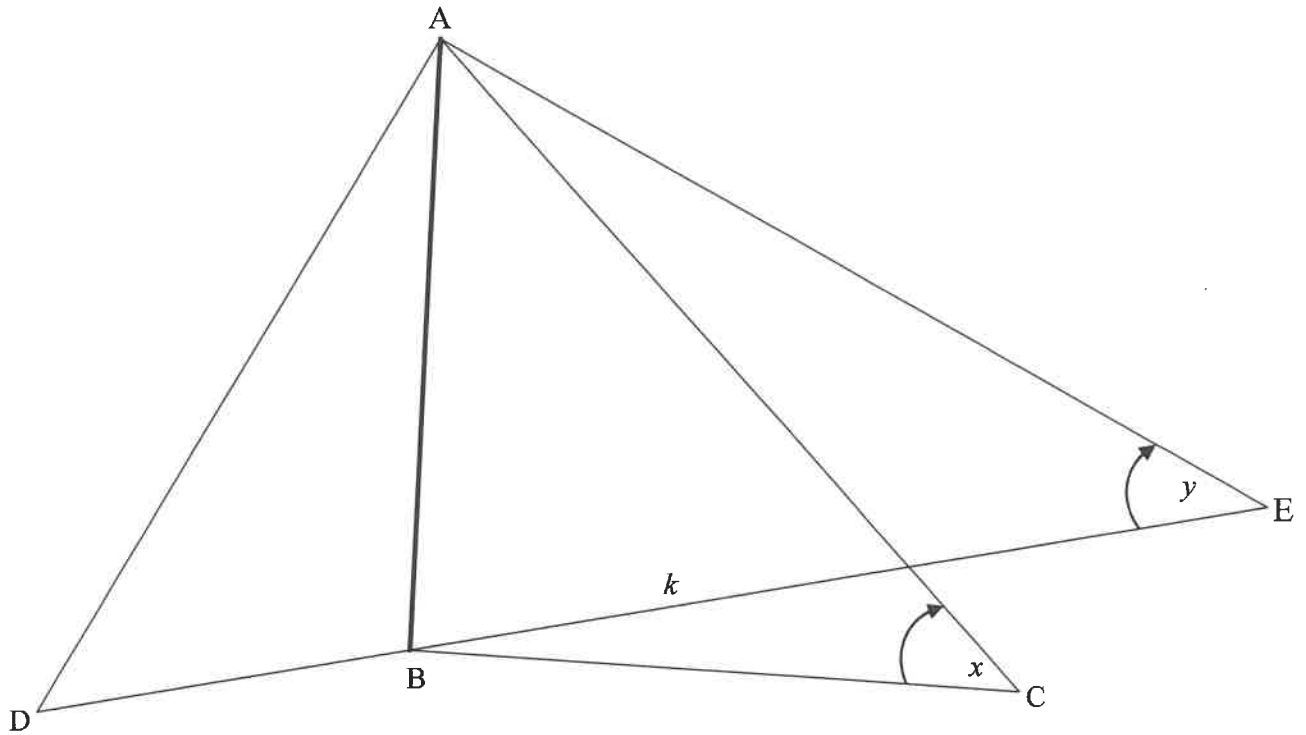
In the diagram, the graph of $f(x) = \cos 2x$ is drawn for the interval $x \in [-270^\circ; 90^\circ]$.



- 6.1 Draw the graph of $g(x) = 2\sin x - 1$ for the interval $x \in [-270^\circ; 90^\circ]$ on the grid given in your ANSWER BOOK. Show ALL the intercepts with the axes, as well as the turning points. (4)
 - 6.2 Let A be a point of intersection of the graphs of f and g . Show that the x -coordinate of A satisfies the equation $\sin x = \frac{-1 + \sqrt{5}}{2}$. (4)
 - 6.3 Hence, calculate the coordinates of the points of intersection of graphs of f and g for the interval $x \in [-270^\circ; 90^\circ]$. (4)
- [12]**

QUESTION 7

AB represents a vertical netball pole. Two players are positioned on either side of the netball pole at points D and E such that D, B and E are on the same straight line. A third player is positioned at C. The points B, C, D and E are in the same horizontal plane. The angles of elevation from C to A and from E to A are x and y respectively. The distance from B to E is k .

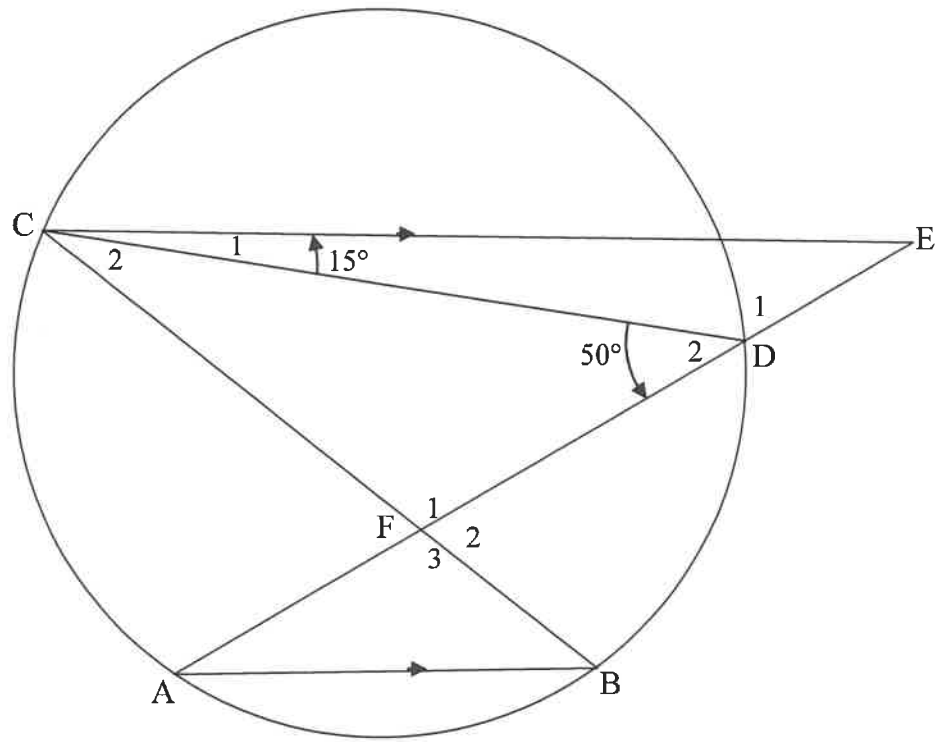


- 7.1 Write down the size of \hat{ABC} . (1)
 - 7.2 Show that $AC = \frac{k \cdot \tan y}{\sin x}$ (4)
 - 7.3 If it is further given that $\hat{DAC} = 2x$ and $AD = AC$, show that the distance DC between the players at D and C is $2k \tan y$. (5)
- [10]**

Give reasons for your statements in QUESTIONS 8, 9, 10 and 11.

QUESTION 8

In the diagram, points A, B, D and C lie on a circle. $CE \parallel AB$ with E on AD produced. Chords CB and AD intersect at F. $\hat{D}_2 = 50^\circ$ and $\hat{C}_1 = 15^\circ$.



8.1 Calculate, with reasons, the size of:

8.1.1 \hat{A} (3)

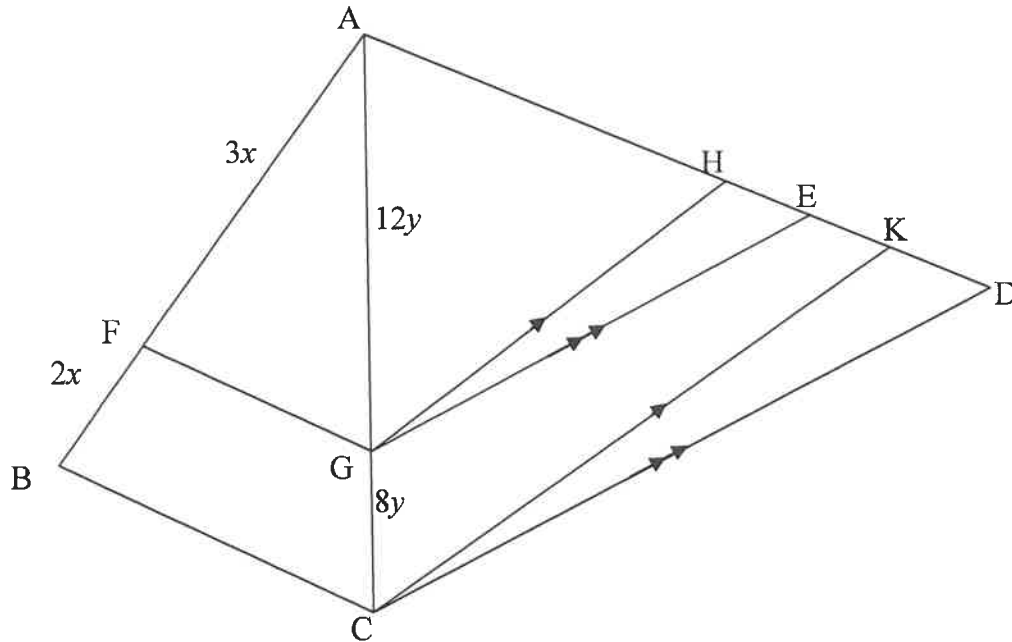
8.1.2 \hat{C}_2 (2)

8.2 Prove, with a reason, that CF is a tangent to the circle passing through points C, D and E. (2)

[7]

QUESTION 9

In the diagram, $\triangle ABC$ and $\triangle ACD$ are drawn. F and G are points on sides AB and AC respectively such that $AF = 3x$, $FB = 2x$, $AG = 12y$ and $GC = 8y$. H, E and K are points on side AD such that $GH \parallel CK$ and $GE \parallel CD$.



9.1 Prove that:

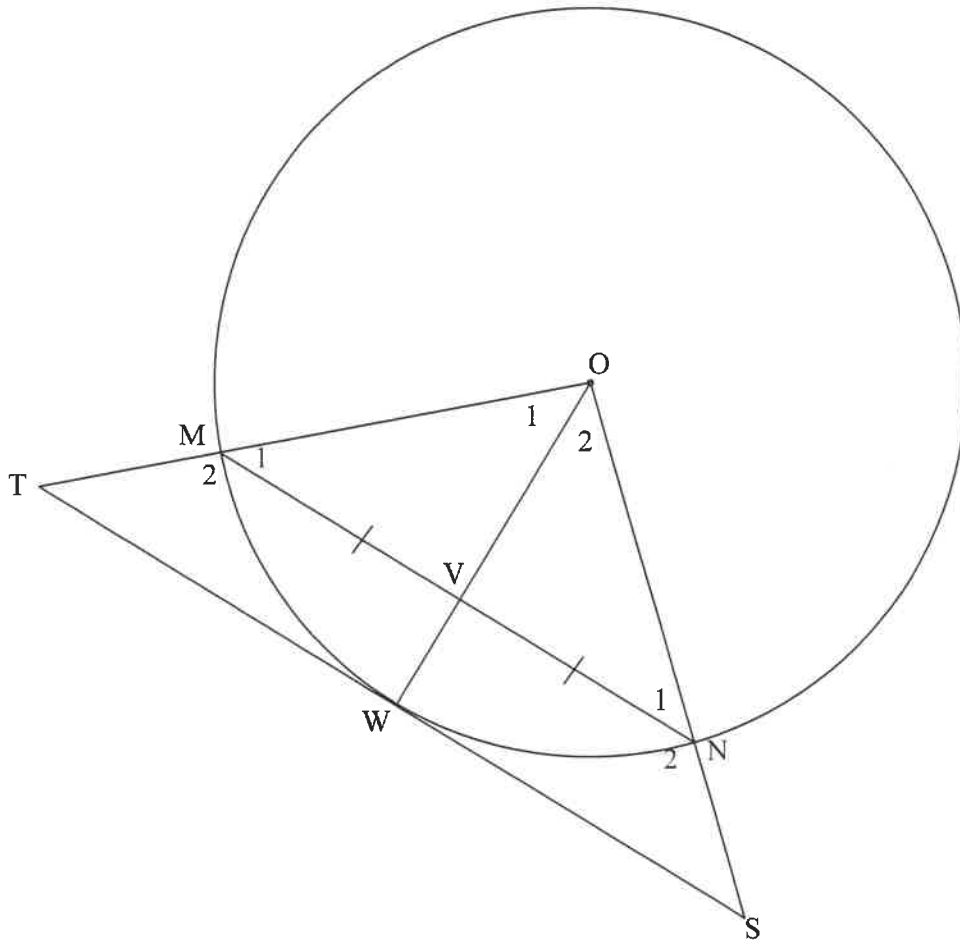
9.1.1 $FG \parallel BC$ (2)

9.1.2 $\frac{AH}{HK} = \frac{AE}{ED}$ (3)

9.2 If it is further given that $AH = 15$ and $ED = 12$, calculate the length of EK . (5)
[10]

QUESTION 10

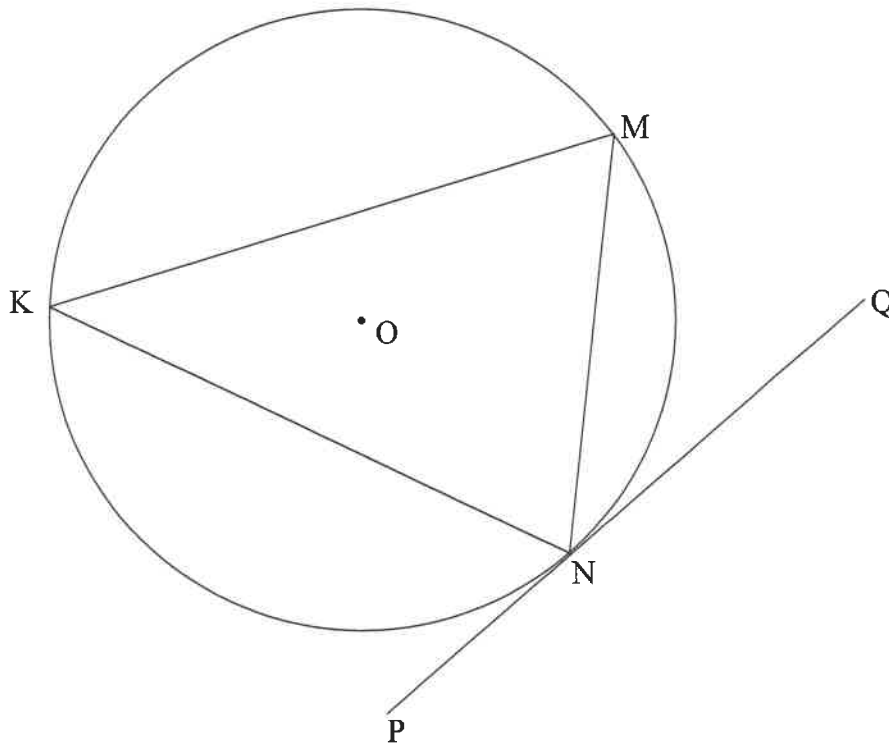
In the diagram, W is a point on the circle with centre O . V is a point on OW . Chord MN is drawn such that $MV = VN$. The tangent at W meets OM produced at T and ON produced at S .



