



Province of the
EASTERN CAPE
EDUCATION

**NATIONAL
SENIOR CERTIFICATE**

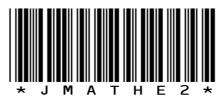
GRADE 12

JUNE 2017

MATHEMATICS P2

MARKS: 150

TIME: 3 hours



* J M A T H E 2 *

This question paper consists of 14 pages, including 1 page information sheet, and a
SPECIAL ANSWER BOOK.

INSTRUCTIONS AND INFORMATION

1. This question paper consists of 11 questions.
2. Answer ALL the questions in the SPECIAL ANSWER BOOK provided.
3. Clearly show ALL calculations, diagrams graphs, et cetera which you have used in determining the answers.
4. Answers only will NOT necessarily be awarded full marks.
5. If necessary round off your answers to TWO decimal places, unless stated otherwise.
6. Diagrams are not necessarily drawn to scale.
7. You may use an approved scientific calculator (non-programmable and non-graphical) unless stated otherwise.
8. An information sheet with formulae is included at the end of the question paper.
9. Write neatly and legibly.

QUESTION 1

The percentages obtained by learners in their first Mathematics test is shown in the table below.

Percentages	Frequency	Cumulative Frequency
$30 \leq x < 40$	1	
$40 \leq x < 50$	2	
$50 \leq x < 60$	9	
$60 \leq x < 70$	12	
$70 \leq x < 80$	11	
$80 \leq x < 90$	9	
$90 \leq x < 100$	6	

- 1.1 Complete the cumulative frequency column in the table given in the ANSWER BOOK. (3)
- 1.2 Draw an ogive (cumulative frequency curve) to represent the data on the grid provided in the ANSWER BOOK. (4)
- 1.3 Estimate how many learners obtained 75% or less for the test. Indicate this by means of B on your graph. (2)
[9]

QUESTION 2

The water consumption (in kilolitres) of 15 households is as follows:

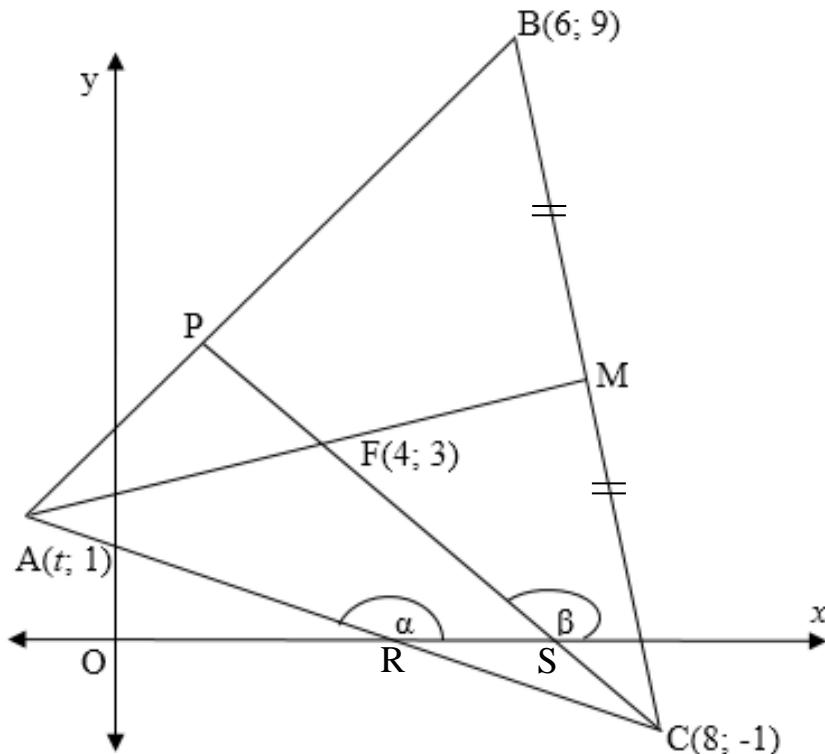
12,4	20,0	34,5	40,1	18,9
19,7	34,9	15,1	23,8	23,7
31,1	20,9	19,7	36,5	33,6

- 2.1 List the five number summary for the data. (4)
- 2.2 Draw a box-whisker diagram to represent the data. (3)
- 2.3 Comment on the skewedness of the data represented in QUESTION 2.2. (1)
- 2.4 Determine the standard deviation of the data. (2)
- 2.5 Use the standard deviation to comment on the spread of the data. (1)

[11]