- 10.1 Give a reason why $OV \perp MN$. (1)
 - 10.2 Prove that:
 - 10.2.1 $MN \parallel TS$ (2)
 - 10.2.2 $TMNS$ is a cyclic quadrilateral (4)
 - 10.2.3 $OS \cdot MN = 2ON \cdot WS$ (5)
- [12]**

QUESTION 11

- 11.1 In the diagram, chords KM, MN and KN are drawn in the circle with centre O. PNQ is the tangent to the circle at N.

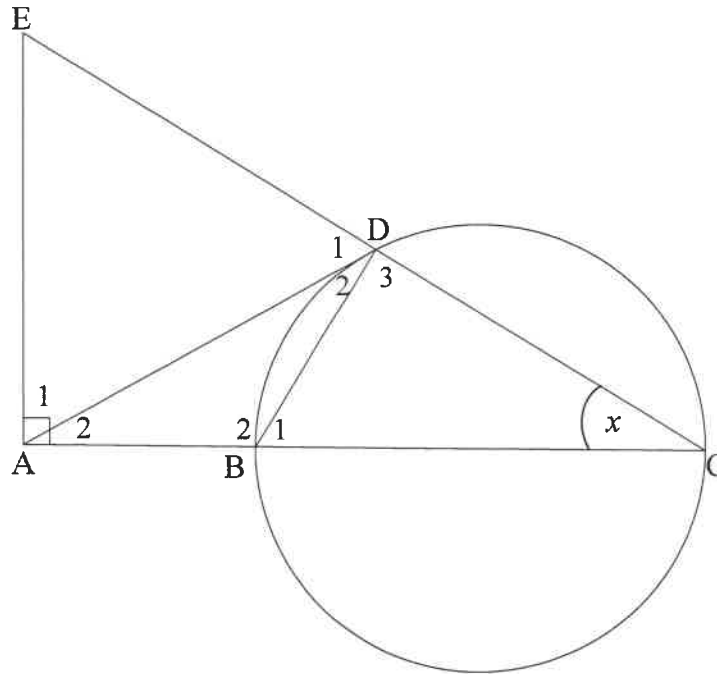


Prove the theorem which states that $\hat{MNQ} = \hat{K}$.

(5)

11.2 In the diagram, BC is a diameter of the circle. The tangent at point D on the circle meets CB produced at A. CD is produced to E such that $EA \perp AC$. BD is drawn.

Let $\hat{C} = x$.



11.2.1 Give a reason why:

- (a) $\hat{D}_3 = 90^\circ$ (1)
- (b) ABDE is a cyclic quadrilateral (1)
- (c) $\hat{D}_2 = x$ (1)

11.2.2 Prove that:

- (a) $AD = AE$ (3)
- (b) $\triangle ADB \parallel \triangle ACD$ (3)

11.2.3 It is further given that $BC = 2AB = 2r$.

- (a) Prove that $AD^2 = 3r^2$ (2)
- (b) Hence, prove that $\triangle ADE$ is equilateral. (4)

[20]

TOTAL: 150

INFORMATION SHEET: MATHEMATICS

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$A = P(1 + ni)$$

$$A = P(1 - ni)$$

$$A = P(1 - i)^n$$

$$A = P(1 + i)^n$$

$$T_n = a + (n-1)d$$

$$S_n = \frac{n}{2}[2a + (n-1)d]$$

$$T_n = ar^{n-1}$$

$$S_n = \frac{a(r^n - 1)}{r - 1}; r \neq 1$$

$$S_\infty = \frac{a}{1 - r}; -1 < r < 1$$

$$F = \frac{x[(1+i)^n - 1]}{i}$$

$$P = \frac{x[1 - (1+i)^{-n}]}{i}$$

$$f'(x) = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$$

$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$M\left(\frac{x_1 + x_2}{2}; \frac{y_1 + y_2}{2}\right)$$

$$y = mx + c$$

$$y - y_1 = m(x - x_1)$$

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

$$m = \tan \theta$$

$$(x - a)^2 + (y - b)^2 = r^2$$

$$\text{In } \triangle ABC: \quad \frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$a^2 = b^2 + c^2 - 2bc \cdot \cos A$$

$$\text{area } \triangle ABC = \frac{1}{2} ab \cdot \sin C$$

$$\sin(\alpha + \beta) = \sin \alpha \cdot \cos \beta + \cos \alpha \cdot \sin \beta$$

$$\sin(\alpha - \beta) = \sin \alpha \cdot \cos \beta - \cos \alpha \cdot \sin \beta$$

$$\cos(\alpha + \beta) = \cos \alpha \cdot \cos \beta - \sin \alpha \cdot \sin \beta$$

$$\cos(\alpha - \beta) = \cos \alpha \cdot \cos \beta + \sin \alpha \cdot \sin \beta$$

$$\cos 2\alpha = \begin{cases} \cos^2 \alpha - \sin^2 \alpha \\ 1 - 2\sin^2 \alpha \\ 2\cos^2 \alpha - 1 \end{cases}$$

$$\sin 2\alpha = 2\sin \alpha \cdot \cos \alpha$$

$$\bar{x} = \frac{\sum x}{n}$$

$$\sigma^2 = \frac{\sum_{i=1}^n (x_i - \bar{x})^2}{n}$$

$$P(A) = \frac{n(A)}{n(S)}$$

$$P(A \text{ or } B) = P(A) + P(B) - P(A \text{ and } B)$$

$$\hat{y} = a + bx$$

$$b = \frac{\sum (x - \bar{x})(y - \bar{y})}{\sum (x - \bar{x})^2}$$

| FOLLOW THESE INSTRUCTIONS CAREFULLY | VOLG HIERDIE INSTRUKSIES NOUKEURIG |
|--|---|
| 1. Clearly write your examination number and centre number in the spaces provided and attach your barcode label in the space provided. | 1. Skryf jou eksamennommer en sentrumnummer duidelik in die ruimtes soos verskaf en plak jou stafieskodeplakker in die ruimte soos verskaf. |
| 2. Remember that your own name (or the name of your school) may not appear anywhere on or in this answer book. | 2. Onthou dat jou eie naam (of die naam van jou skool) nie op of in hierdie antwoordeboek mag voorkom nie. |
| 3. No pages may be torn from this answer book. | 3. Geen bladsye mag uit hierdie antwoordeboek geskeur word nie. |
| 4. Read the instructions printed on your timetable carefully as well as any other instructions which may be given in each examination paper. | 4. Lees die instruksies wat op jou eksamenrooster gedruk is, sorgvuldig deur, asook enige ander instruksies wat in elke eksamenvraestel gegee word. |
| 5. Candidates may not retain any answer book or remove them from the examination room. | 5. Geen antwoordeboek mag deur die kandidaat behou of uit die eksamenlokaal verwyder word nie. |
| 6. Answers must be written in black/blue ink as distinctly as possible. | 6. Skryf die antwoorde so duidelik moontlik met swart/blou. |
| 7. Draw a neat line through any work/rough work that must not be marked. | 7. Trek 'n netjiese lyn deur enige werk/rofwerk wat nie nagesien moet word nie. |

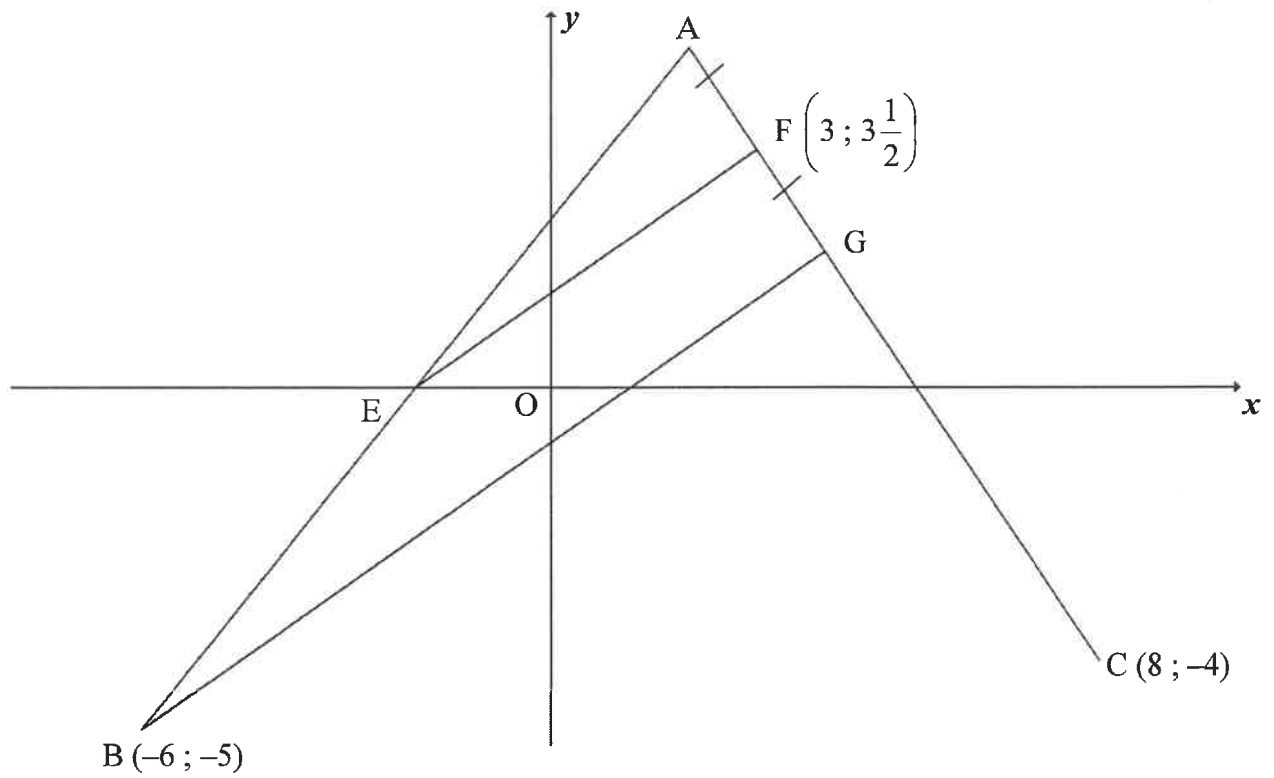
QUESTION/VRAAG 1

| | | | | | | | | | | | | |
|--|------|------|------|------|-----|------|------|------|-----|-----|------|------|
| Time for 100 m sprint (in seconds) <i>Tyd vir 100 m-naelloop (in sekondes)</i> | 10,1 | 10,2 | 10,5 | 10,9 | 11 | 11,1 | 11,2 | 11,5 | 12 | 12 | 12,2 | 12,5 |
| Distance of best long jump (in metres) <i>Afstand van beste sprong in verspring (in meter)</i> | 8 | 7,7 | 7,6 | 7,3 | 7,6 | 7,2 | 6,8 | 7 | 6,6 | 6,3 | 6,8 | 6,4 |

| | Solution/Oplissing | Marks Punte |
|-----|---------------------------|------------------------|
| 1.1 | | (3) |
| 1.2 | | (2) |
| 1.3 | | (2) |
| | | [7] |

| | Solution/<i>Oplossing</i> | Marks <i>Punte</i> |
|-------|----------------------------------|-------------------------------|
| 2.4.1 | | (1) |
| | | |
| | | |
| | | |
| 2.4.2 | | (2) |
| | | |
| | | |
| | | |
| | | |
| | | |
| | | [13] |

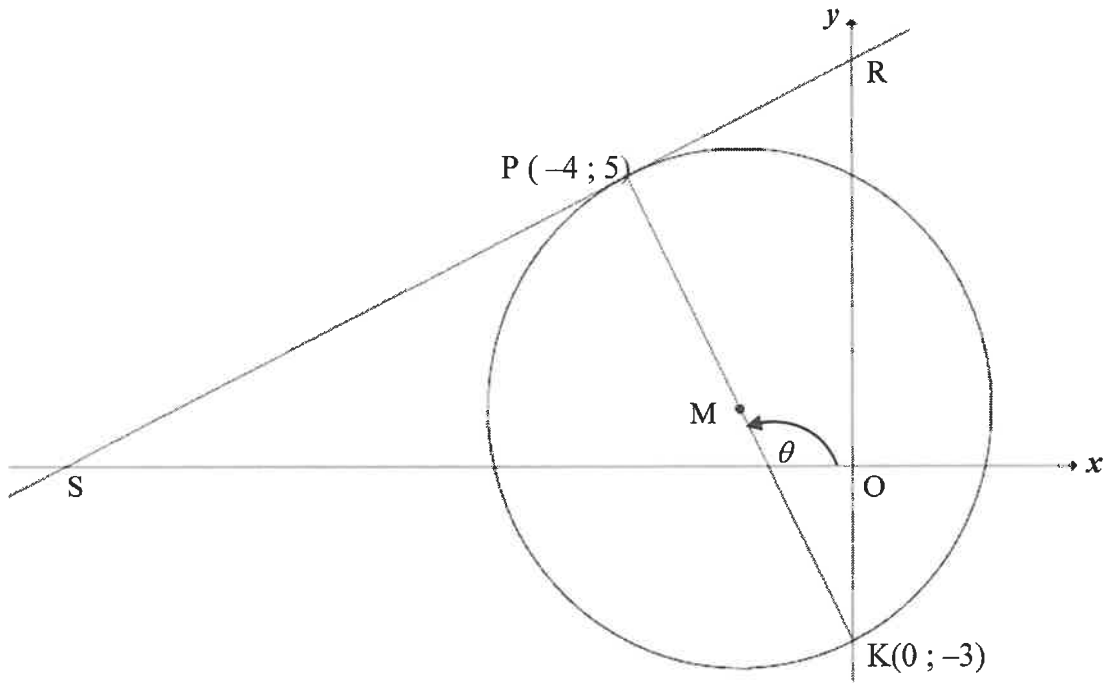
QUESTION/VRAAG 3



| | Solution/Oplissing | Marks Punte |
|-------|---------------------------|------------------------|
| 3.1.1 | | |
| | | |
| | | |
| | | |
| | | |
| | | |
| | | |
| | | |
| | | (4) |
| 3.1.2 | | |
| | | |
| | | |
| | | |
| | | |

| | Solution/Oplissing | Marks Punte |
|------------------------------|---------------------------|------------------------|
| 3.1.2 (cont./ vervolg) | | (3) |
| 3.2 | | (2) |
| 3.3 | | (4) |
| 3.4 | | (4) |
| | | [17] |

QUESTION/VRAAG 4

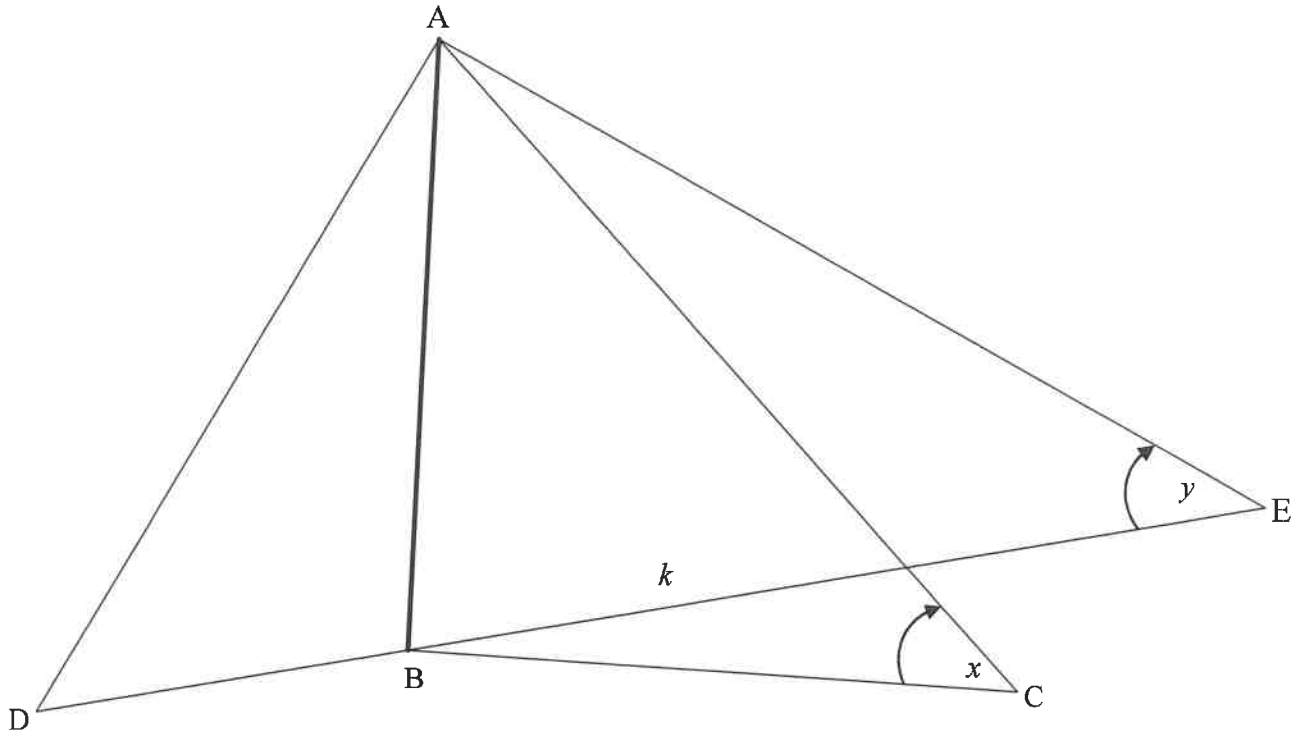


| | Solution/Oplissing | Marks Punte |
|-------|---------------------------|------------------------|
| 4.1.1 | | (4) |
| 4.1.2 | | (2) |

| | Solution/<i>Oplossing</i> | Marks <i>Punte</i> |
|-------|----------------------------------|-------------------------------|
| 4.1.3 | | (4) |
| 4.1.4 | | (3) |
| 4.1.5 | | (2) |
| 4.2 | | (3) |

| | Solution/<i>Oplossing</i> | Marks <i>Punte</i> |
|-------|----------------------------------|-------------------------------|
| 5.2.2 | | (1) |
| 5.2.3 | | (4) |
| 5.3.1 | | (2) |
| 5.3.2 | | (4) |
| | | [19] |

QUESTION/VRAAG 7

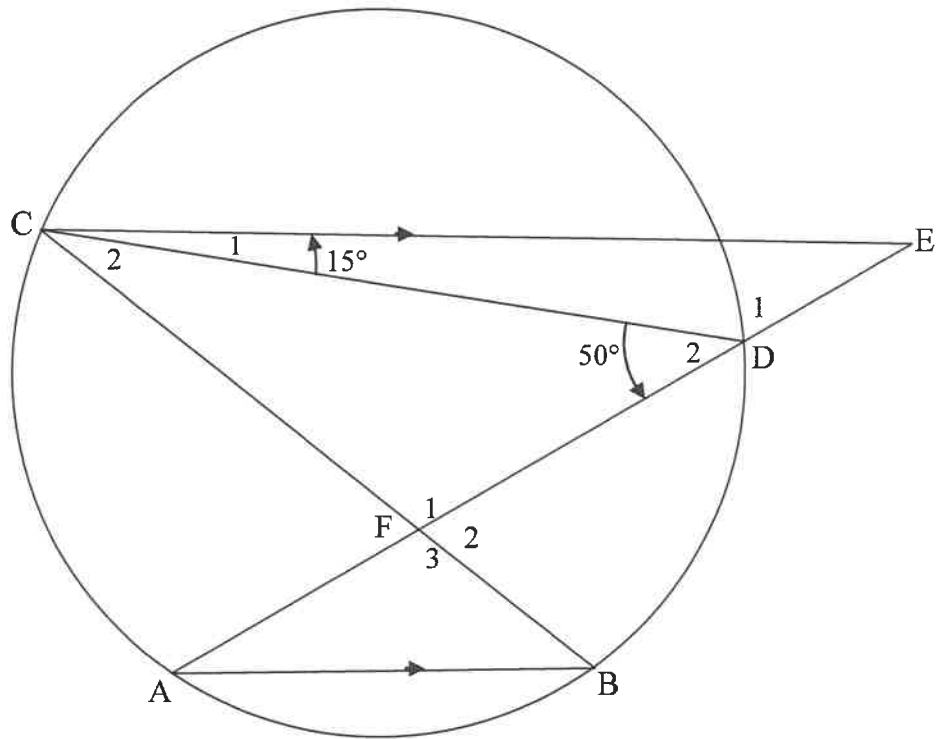


| | Solution/Oplissing | Marks Punte |
|-----|---------------------------|------------------------|
| 7.1 | | (1) |
| | | |
| | | |
| 7.2 | | (4) |
| | | |
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| | | |
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| | | |

| | Solution/<i>Oplossing</i> | Marks <i>Punte</i> |
|-----|----------------------------------|-------------------------------|
| 7.3 | | |
| | | (5) |
| | | [10] |

Give reasons for your statements in QUESTIONS 8, 9, 10 and 11.
Gee redes vir jou bewerings in VRAAG 8, 9, 10 en 11.

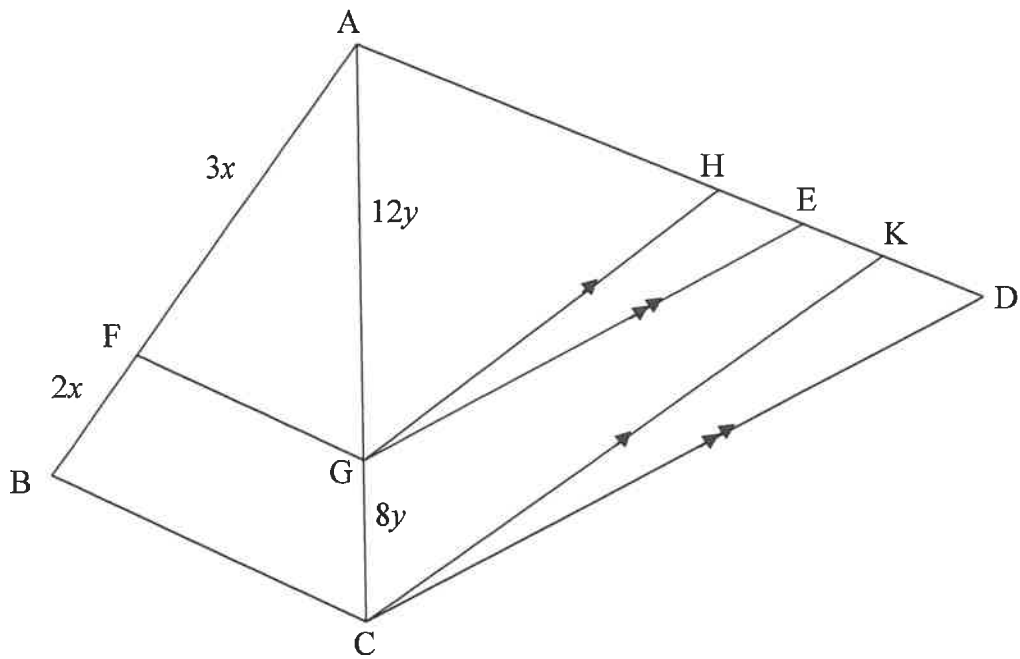
QUESTION/VRAAG 8



| | Solution/Oplissing | Marks Punte |
|-------|---------------------------|------------------------|
| 8.1.1 | | |
| | | |
| | | |
| | | |
| | | |
| | | |
| | | (3) |

| | Solution/<i>Oplossing</i> | Marks <i>Punte</i> |
|-------|----------------------------------|-------------------------------|
| 8.1.2 | | (2) |
| 8.2 | | (2) |
| | | [7] |

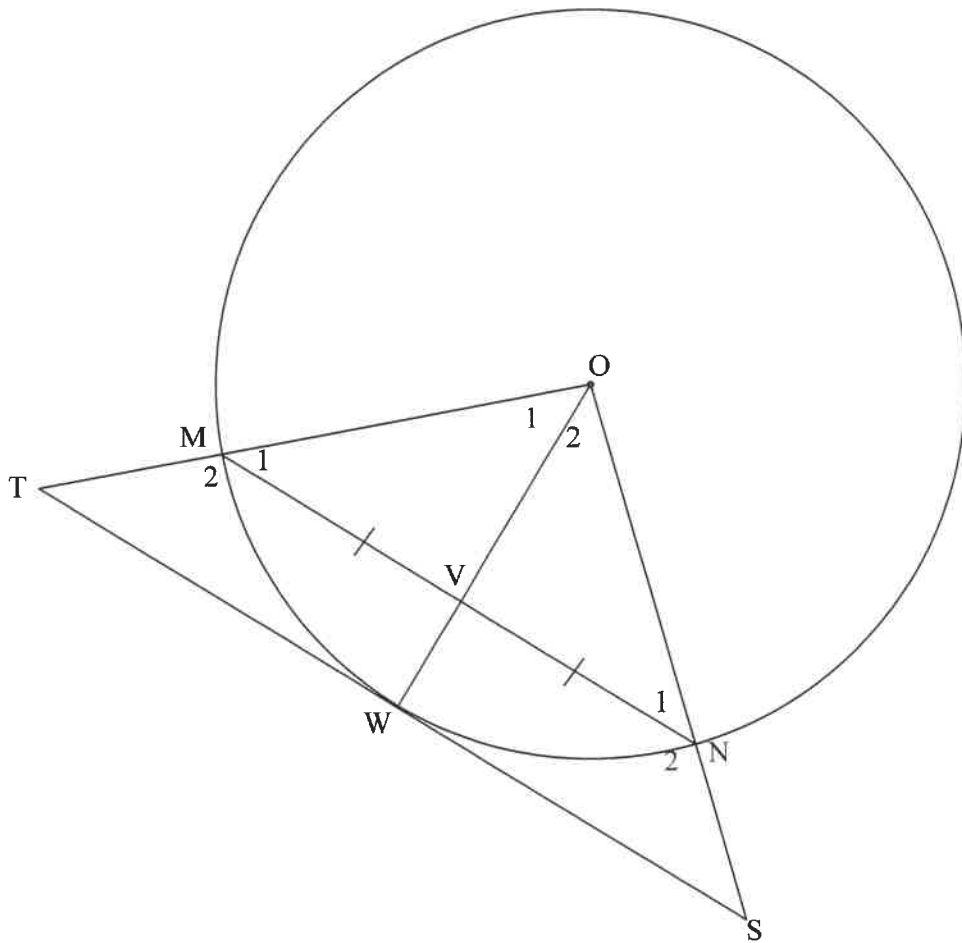
QUESTION/VRAAG 9



| | Solution/Oplissing | Marks Punte |
|-------|---------------------------|------------------------|
| 9.1.1 | | (2) |
| | | |
| | | |
| | | |
| | | |
| 9.1.2 | | (3) |
| | | |
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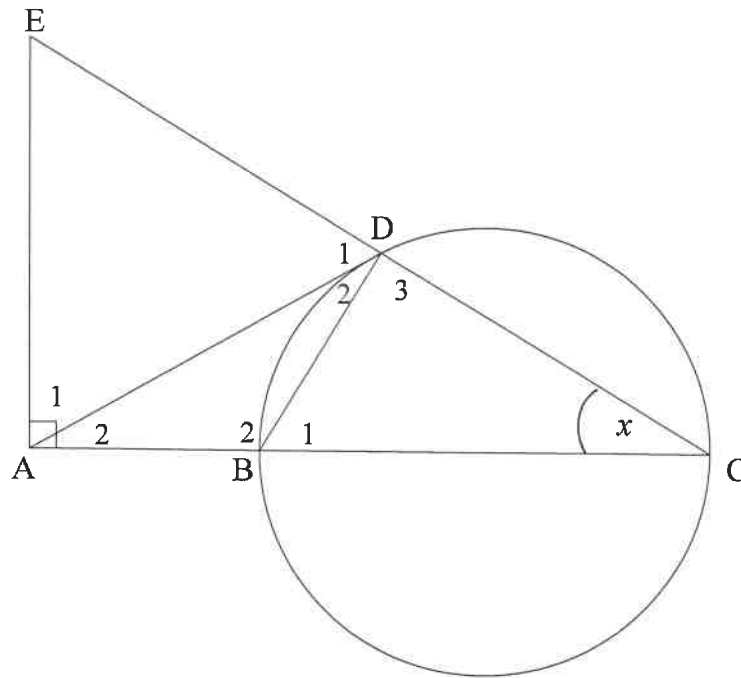
| | Solution/<i>Oplossing</i> | Marks <i>Punte</i> |
|-----|----------------------------------|-------------------------------|
| 9.2 | | |
| | | (5) |
| | | [10] |

QUESTION/VRAAG 10



| | Solution/Oplissing | Marks Punte |
|--------|---------------------------|------------------------|
| 10.1 | | (1) |
| 10.2.1 | | (2) |

11.2



| | Solution/Oplissing | Marks Punte |
|-----------|---------------------------|------------------------|
| 11.2.1(a) | | (1) |
| 11.2.1(b) | | (1) |
| 11.2.1(c) | | (1) |
| 11.2.2(a) | | (3) |



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**NATIONAL
SENIOR CERTIFICATE
*NASIONALE SENIOR
SERTIFIKAAT***

GRADE 12/*GRAAD 12*

MATHEMATICS P2/*WISKUNDE V2*

NOVEMBER 2017

MARKING GUIDELINES/*NASIENRIGLYNE*

MARKS/*PUNTE*: 150

**These marking guidelines consist of 29 pages.
*Hierdie nasienriglyne bestaan uit 28 bladsye.***

NOTE:

- If a candidate answers a question TWICE, only mark the FIRST attempt.
- If a candidate has crossed out an attempt of a question and not redone the question, mark the crossed out version.
- Consistent accuracy applies in ALL aspects of the marking guidelines. Stop marking at the second calculation error.
- Assuming answers/values in order to solve a problem is NOT acceptable.