QUESTION 3

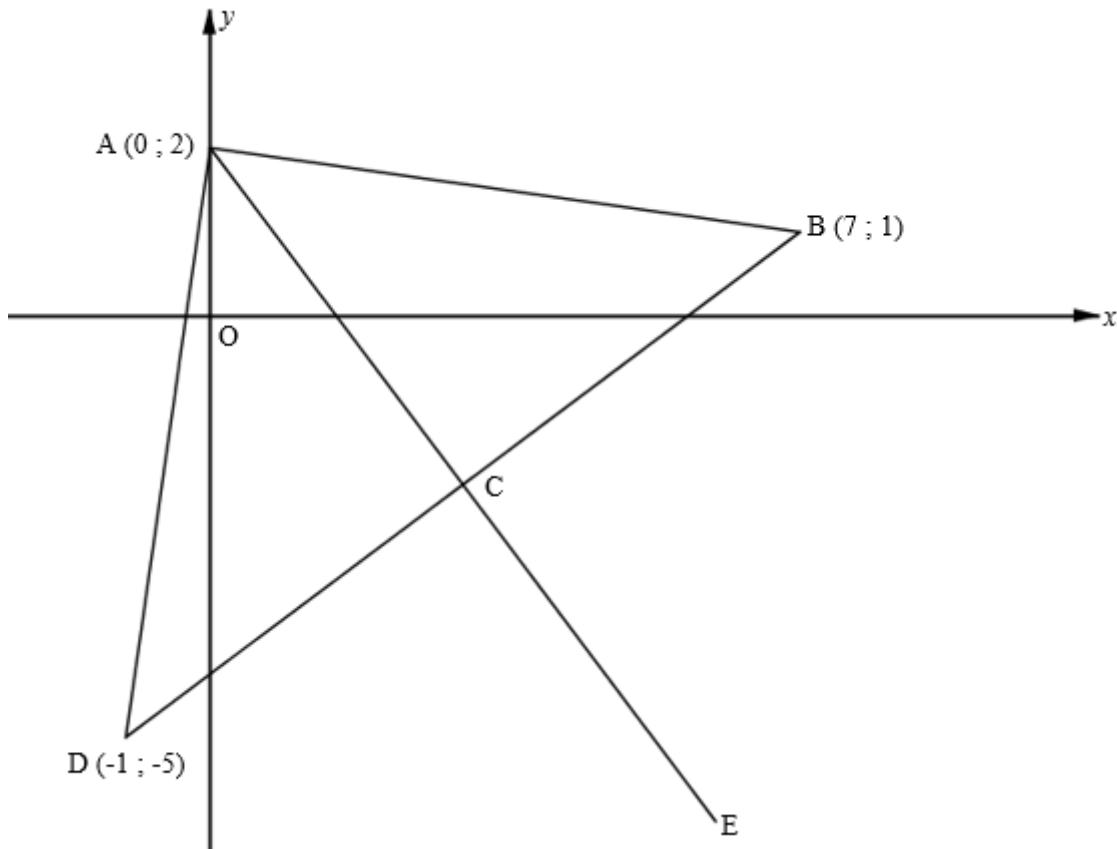
In the diagram, A ($t ; 1$), B (6 ; 9) and C (8 ; -1) are points in a Cartesian plane. M is the midpoint of BC. P is a point on AB. CP intersects AM at F (4 ; 3). R is the x -intercept of line AC and S is the x -intercept of line PC.



- 3.1 Calculate the coordinates of M. (2)
 - 3.2 Determine the equation of the median AM. (4)
 - 3.3 Calculate the value of t . (2)
 - 3.4 Calculate the gradient of PC. (2)
 - 3.5 Determine the size of β . (2)
 - 3.6 Calculate the size of $A\hat{C}P$. (4)
- [16]**

QUESTION 4

Quadrilateral ABED, with vertices A (0 ; 2), B (7; 1), D (-1 ; -5) and E is given below.
Diagonals AE and BD intersect at C.



- 4.1 Calculate the coordinates of C, the midpoint of BD. (2)
 - 4.2 Show that CA = CB if the coordinates of C are (3 ; -2). (3)
 - 4.3 Why is $D\hat{A}B = 90^\circ$? (5)
 - 4.4 Hence, write the equation of the circle with centre C which is passing through A, B, E and D. (2)
 - 4.5 Calculate the gradient of BC, the radius of the circle. (2)
 - 4.6 Determine the equation of the tangent to the circle at B in the form $y = \dots$ (3)
 - 4.7 Explain why ABED is a rectangle. (3)
- [20]**

QUESTION 5

5.1 If $\sin 58^\circ = k$, determine, **without the use of a calculator**:

5.1.1 $\sin 238^\circ$ (2)

5.1.2 $\cos 58^\circ$ (2)

5.2 Simplify, **without the use of a calculator**:

$$\frac{\tan 150^\circ \cdot \sin 300^\circ \cdot \sin 10^\circ}{\cos 225^\circ \cdot \sin 135^\circ \cdot \cos 80^\circ} \quad (7)$$

5.3 Given $\cos(\alpha + \beta) = \cos \alpha \cos \beta + \sin \alpha \sin \beta$

Use the formula for $\cos(\alpha + \beta)$ to derive a formula for $\sin(\alpha + \beta)$. (4)

5.4 Prove the identity: $\frac{\cos 2x + 1}{\sin 2x \cdot \tan x} = \frac{1}{\tan^2 x}$ (4)

5.5 5.5.1 Show that $\tan x = 2\sin x$ can be written as $\sin x = 0$ or $\cos x = \frac{1}{2}$. (3)

5.5.2 Hence, write down the general solution of the equation

$$\tan x = 2 \sin x \quad (4)$$

[26]

QUESTION 6

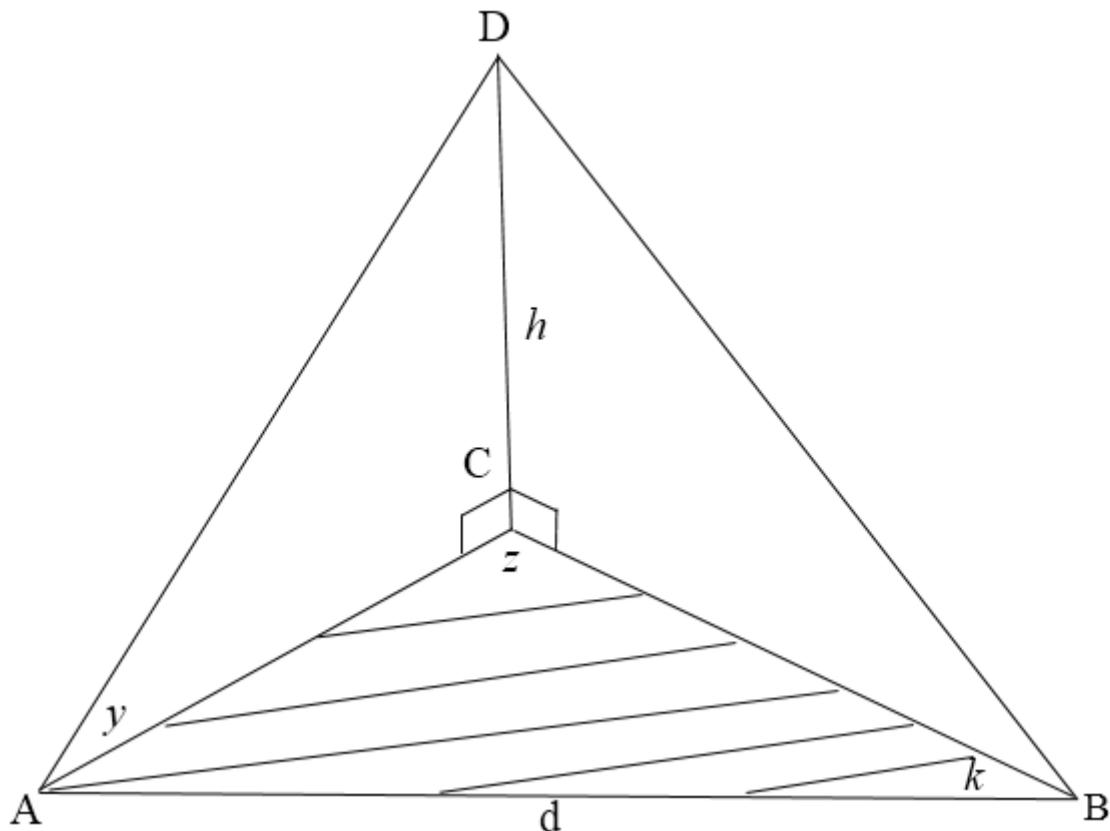
Given $f(x) = \tan x$ and $g(x) = \sin(x + 45^\circ)$

- 6.1 Draw the graphs of $f(x)$ and $g(x)$ on the same set of axes for $x \in [-90^\circ; 180^\circ]$, on the grid provided in the ANSWER BOOK. (6)
- 6.2 Use your graphs to determine the value(s) of x in the interval $x \in [-90^\circ; 90^\circ]$ for which:
- 6.2.1 $g(x) - f(x) = 1$ (2)
- 6.2.2 $g(x) \geq f(x)$ (2)
- 6.3 State the period of $y = f(2x)$. (1)
- [11]

QUESTION 7

To find the height h of a tree CD, the end of the shadow was marked at points A and B in the same horizontal plane as its stem C at different times of the day. The shadow of the tree rotated z° between the times of observation, i.e. $A\hat{C}B = z^\circ$.

$AB = d$ metres, $A\hat{B}C = k^\circ$ and the angle of elevation of the sun at A was y° .