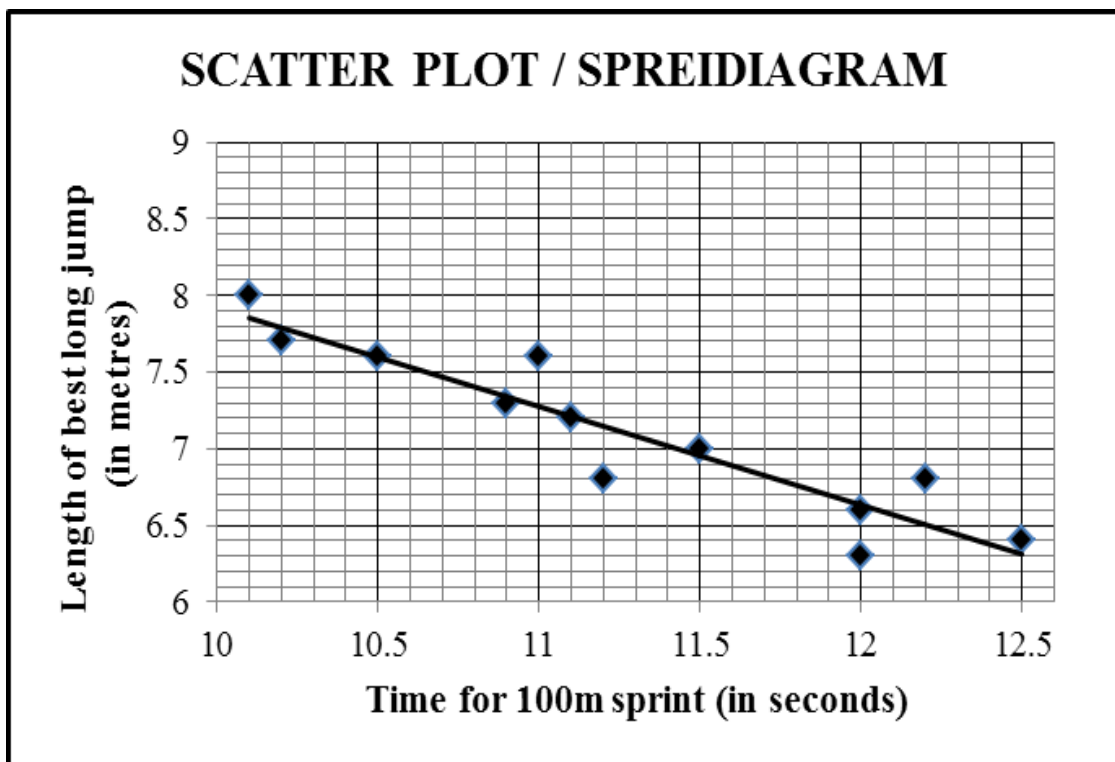
NOTA:

- *As 'n kandidaat 'n vraag TWEE KEER beantwoord, merk slegs die EERSTE poging.*
- *As 'n kandidaat 'n antwoord van 'n vraag doodtrek en nie oordoen nie, merk die doodgetrekte poging.*
- *Volgehoue akkuraatheid word in ALLE aspekte van die nasienriglyne toegepas. Hou op nasien by die tweede berekeningsfout.*
- *Aanvaar van antwoorde/waardes om 'n probleem op te los, word NIE toegelaat nie.*

| GEOMETRY | |
|-----------------|--|
| S | A mark for a correct statement (A statement mark is independent of a reason.) |
| | 'n Punt vir 'n korrekte bewering ('n Punt vir 'n bewering is onafhanklik van die rede.) |
| R | A mark for a correct reason (A reason mark may only be awarded if the statement is correct.) |
| | 'n Punt vir 'n korrekte rede ('n Punt word slegs vir die rede toegeken as die bewering korrek is.) |
| S/R | Award a mark if the statement AND reason are both correct. |
| | Ken 'n punt toe as beide die bewering EN rede korrek is. |

QUESTION/VRAAG 1

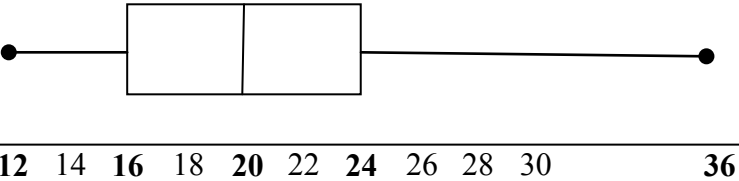
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|--|------|------|------|------|-----|------|------|------|-----|-----|------|------|
| Time for 100 m sprint (in seconds) <i>Tyd vir 100 m-naelloop (in sekondes)</i> | 10,1 | 10,2 | 10,5 | 10,9 | 11 | 11,1 | 11,2 | 11,5 | 12 | 12 | 12,2 | 12,5 |
| Distance of best long jump (in metres) <i>Afstand van beste sprong in verspring (in meter)</i> | 8 | 7,7 | 7,6 | 7,3 | 7,6 | 7,2 | 6,8 | 7 | 6,6 | 6,3 | 6,8 | 6,4 |



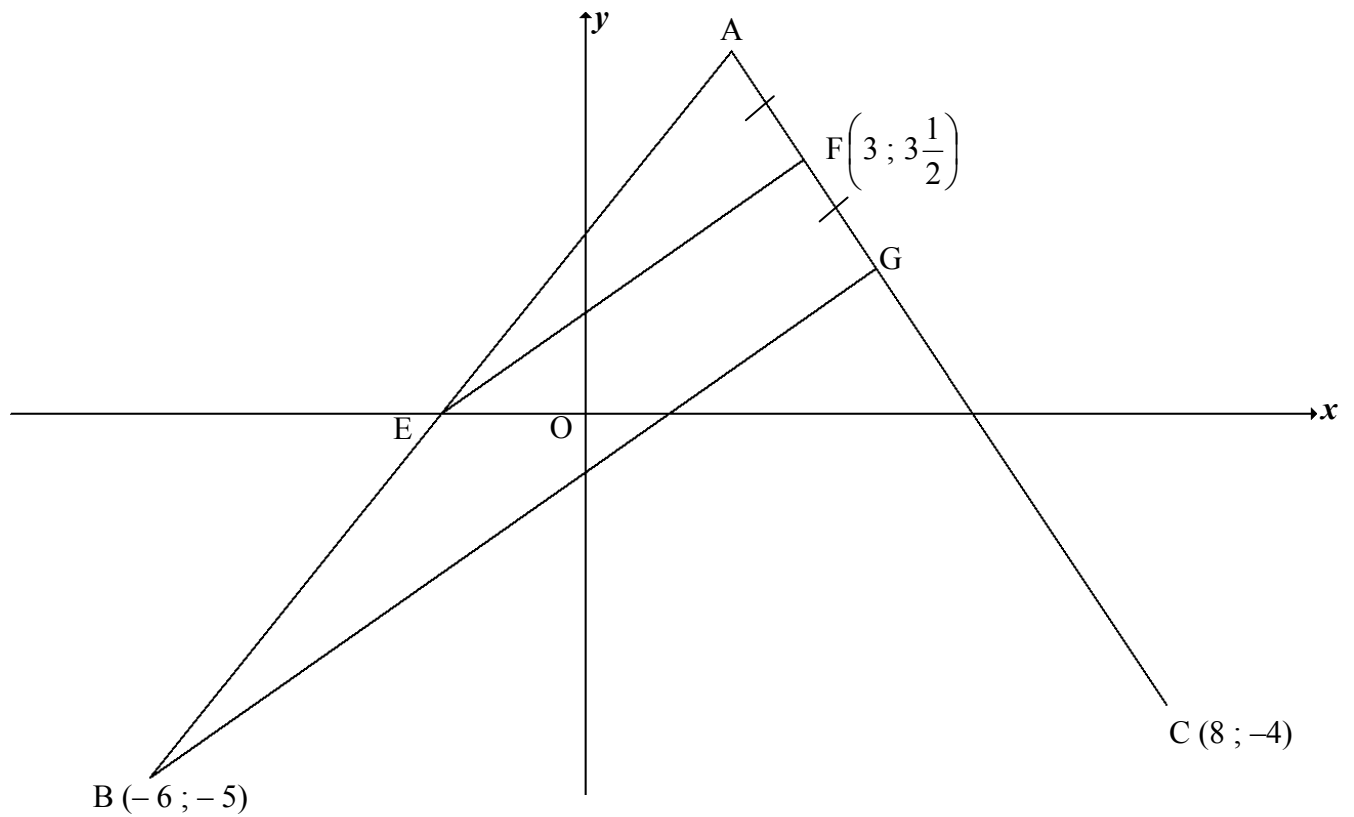
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| 1.1 | $a = 14,343\dots = 14,34$ $b = -0,642\dots = -0,64$ | ✓✓ value of a ✓ value of b (3) |
| 1.2 | $y = 14,34 - 0,64(11,7)$ $= 6,85$ OR/OF $y = 6,83$ (calculator / <i>sakrekenaar</i>) | ✓ substitution correctly ✓ answer ✓✓ answer (2) (2) |
| 1.3 | The gradient increases / <i>Die gradient neem toe</i> The point (12,3 ; 7,6) lies some distance above the current data. <i>/Die punt (12,3 ; 7,6) lê bokant die huidige data.</i> | ✓ increases/ <i>neem toe</i> ✓ reasoning in words/ <i>redenasie in woorde</i> (2) [7] |

QUESTION/VRAAG 2

| | | | | | | | | | | | |
|----|----|----|----|----|----|----|----|----|----|----|----|
| 12 | 13 | 13 | 14 | 14 | 16 | 17 | 18 | 18 | 18 | 19 | 20 |
| 21 | 21 | 22 | 22 | 23 | 24 | 25 | 27 | 29 | 30 | 36 | |

| | | |
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| 2.1.1 | $\bar{x} = \frac{472}{23}$ $\bar{x} = 20,52 \text{ seconds / sekonde}$ | ✓ $\frac{472}{23}$ ✓ answer (2) |
| 2.1.2 | $Q_1 = 16$ $Q_3 = 24$ $IQR/IKO = Q_3 - Q_1$ $= 24 - 16 = 8$ | ✓ Q_1 ✓ Q_3 ✓ answer (3) |
| 2.2 | $20,52 + 5,94 = 26,46$ $\therefore > 26,46$ $\therefore 4 \text{ girls/dogters}$ | ✓ 26,46 ✓ answer (2) |
| 2.3 |  <p>12 14 16 18 20 22 24 26 28 30 36</p> | ✓ whiskers ending at 12 & 36 ✓ $Q_1 = 16$ & $Q_3 = 24$ (box) ✓ $Q_2 = 20$ (3) |
| 2.4.1 | Girls / Meisies | ✓ answer (1) |
| 2.4.2 | Five-number summary of boys: (15 ; 21 ; 23,5 ; 26 ; 38) None of the boys / Nie een van die seuns nie 5 girls completed in less than 15 seconds which was the minimum time taken by the boys. 5 meisies voltooi in minder as 15 sekondes, wat die minimumtyd is wat die seuns geneem het. | ✓ answer ✓ reason/rede (2) [13] |

QUESTION/VRAAG 3



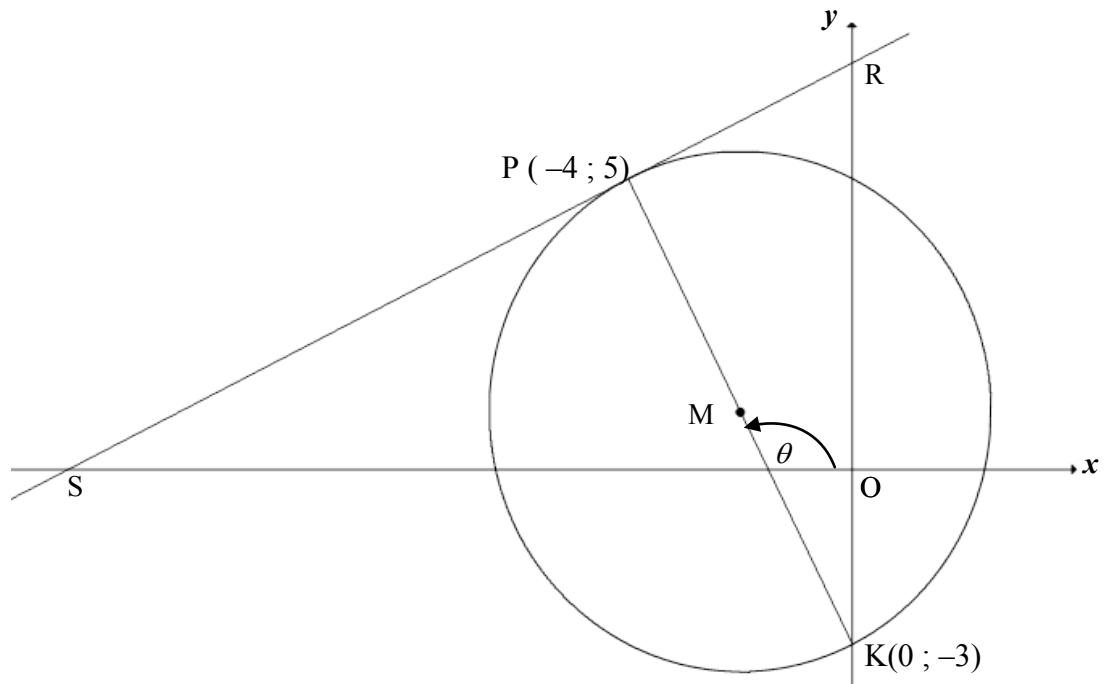
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| <p>3.1.1</p> | $m_{FC} = \frac{y_2 - y_1}{x_2 - x_1}$ $= \frac{3\frac{1}{2} - (-4)}{3 - 8}$ $= -\frac{3}{2}$ $y = mx + c$ $y = -\frac{3}{2}x + c$ $-4 = -\frac{3}{2}(8) + c \quad \text{OR/OF} \quad (y - (-4)) = -\frac{3}{2}(x - 8)$ $c = 8$ $y = -\frac{3}{2}x + 8$ $y + 4 = -\frac{3}{2}x + 12$ $y = -\frac{3}{2}x + 8$ <p>OR/OF</p> | <ul style="list-style-type: none"> ✓ substitution of (8 ; -4) & $\left(3; 3\frac{1}{2}\right)$ ✓ gradient ✓ substitution of m and (8 ; -4) ✓ equation of AC <p style="text-align: right;">(4)</p> |
|--------------|--|---|