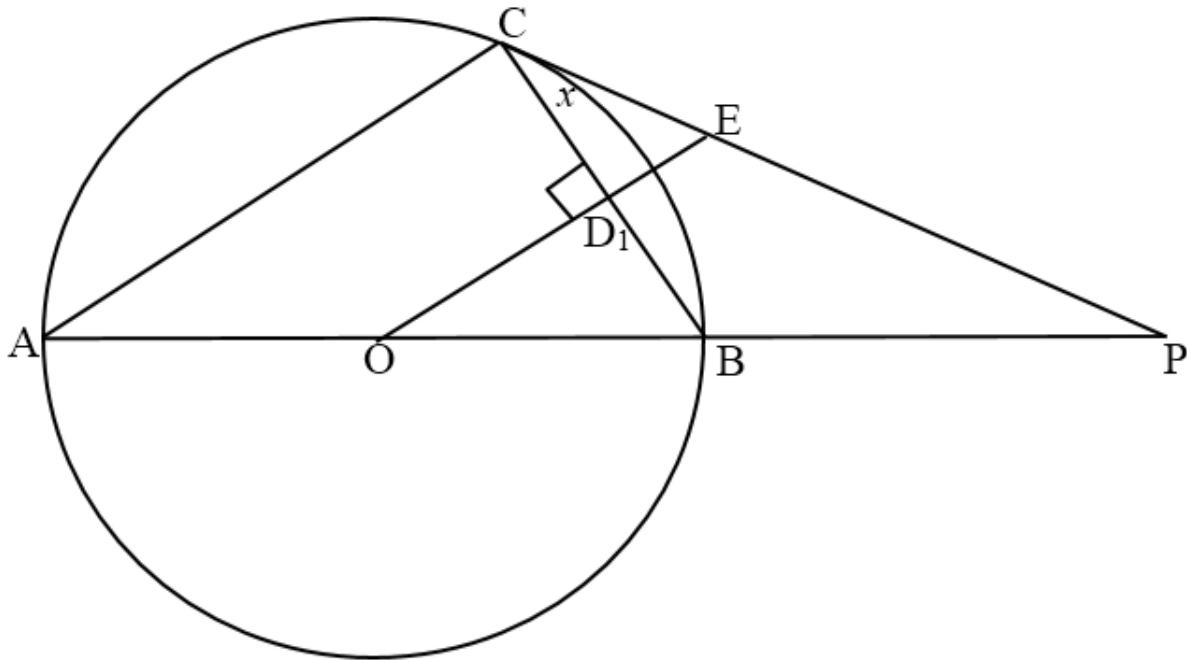


- 7.1 Find the length of AC in terms of z , k and d . (2)
 - 7.2 Find the length of AC in terms of y and h . (2)
 - 7.3 Hence show that $h = \frac{d \sin k \cdot \tan y}{\sin z}$. (1)
 - 7.4 Calculate the length of h if $z = 125^\circ$, $d = 80m$, $k = 38^\circ$ and $y = 40^\circ$. (2)
- [7]

Give reasons for ALL statements in QUESTION 8, 9, 10 AND 11.

QUESTION 8

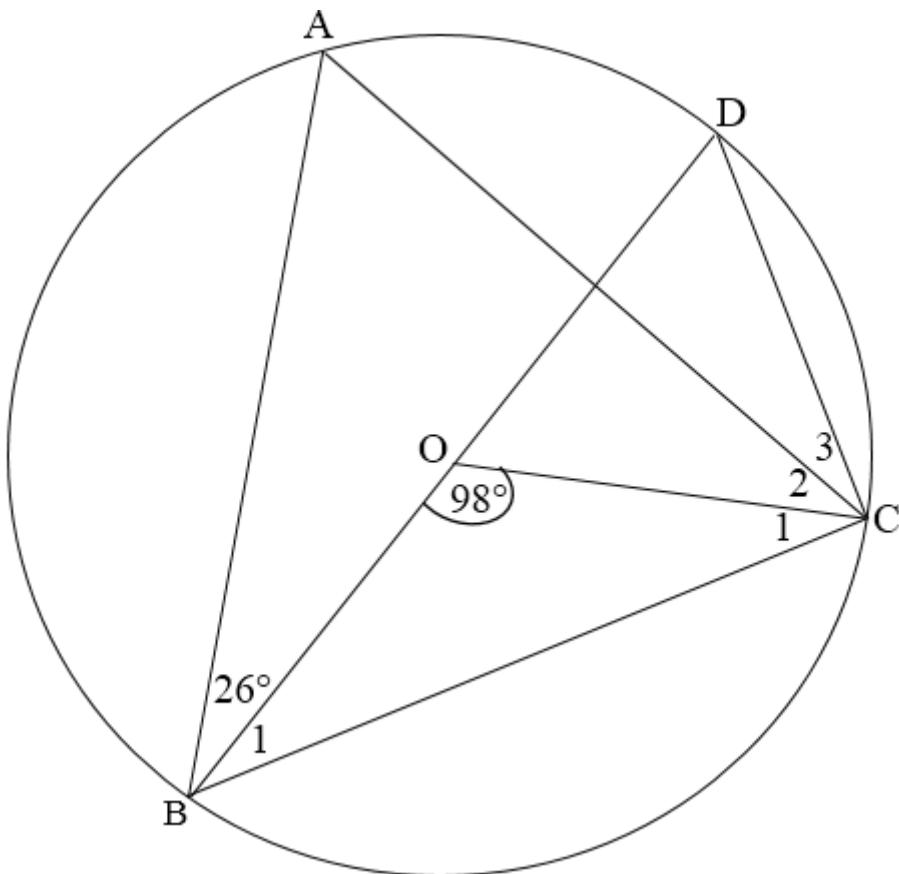
In the figure, AB is a diameter of the circle with centre O. AB is produced to P. PC is a tangent to the circle at C and line ODE perpendicular to BC intersects BC at D and PC at E.



- 8.1 Give a reason why $CD = DB$. (1)
 - 8.2 Show that $AC \parallel OE$. (3)
 - 8.3 If $\hat{B}CP = x$, name two other angles equal to x . (4)
 - 8.4 Prove that $OBEC$ is a cyclic quadrilateral. (2)
- [10]

QUESTION 9

In the diagram, BD is the diameter of the circle ABCD with centre O. $\hat{A}BD = 26^\circ$ and $\hat{B}OC = 98^\circ$.



Calculate:

9.1 \hat{A} (2)

9.2 \hat{B}_1 (3)

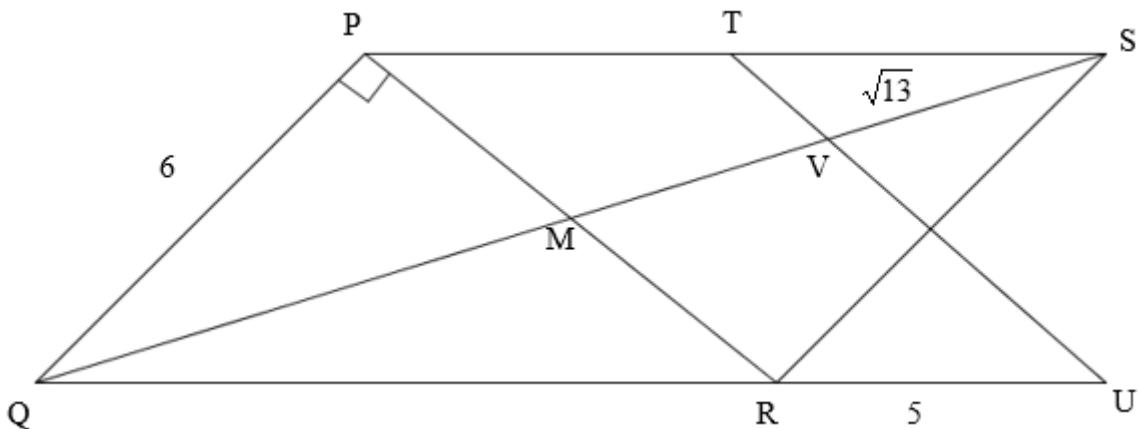
9.3 \hat{C}_2 (3)
[8]

QUESTION 10

In the diagram below PQRS is a parallelogram, with the diagonals intersecting at M.

$\hat{QPR} = 90^\circ$. QR is produced to U. T is a point on PS. TU intersects QS at V.

$PQ = 6$, $PR = 8$, $RU = 5$ and $VS = \sqrt{13}$



10.1 Determine with reasons the following ratios in simplified form:

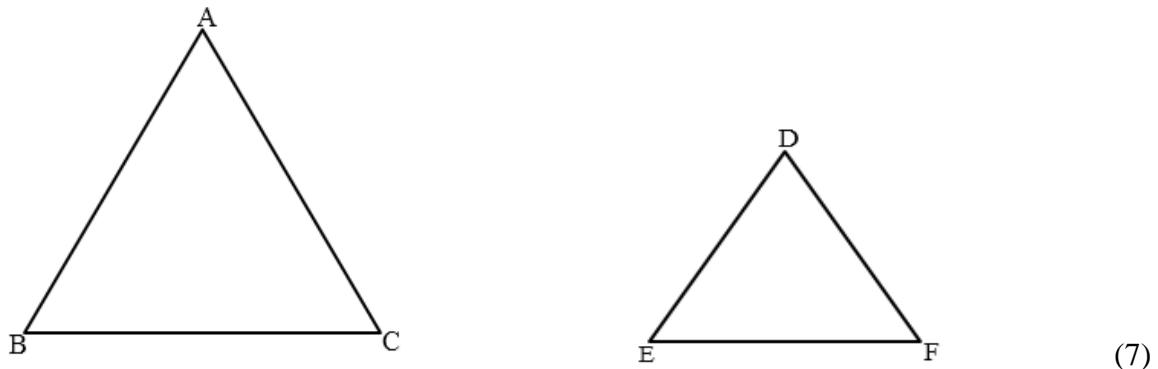
$$10.1.1 \quad \frac{UR}{RQ} \quad (3)$$

$$10.1.2 \quad \frac{VM}{MQ} \quad (4)$$

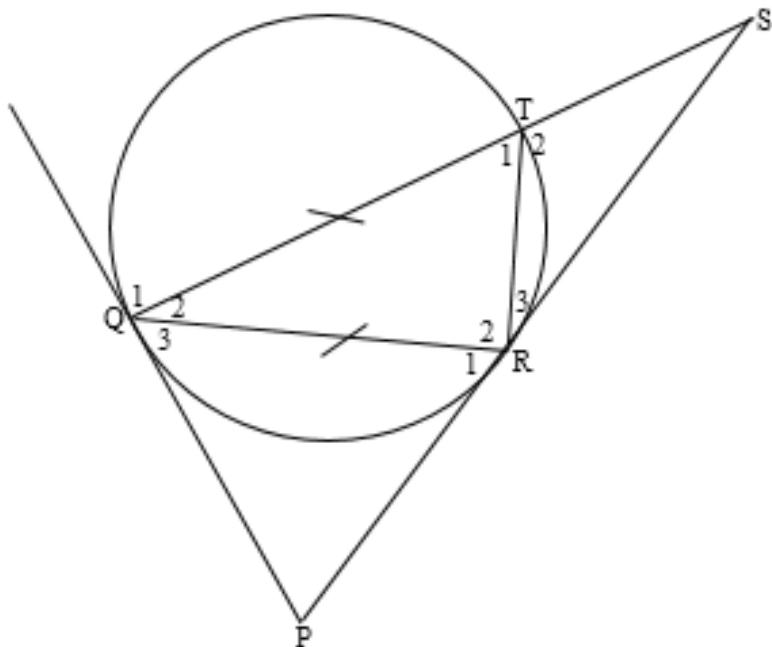
10.2 Hence, prove that $MR \parallel VU$ (2)
[9]

QUESTION 11

- 11.1 In $\triangle ABC$ and $\triangle DEF$, $\hat{A} = \hat{D}$, $\hat{B} = \hat{E}$ and $\hat{C} = \hat{F}$, respectively. Prove that $\frac{AB}{DE} = \frac{AC}{DF}$.



- 11.2 Tangents PQ and PR touch the circle at Q and R respectively. T is a point on the circle such that $QT = QR$. QT and PR are produced and they meet at S. $\hat{Q}_1 = x$.