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| | $m_{FC} = \frac{y_2 - y_1}{x_2 - x_1} = \frac{(-4) - \left(3\frac{1}{2}\right)}{8 - 3}$ $= -\frac{3}{2}$ $y = mx + c$ $3\frac{1}{2} = -\frac{3}{2}(3) + c$ $c = 8$ $y = -\frac{3}{2}x + 8$ $y - y_1 = m(x - x_1)$ $\left(y - 3\frac{1}{2}\right) = -\frac{3}{2}(x - 3)$ <p style="text-align: center;">OR/OF</p> $\left(y - 3\frac{1}{2}\right) = -\frac{3}{2}x + \frac{9}{2}$ $y = -\frac{3}{2}x + 8$ | <ul style="list-style-type: none"> ✓ substitution of $(8 ; -4)$ & $\left(3 ; 3\frac{1}{2}\right)$ ✓ gradient ✓ substitution of m and $\left(3 ; 3\frac{1}{2}\right)$ ✓ equation of AC <p style="text-align: right;">(4)</p> |
| <p>3.1.2</p> | <p>AC: $3x + 2y = 16$ and BG: $7x - 10y = 8$</p> $15x + 10y = 80$ $\underline{7x - 10y = 8}$ $22x = 88$ $x = 4$ $3(4) + 2y = 16$ $y = 2$ <p>∴ G(4 ; 2)</p> <p>OR/OF</p> <p>BG: $7x - 10y = 8$ ∴ $y = \frac{7}{10}x - \frac{8}{10}$</p> $\therefore \frac{7}{10}x - \frac{8}{10} = -\frac{3}{2}x + 8 \quad [\text{CA from 3.1.1}]$ $\frac{11}{5}x = \frac{44}{5}$ $x = 4$ $3(4) + 2y = 16$ $y = 2$ <p>∴ G(4 ; 2)</p> | <ul style="list-style-type: none"> ✓ method /metode: solving simultaneously / los gelyktydig op ✓ x coordinate ($x > 0$) ✓ y coordinate <p style="text-align: right;">(3)</p> <ul style="list-style-type: none"> ✓ method: equating metode: stel vgl's gelyk ✓ x coordinate ($x > 0$) ✓ y coordinate <p style="text-align: right;">(3)</p> |
| <p>3.2</p> | $\frac{x_A + 4}{2} = 3 \quad \text{and} \quad \frac{y_A + 2}{2} = 3\frac{1}{2}$ <p>∴ A(2 ; 5)</p> <p>OR/OF by translation/deur translasie:</p> $x_A = 3 - (4 - 3) = 2$ $y_A = 3\frac{1}{2} + (3\frac{1}{2} - 2) = 5$ <p>∴ A(2 ; 5)</p> | <ul style="list-style-type: none"> ✓ equation ito x ✓ equation ito y <p style="text-align: right;">(2)</p> <ul style="list-style-type: none"> ✓ equation ito x ✓ equation ito y <p style="text-align: right;">(2)</p> |

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| <p>3.3</p> | <p>The coordinates of the midpt of AB / <i>Die koordinaat van midpt van AB is:</i></p> $\left(\frac{2+(-6)}{2}; \frac{5+(-5)}{2}\right) = (-2 ; 0)$ <p>But the y-coordinate of E is 0 ∴ E(-2 ; 0) is the midpoint of AB ∴ EF BG [midpoint theorem/<i>middelpuntst</i> OR/OF line divides 2 sides of Δ in prop/lyn <i>verdeel 2 sye van Δ in dies verh</i>]</p> <p>OR/OF The coordinates of the midpt of AB / <i>Die koordinaat van midpt van AB is:</i></p> $\left(\frac{2+(-6)}{2}; \frac{5+(-5)}{2}\right) = (-2 ; 0)$ $AE = \sqrt{(-2-2)^2 + (0-5)^2} = \sqrt{41}$ $EB = \sqrt{(-2-(-6))^2 + (0-(-5))^2} = \sqrt{41}$ <p>∴ In ΔABG: AE = EB and AF = FG ∴ EF BG [midpoint theorem/<i>middelpuntst</i>]</p> <p>OR/OF Equation of AB:</p> $y - (-5) = \left(\frac{5-(-5)}{2-(-6)}\right)(x - (-6))$ $y + 5 = \frac{10}{8}x + \frac{15}{2} \quad \therefore y = \frac{5}{4}x + \frac{5}{2}$ <p>x-intercept of AB:</p> $0 = \frac{5}{4}x + \frac{5}{2} \quad \therefore x = -2$ <p>∴ E(-2 ; 0)</p> $m_{EF} = \frac{3\frac{1}{2} - 0}{3 - (-2)} = \frac{7}{10}$ $m_{EF} = m_{BG} = \frac{7}{10}$ <p>∴ EF BG</p> <div style="border: 1px solid black; padding: 5px; width: fit-content; margin: 10px auto;"> <p>BG: $7x - 10y = 8$ $\therefore y = \frac{7}{10}x - \frac{8}{10}$ $\therefore m_{BG} = \frac{7}{10}$</p> </div> | <ul style="list-style-type: none"> ✓ subst A & B into midpt formula ✓ y coordinate = 0 ✓ E = midpt ✓ Reason (4) <ul style="list-style-type: none"> ✓ subst A & B into midpt formula ✓ lengths of AE & EB ✓ AE = EB or E = midpt ✓ Reason (4) <ul style="list-style-type: none"> ✓ equation of AB ✓ coordinates of E ✓ gradient of EF ✓ gradient EF = gradient BG (4) |
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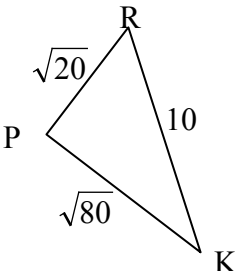
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| 3.4 | <p>Midpoint of AC = $\left(5; \frac{1}{2}\right)$</p> $\frac{x_D + (-6)}{2} = 5 \quad \text{and} \quad \frac{y_D + (-5)}{2} = \frac{1}{2}$ <p>$\therefore D(16; 6)$</p> <p>OR/OF by translation/<i>dmv translasie</i>: D(16; 6)</p> <p>OR/OF</p> $m_{BC} = \frac{-5 - (-4)}{-6 - 8} = \frac{1}{14} \quad \text{and} \quad m_{AB} = \frac{5 - (-5)}{2 - (-6)} = \frac{5}{4}$ <p>AD: $y - 5 = \frac{1}{14}(x - 2) \Rightarrow y = \frac{1}{14}x + \frac{34}{7}$</p> <p>CD: $y + 4 = \frac{5}{4}(x - 8) \Rightarrow y = \frac{5}{4}x - 14$</p> $\frac{5}{4}x - 14 = \frac{1}{14}x + \frac{34}{7}$ <p>$\therefore x = 16$ $y = 6$</p> | <p>$\checkmark\checkmark \left(5; \frac{1}{2}\right)$</p> <p>$\checkmark$ x value \checkmark y value (4)</p> <p>\checkmark method finding x \checkmark method finding y \checkmark x value \checkmark y value (4)</p> <p>$\checkmark\checkmark$ equating \checkmark x value \checkmark y value (4)</p> <p>[17]</p> |
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QUESTION/VRAAG 4



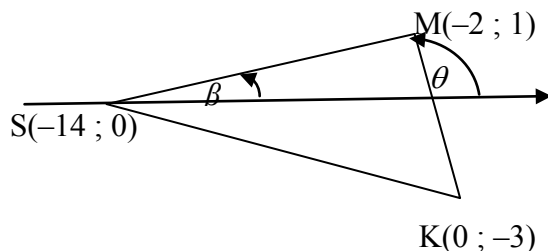
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| <p>4.1.1</p> | $m_{PK} = \frac{5 - (-3)}{-4 - 0}$ $= -2$ <p>$PK \perp SR$ [radius \perp tangent/raaklyn]</p> $\therefore m_{PK} \times m_{RS} = -1$ $\therefore m_{RS} = \frac{1}{2}$ | <ul style="list-style-type: none"> ✓ substitution P & K into gradient formula ✓ gradient of PK ✓ $PK \perp SR$ OR $r \perp$ tangent ✓ answer <p style="text-align: right;">(4)</p> |
| <p>4.1.2</p> | $y = \frac{1}{2}x + c$ $5 = \frac{1}{2}(-4) + c \quad \mathbf{OR/OR} \quad (y - 5) = \frac{1}{2}(x - (-4))$ $c = 7 \quad (y - 5) = \frac{1}{2}x + 2$ $y = \frac{1}{2}x + 7 \quad y = \frac{1}{2}x + 7$ | <ul style="list-style-type: none"> ✓ substitution of m and P ✓ equation <p style="text-align: right;">(2)</p> |

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| <p>4.1.3</p> | $M\left(\frac{-4+0}{2}; \frac{5+(-3)}{2}\right)$ $\therefore M(-2; 1)$ $r^2 = (x_2 - x_1)^2 + (y_2 - y_1)^2$ $r^2 = (-2 + 4)^2 + (1 - 5)^2$ $\therefore r^2 = 20$ $\therefore (x + 2)^2 + (y - 1)^2 = 20 \text{ or } (\sqrt{20})^2$ <p>OR/OF</p> $M\left(\frac{-4+0}{2}; \frac{5+(-3)}{2}\right) \therefore M(-2; 1)$ $(x + 2)^2 + (y - 1)^2 = r^2$ $(-4 + 2)^2 + (5 - 1)^2 = r^2$ $\therefore r^2 = 20$ $\therefore (x + 2)^2 + (y - 1)^2 = 20 \text{ or } (\sqrt{20})^2$ <p>OR/OF</p> $M\left(\frac{-4+0}{2}; \frac{5+(-3)}{2}\right) \therefore M(-2; 1)$ $PK = \sqrt{(-4 - 0)^2 + (5 - (-3))^2} = \sqrt{80}$ $r = \frac{\sqrt{80}}{2} = \sqrt{20}$ $\therefore (x + 2)^2 + (y - 1)^2 = 20 \text{ or } (\sqrt{20})^2$ | <p>✓ x value of M ✓ y value of M</p> <p>✓ $r^2 = 20$</p> <p>✓ equation (4)</p> <p>✓✓ M (- 2 ; 1)</p> <p>$r^2 = 20$</p> <p>✓ equation (4)</p> <p>✓✓ M (- 2 ; 1)</p> <p>$r^2 = 20$</p> <p>✓ equation (4)</p> |
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| <p>4.1.4</p> | <p> $\tan \theta = m_{PK} = -2$ $\therefore \theta = 180^\circ - 63,43^\circ$ $= 116,57^\circ$ $\hat{P}KR = 116,57^\circ - 90^\circ$ [ext \angle of ΔMOK] $= 26,57^\circ$ OR/OF </p>  <p> <u>In ΔRPK:</u> $PK = \sqrt{(0 - (-4))^2 + (-3 - 5)^2} = \sqrt{80}$ $PR = \sqrt{(-4 - 0)^2 + (5 - 7)^2} = \sqrt{20}$ $RK = 10$ $\cos \hat{P}KR = \frac{PK^2 + KR^2 - PR^2}{2 \cdot PK \cdot KR} = \frac{(\sqrt{80})^2 + (10)^2 - (\sqrt{20})^2}{2(\sqrt{80})(10)}$ $= \frac{2\sqrt{5}}{5}$ $\hat{P}KR = 26,57^\circ$ OR/OF </p> <p> $\sin \hat{P}KR = \frac{\sqrt{20}}{10}$ OR/OF $\cos \hat{P}KR = \frac{\sqrt{80}}{10}$ $\hat{P}KR = 26,57^\circ$ $\hat{P}KR = 26,57^\circ$ </p> <p> OR/OF $\tan \hat{P}KR = \frac{\sqrt{20}}{\sqrt{80}}$ $\hat{P}KR = 26,57^\circ$ </p> | <p> $\checkmark \tan \theta = -2$ \checkmark size of θ \checkmark answer (3) </p> <p> \checkmark lengths of PK, PR & RK </p> <p> \checkmark correct values into cos rule </p> <p> \checkmark answer (3) </p> <p> \checkmark lengths of sides \checkmark ratio \checkmark answer (3) </p> <p> \checkmark lengths of sides \checkmark ratio \checkmark answer (3) </p> |
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| 4.1.5 | <p>RS tangent at K(0 ; - 3)</p> $\therefore m_{PS} = m_{\text{tang}} = \frac{1}{2}$ $\therefore y = \frac{1}{2}x - 3$ <p>OR/OF</p> $m_{PK} = \frac{1-5}{-2+4} = -2$ $m_{PK} \times m_{\text{tang}} = -1 \quad [\text{radius } \perp \text{ tangent/raaklyn}]$ $\therefore m_{\text{tang}} = \frac{1}{2}$ $\therefore y = \frac{1}{2}x - 3$ | <p>✓ gradient</p> <p>✓ equation</p> <p>(2)</p> <p>✓ gradient</p> <p>✓ equation</p> <p>(2)</p> |
| 4.2 | <p>$t \in (-3 ; 7)$</p> <p>OR/OF</p> $-3 < t < 7$ | <p>✓ - 3 (A)</p> <p>✓ 7 (CA from 4.1.2)</p> <p>✓ correct inequality</p> <p>(3)</p> <p>✓ - 3 (A)</p> <p>✓ 7 (CA from 4.1.2)</p> <p>✓ correct inequality</p> <p>(3)</p> |
| 4.3 | <p>RS: $y = \frac{1}{2}x + 7 \quad \therefore S(-14 ; 0)$</p> $SP = \sqrt{(-14 - (-4))^2 + (0 - 5)^2} = \sqrt{100 + 25} = \sqrt{125}$ $\text{Area } \triangle SMK = \frac{1}{2} \cdot MK \cdot SP$ $= \frac{1}{2} (\sqrt{20})(\sqrt{125})$ $= 25 \text{ square units}$ | <p>✓ coordinates of S</p> <p>✓ length of SP</p> <p>✓ correct base & height into Area rule</p> <p>✓ correct substitution</p> <p>✓ answer</p> <p>(5)</p> |