11.2.1 Name THREE other angles equal to x . (3)

11.2.2 Determine, in terms of x , the size of \hat{Q}_2 . (2)

11.2.3 Hence show that $TR \parallel QP$. (3)

11.2.4 Prove that $\triangle STR \parallel\!\!\!\parallel \triangle SRQ$. (3)

11.2.5 Hence show that $RS^2 = ST \times SQ$. (2)

11.2.6 If it is further given that $QT : TS = 3 : 2$, show that $\frac{SP}{PQ} = \frac{5}{3}$. (3)

[23]

TOTAL: 150

INFORMATION SHEET MATHEMATICS

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$A = P(1 + ni)$$

$$A = P(1 - ni)$$

$$A = P(1 - i)^n$$

$$A = P(1 + i)^n$$

$$\sum_{i=1}^n 1 = n$$

$$\sum_{i=1}^n i = \frac{n(n+1)}{2}$$

$$T_n = a + (n-1)d$$

$$S_n = \frac{n}{2}(2a + (n-1)d)$$

$$T_n = ar^{n-1}$$

$$S_n = \frac{a(r^n - 1)}{r - 1}; \quad r \neq 1$$

$$S_\infty = \frac{a}{1-r}; \quad -1 < r < 1$$

$$F = \frac{x[(1+i)^n - 1]}{i}$$

$$P = \frac{x[1 - (1+i)^{-n}]}{i}$$

$$f'(x) = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$$

$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$M\left(\frac{x_1 + x_2}{2}; \frac{y_1 + y_2}{2}\right)$$

$$y = mx + c$$

$$y - y_1 = m(x - x_1)$$

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

$$m = \tan \theta$$

$$(x - a)^2 + (y - b)^2 = r^2$$

$$\text{In } \Delta ABC: \quad \frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C} \quad a^2 = b^2 + c^2 - 2bc \cos A$$

$$\text{area } \Delta ABC = \frac{1}{2} ab \sin C$$

$$\sin(\alpha + \beta) = \sin \alpha \cos \beta + \cos \alpha \sin \beta$$

$$\sin(\alpha - \beta) = \sin \alpha \cos \beta - \cos \alpha \sin \beta$$

$$\cos(\alpha + \beta) = \cos \alpha \cos \beta - \sin \alpha \sin \beta$$

$$\cos(\alpha - \beta) = \cos \alpha \cos \beta + \sin \alpha \sin \beta$$

$$\cos 2\alpha = \begin{cases} \cos^2 \alpha - \sin^2 \alpha \\ 1 - 2\sin^2 \alpha \\ 2\cos^2 \alpha - 1 \end{cases}$$

$$\sin 2\alpha = 2\sin \alpha \cos \alpha$$

$$\bar{x} = \frac{\sum x}{n}$$

$$\sigma^2 = \frac{\sum_{i=1}^n (x_i - \bar{x})^2}{n}$$

$$P(A) = \frac{n(A)}{n(S)}$$

$$P(A \text{ or } B) = P(A) + P(B) - P(A \text{ and } B)$$

$$\hat{y} = a + bx$$

$$b = \frac{\sum (x - \bar{x})(y - \bar{y})}{\sum (x - \bar{x})^2}$$



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LEERDERNAAM:

GRADE 12
GRAAD 12

**NATIONAL/NASIONALE SENIOR
CERTIFICATE/SERTIFIKAAT**

GRADE 12/GRAAD 12



* J M A T H E 4 *

JUNE/JUNIE 2017

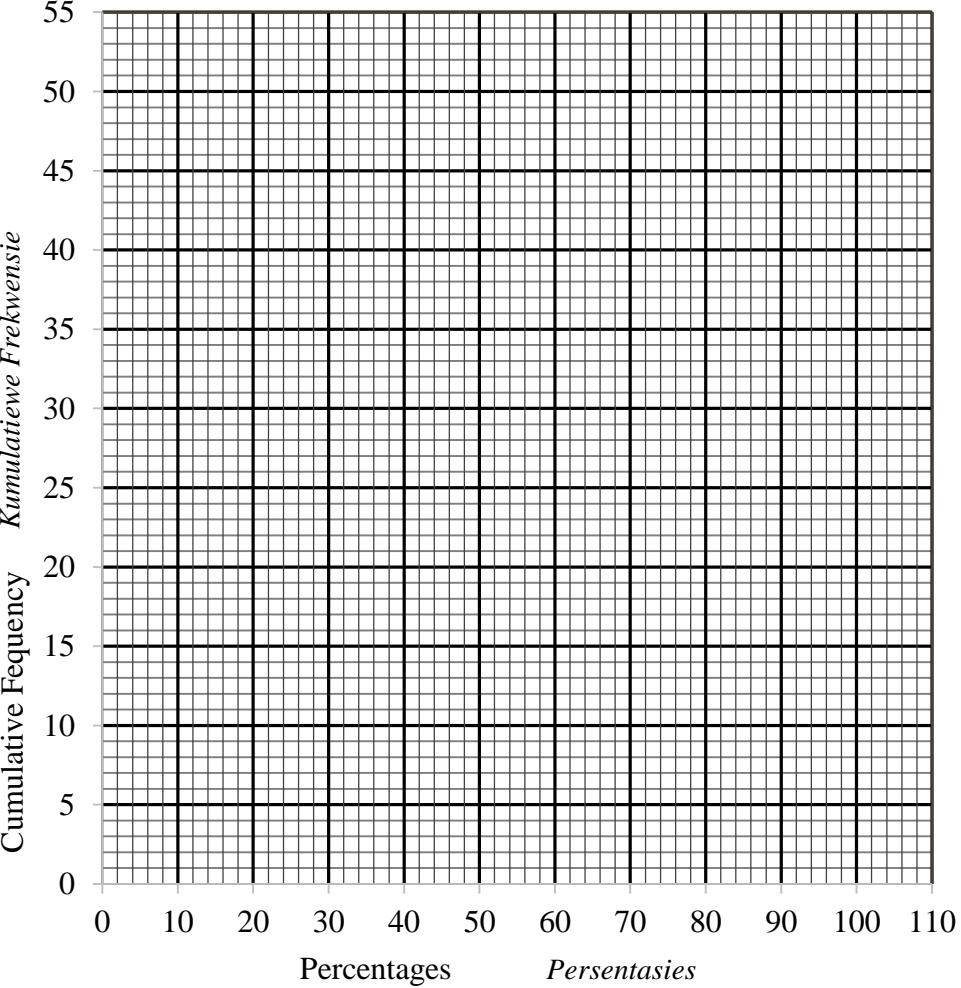
**MATHEMATICS P2/WISKUNDE V2
SPECIAL ANSWER BOOK/
SPESIALE ANTWOORDEBOEK**

QUESTION/VRAAG	MARK/PUNT	INITIAL/PARAAF	MOD.
1			
2			
3			
4			
5			
6			
7			
8			
9			
10			
11			
TOTAL/TOTAL			

This SPECIAL ANSWER BOOK consists of 22 pages. /
Hierdie SPESIALE ANTWOORDEBOEK bestaan uit 22 bladsye.

QUESTION/VRAAG 1

1.1	Percentages/ Persentasies	Frequency/ Frekwensie	Cumulative Frequency/ Kumulatiewe Frekwensie	
	$30 \leq x < 40$	1		
	$40 \leq x < 50$	2		
	$50 \leq x < 60$	9		
	$60 \leq x < 70$	12		
	$70 \leq x < 80$	11		
	$80 \leq x < 90$	9		
	$90 \leq x < 100$	6		

1.2	Cumulative Frequency curve Kumulatiewe Frekwensie kurwe		
			

1.3			

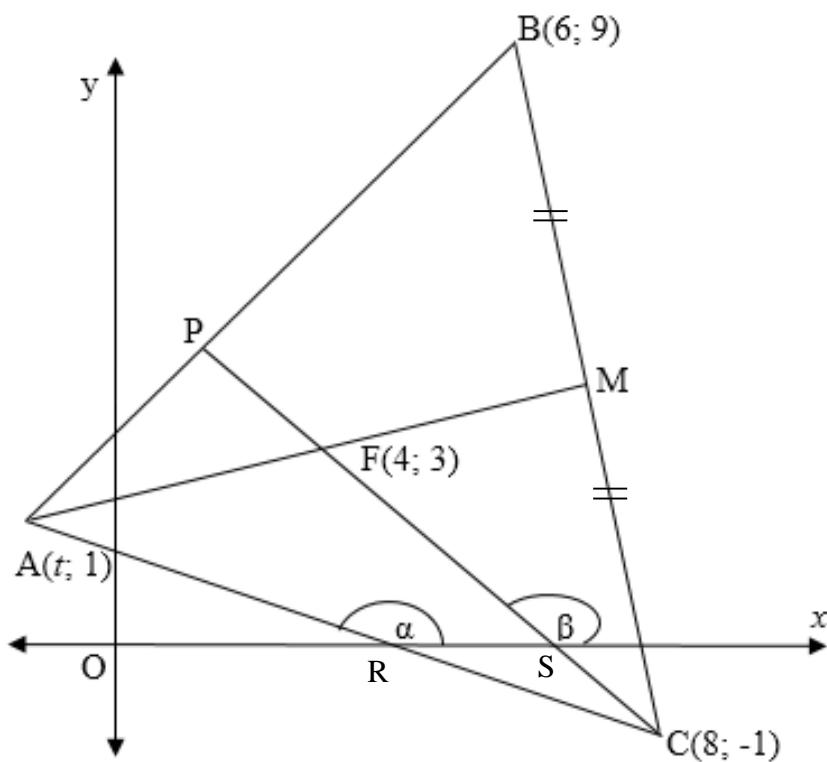
QUESTION/VRAAG 2

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[11]

QUESTION/VRAAG 3



3.1

(2)