OR/OF



Let β = inclination of SM/ *inklinasie van SM*

RS: $y = \frac{1}{2}x + 7 \quad \therefore S(-14; 0)$

$SM = \sqrt{(-14 - (-2))^2 + (0 - 1)^2} = \sqrt{145}$

$\tan \beta = \frac{1 - 0}{-2 - (-14)} = \frac{1}{12} \quad \therefore \beta = 4,76^\circ$

$\therefore \hat{SMK} = 116,57^\circ - 4,76^\circ \quad [\text{ext } \angle \text{ of } \Delta]$
 $= 111,81^\circ$

Area $\Delta SMK = \frac{1}{2}(SM)(MK) \cdot \sin \hat{SMK}$
 $= \frac{1}{2}(\sqrt{145})(\sqrt{20}) \cdot \sin 111,81^\circ$
 $= 24,9985 = 25 \text{ square units}$

✓ coordinates of S

✓ length of SM

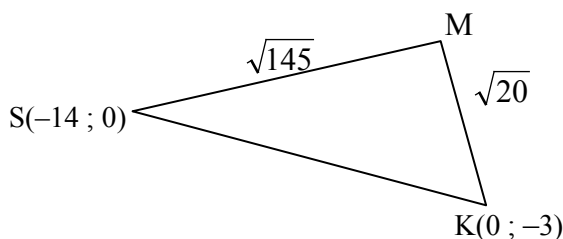
✓ size of/grootte v \hat{SMK}

✓ correct substitution into area rule

✓ answer

(5)

OR/OF



RS: $y = \frac{1}{2}x + 7 \quad \therefore S(-14; 0)$

$SK = \sqrt{(-14 - 0)^2 + (0 + 3)^2} = \sqrt{205}$

$\cos \hat{SMK} = \frac{(\sqrt{145})^2 + (\sqrt{20})^2 - (\sqrt{205})^2}{2(\sqrt{145})(\sqrt{20})} = -\frac{2\sqrt{29}}{29}$

$\hat{SMK} = 111,80^\circ$

Area $\Delta SMK = \frac{1}{2}(SM)(MK) \cdot \sin \hat{SMK}$
 $= \frac{1}{2}(\sqrt{145})(\sqrt{20}) \cdot \sin 111,81^\circ$
 $= 24,9985 = 25 \text{ square units}$

✓ coordinates of S

✓ length of SK

✓ size of/grootte v \hat{SMK}

✓ correct substitution into area rule

✓ answer

(5)

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| | <p>OR/OF</p> <p>Produce KS to T</p> <p>RS: $y = \frac{1}{2}x + 7 \quad \therefore S(-14; 0)$</p> <p>$SK = \sqrt{(-14 - 0)^2 + (0 + 3)^2} = \sqrt{205}$</p> <p>$SM = \sqrt{(-14 - (-2))^2 + (0 - 1)^2} = \sqrt{145}$</p> <p>$m_{SK} = -\frac{3}{14} \Rightarrow T\hat{S}O = 167,91^\circ$</p> <p>$m_{SM} = \frac{1}{12} \Rightarrow M\hat{S}O = 4,76^\circ$</p> <p>$M\hat{S}K = 180^\circ - 167,91^\circ + 4,76^\circ = 16,85^\circ$</p> <p>Area $\Delta SMK = \frac{1}{2}(SM)(SK) \cdot \sin M\hat{S}K$</p> <p>$= \frac{1}{2}(\sqrt{145})(\sqrt{205}) \cdot \sin 16,85^\circ$</p> <p>$= 24,9985 = 25 \text{ square units}$</p> | <p>✓ coordinates of S</p> <p>✓ length of SK & SM</p> <p>✓ size of /grootte v $M\hat{S}K$</p> <p>✓ correct substitution into area rule</p> <p>✓ answer</p> <p>(5)</p> |
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QUESTION/VRAAG 5

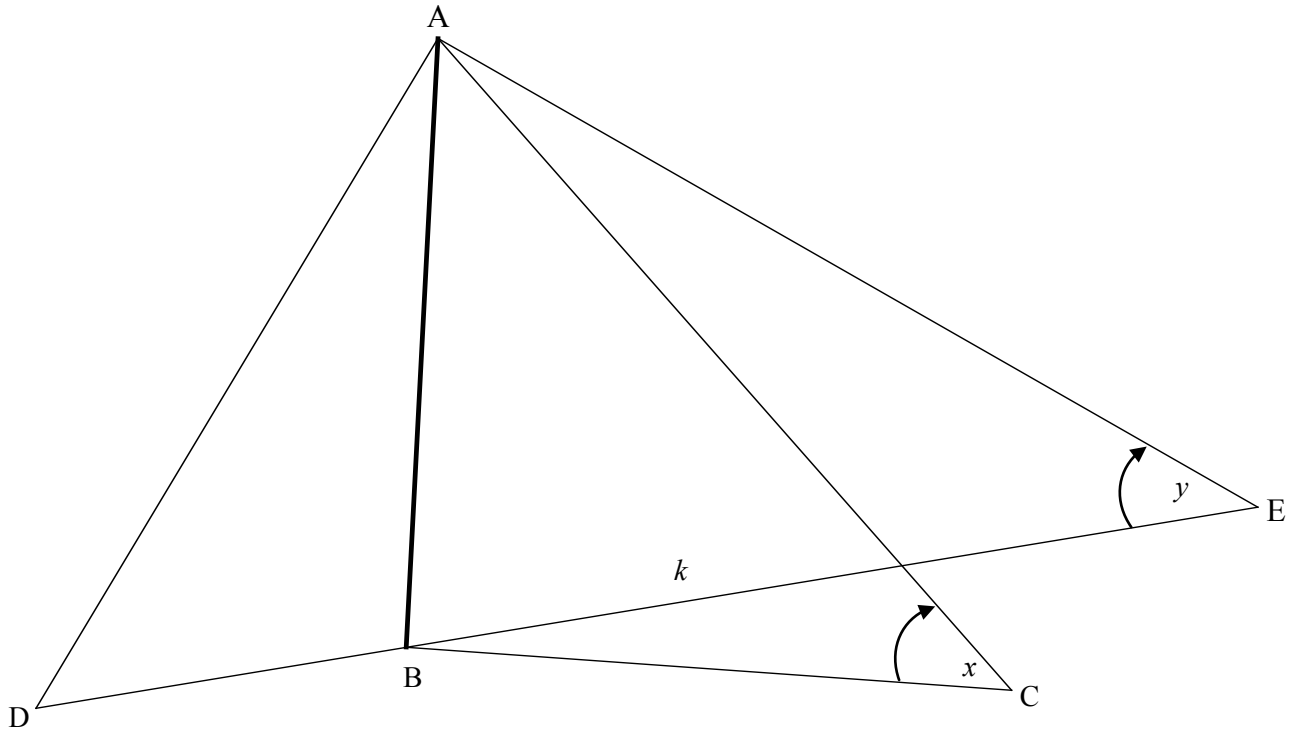
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| 5.1 | $\frac{\sin(A - 360^\circ) \cdot \cos(90^\circ + A)}{\cos(90^\circ - A) \cdot \tan(-A)}$ $= \frac{\sin A(-\sin A)}{\sin A(-\tan A)}$ $= \frac{\sin A}{\left(\frac{\sin A}{\cos A}\right)}$ $= \cos A$ | <ul style="list-style-type: none"> ✓ sin A ✓ -sin A ✓ sin A ✓ -tan A ✓ $\tan A = \frac{\sin A}{\cos A}$ ✓ answer | (6) |
| 5.2.1 | $t^2 = (\sqrt{34})^2 - (3)^2$ $\therefore t = -5$ | <ul style="list-style-type: none"> ✓ substitution ✓ answer | (2) |
| 5.2.2 | $\tan \beta = \frac{-5}{3}$ | <ul style="list-style-type: none"> ✓ correct ratio | (1) |
| 5.2.3 | $\cos 2\beta = 2 \cos^2 \beta - 1$ $= 2 \left(\frac{3}{\sqrt{34}} \right)^2 - 1$ $= 2 \left(\frac{9}{34} \right) - 1$ $= -\frac{16}{34} \text{ OR } -\frac{8}{17}$ <p>OR/OF</p> $\cos 2\beta = 1 - 2 \sin^2 \beta$ $= 1 - 2 \left(-\frac{5}{\sqrt{34}} \right)^2$ $= 1 - 2 \left(\frac{25}{34} \right)$ $= -\frac{16}{34} \text{ OR } -\frac{8}{17}$ <p>OR/OF</p> $\cos 2\beta = \cos^2 \beta - \sin^2 \beta$ $= \left(\frac{3}{\sqrt{34}} \right)^2 - \left(-\frac{5}{\sqrt{34}} \right)^2$ $= \frac{9}{34} - \frac{25}{34}$ $= -\frac{16}{34} \text{ OR } -\frac{8}{17}$ | <ul style="list-style-type: none"> ✓ compound formula ✓ substitution ✓ simplification ✓ answer | (4) |
| | | <ul style="list-style-type: none"> ✓ compound formula ✓ substitution ✓ simplification ✓ answer | (4) |
| | | <ul style="list-style-type: none"> ✓ compound formula ✓ substitution ✓ simplification ✓ answer | (4) |

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| 5.3.1 | $\begin{aligned} \text{LHS} &= \sin(A + B) - \sin(A - B) \\ &= \sin A \cdot \cos B + \cos A \cdot \sin B - (\sin A \cdot \cos B - \cos A \cdot \sin B) \\ &= \sin A \cdot \cos B + \cos A \cdot \sin B - \sin A \cdot \cos B + \cos A \cdot \sin B \\ &= 2\cos A \cdot \sin B \\ &= \text{RHS} \end{aligned}$ | ✓ compound formula ✓ compound formula (2) |
| 5.3.2 | $\begin{aligned} \sin 77^\circ - \sin 43^\circ &= \sin(60^\circ + 17^\circ) - \sin(60^\circ - 17^\circ) \\ &= 2\cos 60^\circ \cdot \sin 17^\circ \\ &= 2 \times \frac{1}{2} \times \sin 17^\circ \\ &= \sin 17^\circ \end{aligned}$ <p>OR/OF</p> $\begin{aligned} \sin 77^\circ - \sin 43^\circ &= \sin(60^\circ + 17^\circ) - \sin(60^\circ - 17^\circ) \\ &= (\sin 60^\circ \cos 17^\circ + \cos 60^\circ \sin 17^\circ) - \\ &\quad (\sin 60^\circ \cos 17^\circ - \cos 60^\circ \sin 17^\circ) \\ &= \frac{\sqrt{3}}{2} \cos 17^\circ + \frac{1}{2} \sin 17^\circ - \frac{\sqrt{3}}{2} \cos 17^\circ + \frac{1}{2} \sin 17^\circ \\ &= \sin 17^\circ \end{aligned}$ | ✓ $60^\circ + 17^\circ$ ✓ $60^\circ - 17^\circ$ ✓ simplify ✓ $\frac{1}{2}$ (4) ✓ $60^\circ + 17^\circ$ ✓ $60^\circ - 17^\circ$ ✓ expansion ✓ $\frac{1}{2}$ (4) [19] |

QUESTION/VRAAG 6

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| <p>6.1</p> | | <ul style="list-style-type: none"> ✓ $(-90^\circ ; -3)$ ✓ $(0 ; -1)$ ✓ x – intercepts: -210° & 30° ✓ shape <p style="text-align: right;">(4)</p> |
| <p>6.2</p> | $\cos 2x = 2 \sin x - 1$ $1 - 2 \sin^2 x = 2 \sin x - 1$ $2 \sin^2 x + 2 \sin x - 2 = 0$ $\sin^2 x + \sin x - 1 = 0$ $\sin x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$ $= \frac{-1 \pm \sqrt{1^2 - 4(1)(-1)}}{2(1)}$ $\sin x = \frac{-1 + \sqrt{5}}{2}, \text{ since } \sin x = \frac{-1 - \sqrt{5}}{2} < -1 \text{ has no solution}$ | <ul style="list-style-type: none"> ✓ $\cos 2x = 1 - 2 \sin^2 x$ ✓ standard form ✓ using quadratic formula ✓ substitution into quadratic formula <p style="text-align: right;">(4)</p> |
| <p>6.3</p> | $\sin x = \frac{-1 + \sqrt{5}}{2} = 0,618\dots$ <p>Reference $\angle = 38,17^\circ$</p> <p>$\therefore x = 38,17^\circ + k \cdot 360^\circ$ or $x = 141,83^\circ + k \cdot 360^\circ ; k \in \mathbb{Z}$</p> <p>$\therefore x = 38,17^\circ$ or $-218,17^\circ$</p> <p>$y = 0,24$</p> <p>\therefore Points of intersection/snyppunte: $(38,17^\circ ; 0,24)$ and $(-218,17^\circ ; 0,24)$</p> | <ul style="list-style-type: none"> ✓ $38,17^\circ$ ✓ $141,83^\circ$ ✓ $-218,17^\circ$ ✓ $0,24$ <p style="text-align: right;">(4) [12]</p> |

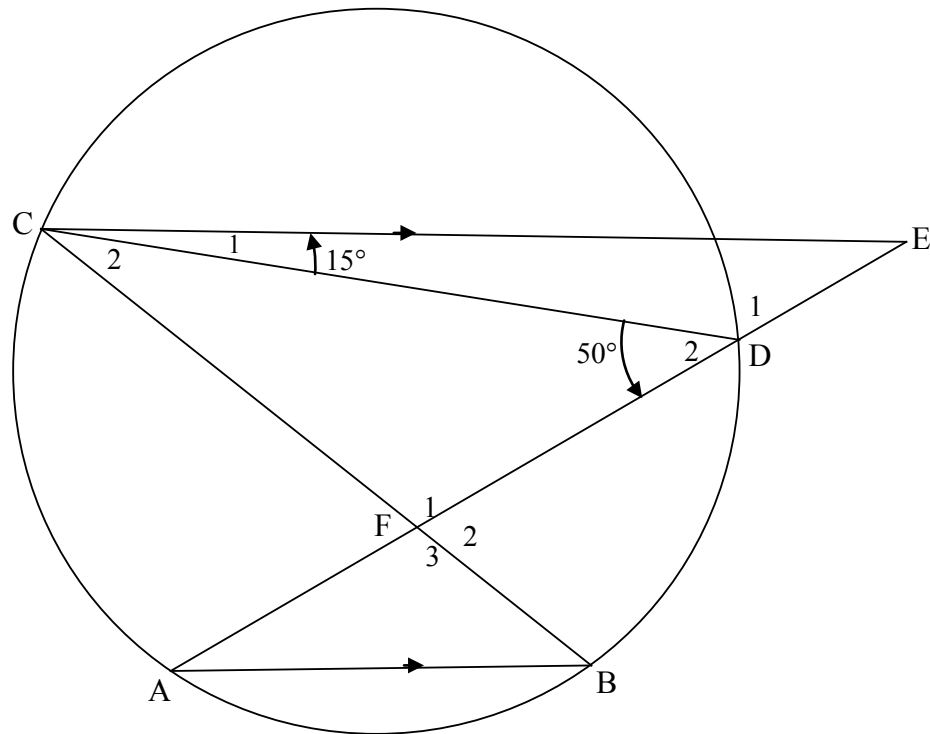
QUESTION/VRAAG 7



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| 7.1 | $\hat{A}BC = 90^\circ$ | ✓ answer (1) |
| 7.2 | <p>In $\triangle ABE$:</p> $\frac{AB}{BE} = \tan y$ $AB = k \tan y$ <p>In $\triangle ABC$:</p> $\frac{AB}{AC} = \sin x$ $AC = \frac{AB}{\sin x}$ $= \frac{k \tan y}{\sin x}$ | <p>✓ correct ratio ✓ value AB</p> <p>✓ correct ratio ✓ AC as subject and substitution</p> <p>(4)</p> |

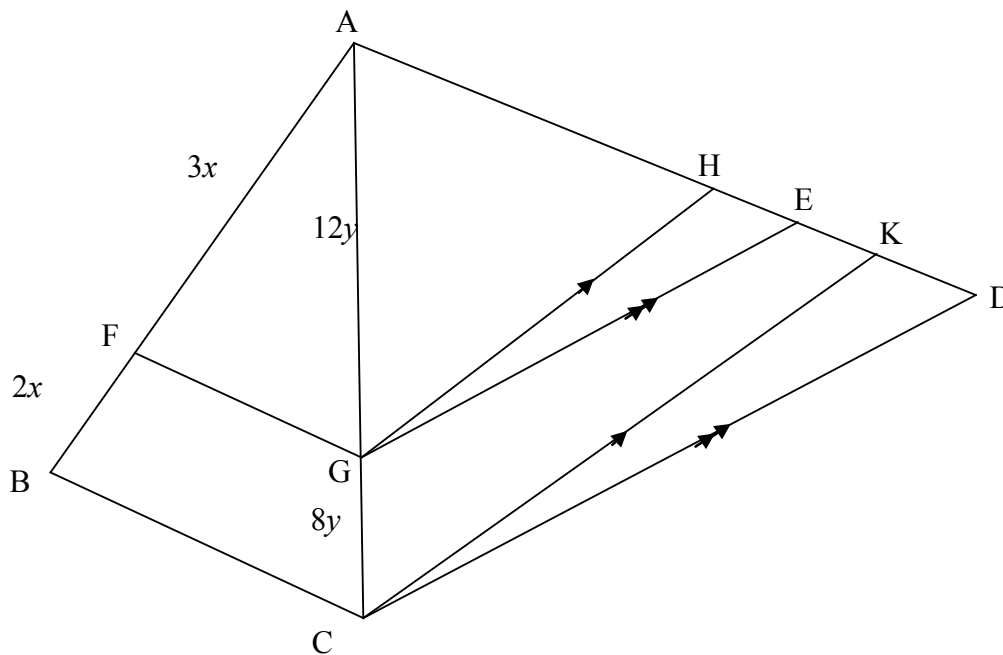
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| 7.3 | $\hat{A}DC = \hat{A}CD = \frac{180^\circ - 2x}{2} = 90^\circ - x$ $\frac{DC}{\sin 2x} = \frac{AC}{\sin(90^\circ - x)}$ $\frac{DC}{2 \sin x \cos x} = \frac{AC}{\cos x}$ $DC = \frac{AC(2 \sin x \cos x)}{\cos x}$ $= \frac{k \tan y}{\sin x} \cdot \frac{2 \sin x \cos x}{\cos x}$ $= 2k \tan y$ <p>OR/OF</p> $DC^2 = AD^2 + AC^2 - 2AD \cdot AC \cos 2x$ $= AC^2 + AC^2 - 2AC^2 \cos 2x$ $= 2AC^2(1 - \cos 2x)$ $= 2AC^2(1 - 1 + \sin^2 x)$ $= 4AC^2 \sin^2 x$ $DC = 2AC \cdot \sin x$ $= 2 \left(\frac{k \cdot \tan y}{\sin x} \right) \cdot \sin x$ $= 2k \cdot \tan y$ <p>OR/OF</p> $DC^2 = AD^2 + AC^2 - 2AD \cdot AC \cos 2x$ $= 2 \left(\frac{k \tan y}{\sin x} \right)^2 - 2 \left(\frac{k \tan y}{\sin x} \right)^2 \cos 2x$ $= \frac{2k^2 \tan^2 y}{\sin^2 x} - \frac{2k^2 \tan^2 y}{\sin^2 x} (1 - 2 \sin^2 x)$ $= \frac{2k^2 \tan^2 y}{\sin^2 x} - \frac{2k^2 \tan^2 y}{\sin^2 x} + 4k^2 \tan^2 y$ $DC = \sqrt{4k^2 \tan^2 y}$ $= 2k \tan y$ | <ul style="list-style-type: none"> ✓ $90^\circ - x$ ✓ subst into sine rule ✓ $2 \sin x \cos x$ ✓ $\cos x$ ✓ substitution (5) ✓ substitution into cos rule ✓ factorisation ✓ $1 - 2 \sin^2 x$ ✓ DC ito AC and $\sin x$ ✓ substitution (5) ✓ correct cos rule ✓ substitution ✓ $1 - 2 \sin^2 x$ ✓ squaring and multiplication ✓ $\sqrt{4k^2 \tan^2 y}$ (5) <p style="text-align: right;">[10]</p> |
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QUESTION/VRAAG 8



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| <p>8.1.1</p> | <p>$\hat{E} = 50^\circ - 15^\circ = 35^\circ$ [ext \angle of Δ/buite \angle van Δ] $\hat{A} = 35^\circ$ [alt \angles / verwiss \anglee; CE AB]</p> <p>OR/OF $\hat{E} = 180^\circ - (130^\circ + 15^\circ) = 35^\circ$ [str line; \angles of Δ/rt lyn; \anglee van Δ] $\hat{A} = 35^\circ$ [alt \angles / verwiss \anglee; CE AB]</p> <p>OR/OF $\hat{B} = 50^\circ$ [\angles in same segment/\anglee in dieselfde segment] $\hat{C}_2 + 15^\circ = 50^\circ$ [alt \angles / verwiss \anglee; CE AB] $\therefore \hat{C}_2 = 35^\circ$ $\hat{A} = 35^\circ$ [\angles in same segment/\anglee in dieselfde segment]</p> | <p>✓ S ✓ S ✓ R (3)</p> <p>✓ S ✓ S ✓ R (3)</p> <p>✓ S ✓ S ✓ R (3)</p> |
| <p>8.1.2</p> | <p>$\hat{C}_2 = 35^\circ$ [\angles in same segment/\anglee in dieselfde segment]</p> | <p>✓ S ✓ R (2)</p> |
| <p>8.2</p> | <p>$\hat{C}_2 = \hat{E}$ [from 8.1.1 and 8.1.2] \therefore CF is a tangent to the circle [converse tan chord theorem] \therefore CF is 'n raaklyn aan die sirkel [omgekeerde raakl koordst]</p> | <p>✓ S ✓ R (2) [7]</p> |

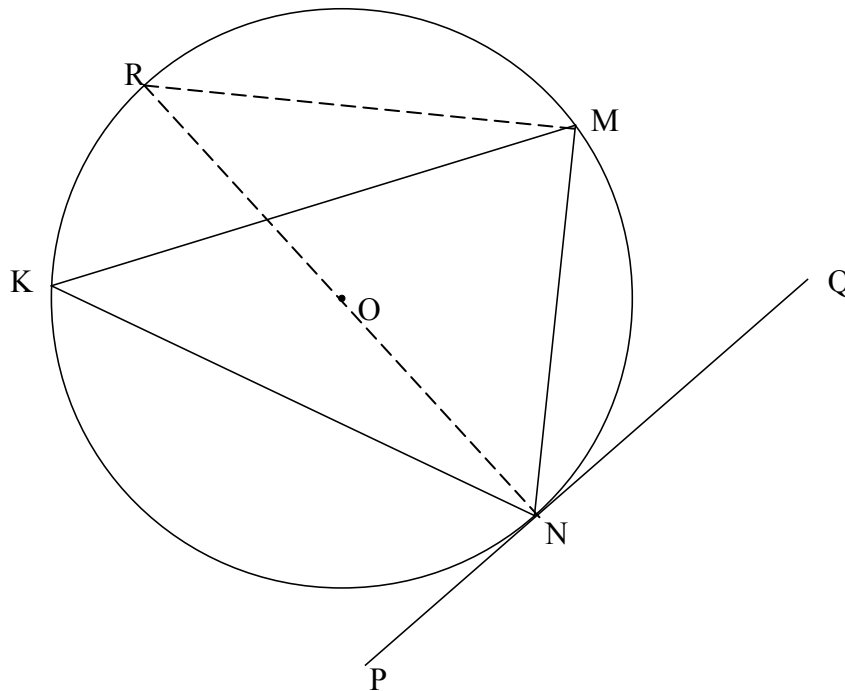
QUESTION/VRAAG 9



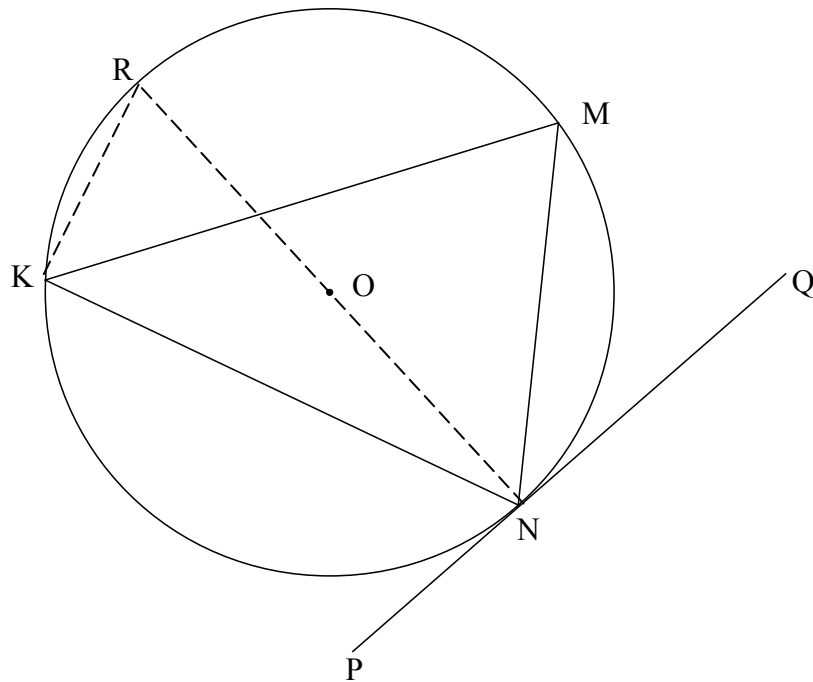
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| <p>9.1.1</p> | $\frac{AF}{BF} = \frac{3x}{2x} = \frac{3}{2} \quad \& \quad \frac{AG}{CG} = \frac{12y}{8y} = \frac{3}{2}$ $\therefore \frac{AF}{BF} = \frac{AG}{CG}$ <p>$\therefore FG \parallel BC$ [conv prop th/omg eweredigh st. OR line divides 2 sides of Δ in prop/lyn verdeel 2 sye v Δ in dies verh]</p> | <p>$\checkmark \frac{AF}{BF} = \frac{AG}{CG}$</p> <p>$\checkmark R$</p> <p style="text-align: right;">(2)</p> |
| <p>9.1.2</p> | $\frac{AG}{GC} = \frac{AH}{HK} \quad \text{[prop theorem/eweredigh st; } \underline{GH \parallel CK} \text{ OR line } \parallel \text{ to 1 side of } \Delta \text{/lyn } \parallel \text{ 1 sy van } \Delta]$ $\frac{AG}{GC} = \frac{AE}{ED} \quad \text{[prop theorem/eweredigh st; } \underline{GE \parallel CD}]$ $\therefore \frac{AH}{HK} = \frac{AE}{ED}$ | <p>$\checkmark S \checkmark R$</p> <p>$\checkmark S$</p> <p style="text-align: right;">(3)</p> |
| <p>9.2</p> | $\frac{AE}{ED} = \frac{3}{2} \quad \text{and} \quad \frac{AH}{HK} = \frac{3}{2}$ $\frac{AE}{12} = \frac{3}{2} \quad \text{and} \quad \frac{15}{HK} = \frac{3}{2}$ <p>$\therefore AE = 18$ and $HK = 10$</p> <p>$\therefore HE = AE - AH$ $= 18 - 15$ $= 3$</p> <p>$\therefore EK = HK - HE$ $= 10 - 3$ $= 7$</p> <p style="text-align: center;">OR/OF</p> $AD = 30$ $KD = AD - AH - HK$ $= 30 - 15 - 10$ $= 5$ $EK = ED - KD$ $= 12 - 5$ $= 7$ | <p>\checkmark use of ratios</p> <p>$\checkmark AE = 18$</p> <p>$\checkmark HK = 10$</p> <p>$\checkmark HE = 3$ or $KD = 5$</p> <p>$\checkmark EK = 7$</p> <p style="text-align: right;">(5) [10]</p> |

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| <p>10.2.3</p> <p>In $\triangle OVN$ and $\triangle OWS$</p> <p>$\hat{O}_2 = \hat{O}_2$ [common/<i>gemeenskaplik</i>]</p> <p>$O\hat{V}N = O\hat{W}S = 90^\circ$ [from 10.1]</p> <p>$O\hat{N}V = O\hat{S}W$ [sum $\angle s \triangle / som \angle e \triangle$]</p> <p>$\therefore \triangle OVN \parallel \triangle OWS$ [\angle, \angle, \angle]</p> <p>$\therefore \frac{VN}{WS} = \frac{ON}{OS}$</p> <p>But $VN = \frac{1}{2} MN$ [given]</p> <p>$\therefore \frac{\frac{1}{2} MN}{WS} = \frac{ON}{OS}$</p> <p>$\therefore OS \cdot MN = 2ON \cdot WS$</p> <p>OR/OF</p> <p>In $\triangle OVM$ and $\triangle OWS$</p> <p>$O\hat{V}M = O\hat{W}S = 90^\circ$ [from 10.1]</p> <p>$O\hat{M}V = O\hat{S}W$ [sum $\angle s \triangle / som \angle e \triangle$]</p> <p>$\therefore \triangle OVM \parallel \triangle OWS$ [\angle, \angle, \angle]</p> <p>$\therefore \frac{OM}{OS} = \frac{VM}{WS}$</p> <p>But $VN = \frac{1}{2} MN$ [given]</p> <p>$\therefore \frac{\frac{1}{2} MN}{WS} = \frac{OM}{OS}$</p> <p>$\therefore OS \cdot MN = 2ON \cdot WS$ [VM = VN]</p> <p>OR/OF</p> <p>If any other 2 $\triangle s$ are used, first need to prove that $TW = WS$ by proving $\triangle OWT \equiv \triangle OWS$</p> <p>In $\triangle OVM$ and $\triangle OWT$</p> <p>$\hat{O}_1 = \hat{O}_1$ [common/<i>gemeenskaplik</i>]</p> <p>$O\hat{V}M = O\hat{W}T = 90^\circ$ [from 10.1]</p> <p>$O\hat{M}V = O\hat{T}W$ [sum $\angle s \triangle / som \angle e \triangle$]</p> <p>$\therefore \triangle OVM \parallel \triangle OWT$ [\angle, \angle, \angle]</p> <p>$\therefore \frac{VM}{WT} = \frac{OM}{OT}$</p> <p>But $VN = VM = \frac{1}{2} MN$ [given]</p> <p>and $WT = WS$ and $OT = OS$ [$\triangle OWT \equiv \triangle OWS$]</p> <p>$\therefore \frac{\frac{1}{2} MN}{WS} = \frac{ON}{OS}$</p> <p>$\therefore OS \cdot MN = 2ON \cdot WS$</p> | <p>$\checkmark$ S; S; S OR S; S; R</p> <p>$\checkmark \triangle OVN \parallel \triangle OWS$ $\checkmark \frac{VN}{WS} = \frac{ON}{OS}$ $\checkmark VN = \frac{1}{2} MN$</p> <p>$\checkmark$ substitution</p> <p>(5)</p> <p>\checkmark S; S; S OR S; S; R</p> <p>$\checkmark \triangle OVM \parallel \triangle OWS$ $\checkmark \frac{OM}{OS} = \frac{VM}{WS}$ $\checkmark VN = \frac{1}{2} MN$</p> <p>$\checkmark$ substitution</p> <p>(5)</p> <p>$\checkmark \checkmark$ similarity $\checkmark \checkmark$ congruency</p> <p>$\checkmark VN = VM = \frac{1}{2} MN$</p> <p>(5)</p> <p>[12]</p> |
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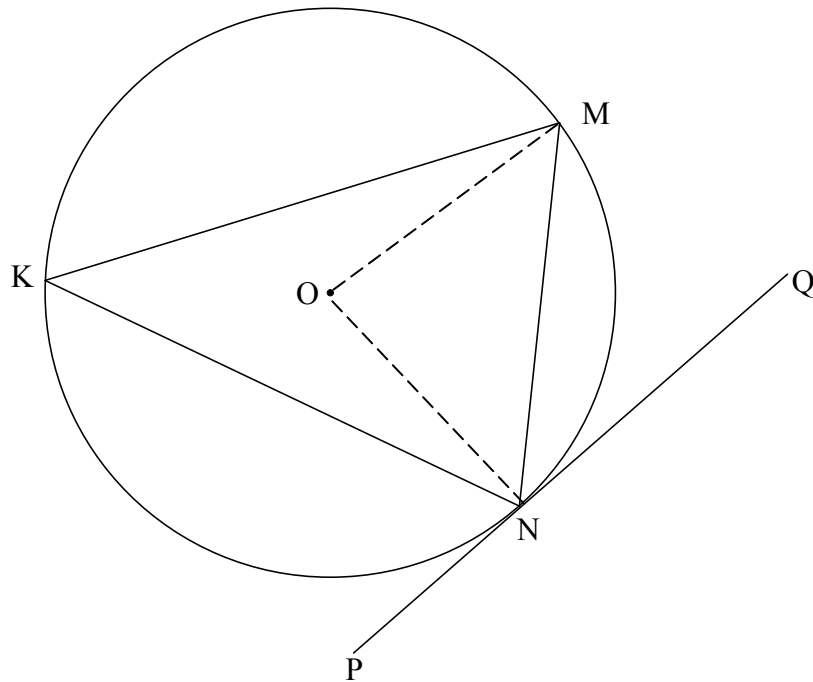
QUESTION/VRAAG 11



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| <p>11.1</p> | <p>Construction: Draw diameter NR and draw RM <i>Konstruksie: Trek middellyn NR en verbind RM</i> $\widehat{ONM} + \widehat{MNQ} = 90^\circ$ [radius \perp tangent/raaklyn] $\widehat{NMR} = 90^\circ$ [\angle in semi circle/semi-sirkel] $\therefore \widehat{MRN} = 180^\circ - (90^\circ + 90^\circ - \widehat{MNQ})$ [sum \angles Δ] $= \widehat{MNQ}$ but $\widehat{MRN} = \widehat{MKN}$ [\angles same segment/\anglee dieselfde segment] $\therefore \widehat{MNQ} = \widehat{MKN}$ OR/OF</p> | <p>✓ construction ✓ S / R ✓ S / R ✓ S ✓ S / R (5)</p> |
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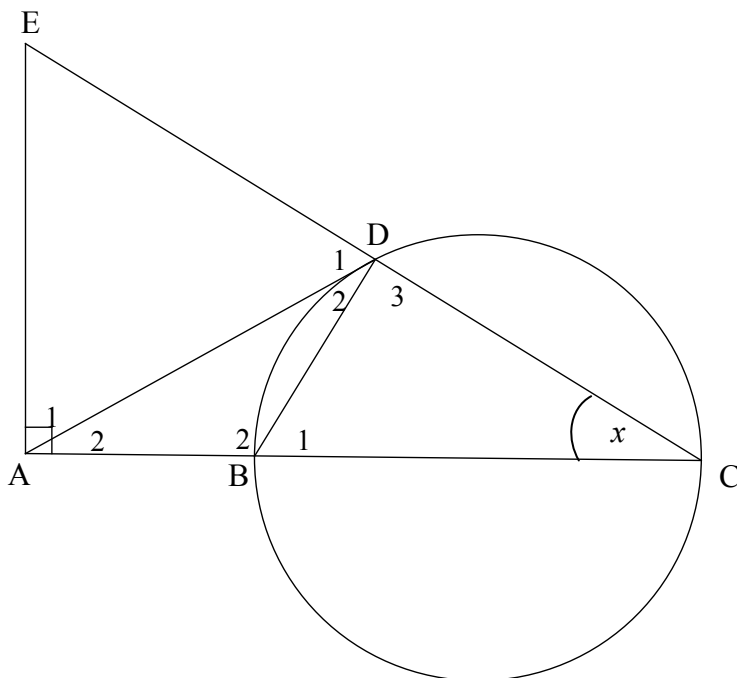


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| <p>11.1</p> | <p>Construction: Draw diameter NR and draw RK <i>Konstruksie: Trek middellyn NR en verbind RK</i> $M\hat{N}Q + R\hat{N}M = 90^\circ$ [radius \perp tangent/raaklyn] $N\hat{K}R = 90^\circ$ [\angle in semicircle/semi-sirkel] $\therefore M\hat{K}N = 90^\circ - R\hat{K}M$ $= 90^\circ - R\hat{N}M$ [\angles same segment/\anglee dieselfde segment] $\therefore M\hat{N}Q = \hat{K}$</p> | <p>✓ construction ✓ S / R ✓ S / R ✓ S ✓ S / R (5)</p> |
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| <p>11.1</p> | <p>Construction: Draw radii ON and OM <i>Konstruksie: Trek radiusse ON en OM</i> $\widehat{M\hat{O}N} = 2\hat{K}$ [\angle at centre = $2\angle$ at circumf/midpts $\angle = 2$ omtreks \angle] $\widehat{O\hat{N}M} + \widehat{O\hat{M}N} = 180^\circ - 2\hat{K}$ [\angles of Δ/ \anglee van Δ] $\widehat{O\hat{N}M} = \widehat{O\hat{M}N} = \frac{180^\circ - 2\hat{K}}{2} = 90^\circ - \hat{K}$ [\angles opp = sides/ \anglee teenoor = sye] $\widehat{O\hat{N}Q} = 90^\circ$ [radius \perp tangent/ radius \perp raaklyn] $\therefore \widehat{M\hat{N}Q} = \hat{K}$</p> | <p>✓ construction ✓ S / R ✓ S ✓ S / R ✓ S / R (5)</p> |
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11.2



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| 11.2.1(a) | Angle in a semi circle/ <i>Hoek in halfsirkel</i> | ✓ R (1) |
| 11.2.1(b) | Exterior \angle of quad = opp interior \angle / <i>Buite \angle van vierh = teenoorst binne \angle</i> OR/OF Opp \angle s of quad supplementary/ <i>Teenoorst \anglee van vierh is supplementêr</i> | ✓ R (1) |
| 11.2.1(c) | tangent chord theorem/ <i>raaklyn koord stelling</i> | ✓ R (1) |
| 11.2.2(a) | In $\triangle AEC$ $\hat{E} = 180^\circ - (90^\circ + x)$ [sum \angle s \triangle] $= 90^\circ - x$ $\hat{D}_1 = 180^\circ - (90^\circ + x)$ [\angle s on a straight line] $= \hat{E} = 90^\circ - x$ $\therefore AD = AE$ [sides opp = \angle s/ <i>syte teenoor = \anglee</i>] | ✓ S ✓ S ✓ R (3) |
| 11.2.2(b) | In $\triangle ADB$ and $\triangle ACD$ $\hat{A}_2 = \hat{A}_2$ [common] $\hat{D}_2 = \hat{C}$ [proven] $\hat{B}_2 = \hat{D}_2 + \hat{D}_3$ [sum \angle \triangle] $\therefore \triangle ADB \parallel \triangle ACD$ OR/OF In $\triangle ADB$ and $\triangle ACD$ $\hat{A}_2 = \hat{A}_2$ [common] $\hat{D}_2 = \hat{C}$ [proven] $\therefore \triangle ADB \parallel \triangle ACD$ [\angle , \angle , \angle] | ✓ S ✓ S ✓ S (3) ✓ S ✓ S ✓ R (3) |

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| <p>11.2.3(a)</p> | $\frac{AD}{AC} = \frac{AB}{AD} \quad [\Delta s]$ $AD^2 = AC \cdot AB$ $= 3r \times r$ $= 3r^2$ | <p>✓ ratio</p> <p>✓ substitution</p> <p>(2)</p> |
| <p>11.2.3(b)</p> | <p>$AD = AE = \sqrt{3}r$ [from 11.2.2(a) & 11.2.3(a)]</p> <p>$AB = r$ and $BC = 2r \therefore AC = 3r$</p> <p><u>In ΔACE:</u></p> $\tan \hat{E} = \frac{AC}{AE}$ $= \frac{3r}{\sqrt{3}r} = \sqrt{3}$ <p>$\therefore \hat{E} = 60^\circ$</p> <p>$\therefore \hat{D}_1 = 60^\circ$ [from 11.2.2(a)]</p> <p>$\therefore \hat{A}_1 = 60^\circ$ [$\angle s$ of $\Delta = 180^\circ$]</p> <p>$\therefore \Delta ADE$ is equilateral/<i>is gelyksydig</i></p> <p>OR/OF</p> $\frac{AD}{AC} = \frac{DB}{CD} \quad [\Delta s]$ $\frac{\sqrt{3}r}{3r} = \frac{DB}{CD}$ $\tan x = \frac{1}{\sqrt{3}}$ <p>\therefore In ΔBDC: $x = 30^\circ$</p> <p>$\therefore \hat{E} = 60^\circ$</p> <p>$\therefore \hat{D}_1 = 60^\circ$ [from 11.2.2(a)]</p> <p>$\therefore \hat{A}_1 = 60^\circ$ [$\angle s$ of $\Delta = 180^\circ$]</p> <p>$\therefore \Delta ADE$ is equilateral/<i>is gelyksydig</i></p> <p>OR/OF</p> $\frac{AD}{AC} = \frac{DB}{CD} \quad [\Delta s]$ $\frac{\sqrt{3}r}{3r} = \frac{DB}{CD} \quad \therefore BD = \frac{CD}{\sqrt{3}}$ $DC^2 = BC^2 - DB^2$ $= 4r^2 - \frac{CD^2}{3}$ $3DC^2 = 12r^2 - CD^2$ $4CD^2 = 12r^2$ $DC = \sqrt{3}r$ | <p>✓ AC ito r</p> <p>✓ trig ratio</p> <p>✓ simplification</p> <p>✓ all 3 $\angle s = 60^\circ$</p> <p>(4)</p> <p>✓ $\frac{\sqrt{3}r}{3r} = \frac{DB}{CD}$</p> <p>✓ $\frac{1}{\sqrt{3}} = \tan x$</p> <p>✓ $x = 30^\circ$</p> <p>✓ all 3 $\angle s = 60^\circ$</p> <p>(4)</p> <p>✓ $BD = \frac{CD}{\sqrt{3}}$</p> <p>✓ $DC = \sqrt{3}r$</p> |

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| | $EC^2 = EA^2 + AC^2$ $= 3r^2 + 9r^2$ $EC = 2\sqrt{3}r$ $\therefore ED = EC - DC$ $= \sqrt{3}r$ $\therefore ED = EA = AD$ $\therefore \triangle ADE \text{ is equilateral/is gelyksydig}$ | $\checkmark EC = 2\sqrt{3}r$ $\checkmark ED = EA = AD$ <p style="text-align: right;">(4) [20]</p> |
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TOTAL/TOTAAL: 150