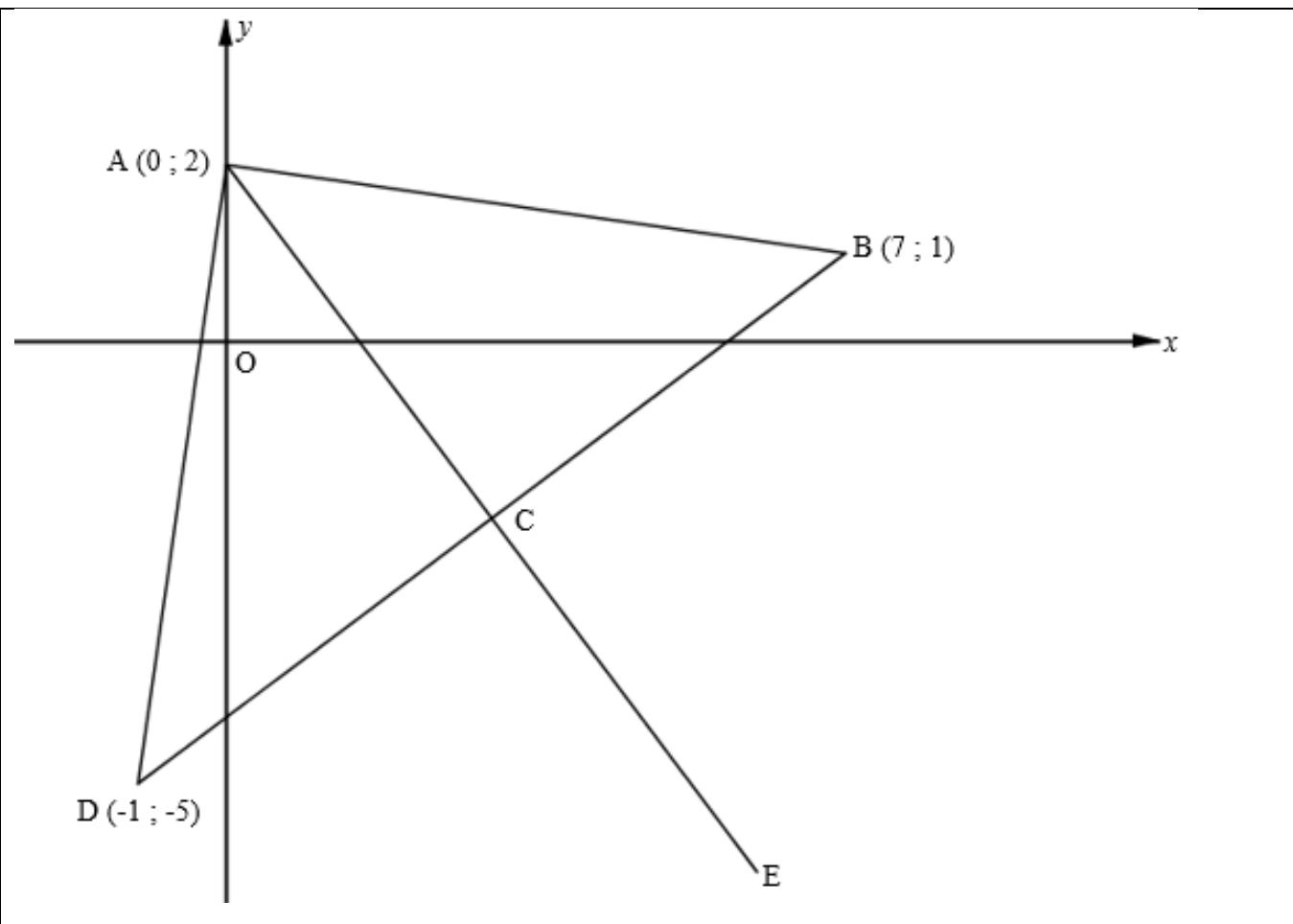
3.2

(4)

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QUESTION/VRAAG 4



4.1		
		(2)
4.2		
		(3)

4.3		(5)
4.4		(2)
4.5		(2)
4.6		(3)
4.7		(3)

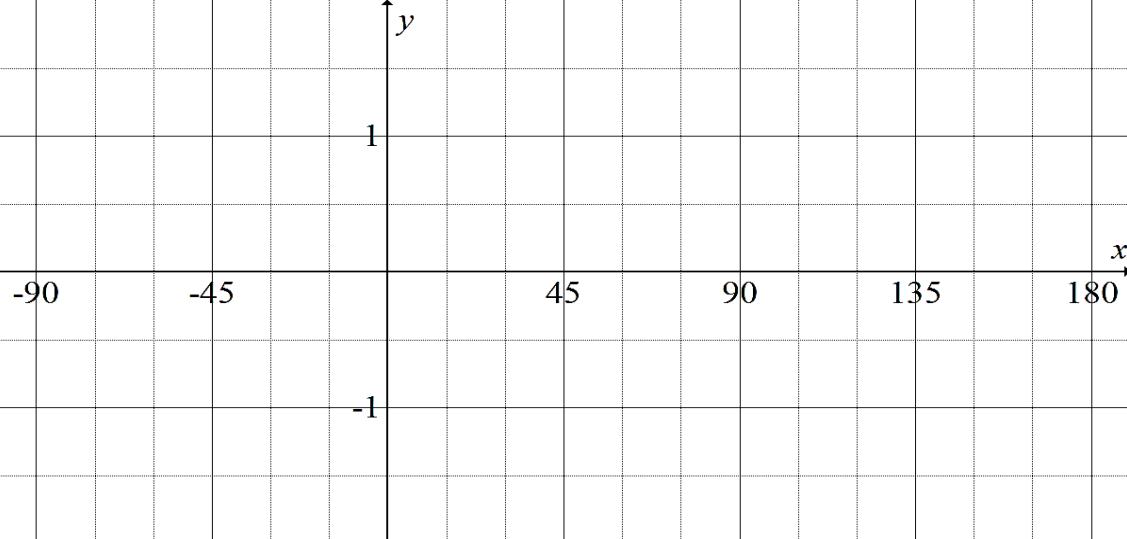
[20]

QUESTION/VRAAG 5

5.1	5.1.1		(2)
5.1.2			(2)
5.2			(7)
5.3			(4)

5.4		(4)
5.5	5.5.1	(3)
	5.5.2	(4)

QUESTION/VRAAG 6

6.1		(6)
6.2.1		
6.2.2		
6.3		

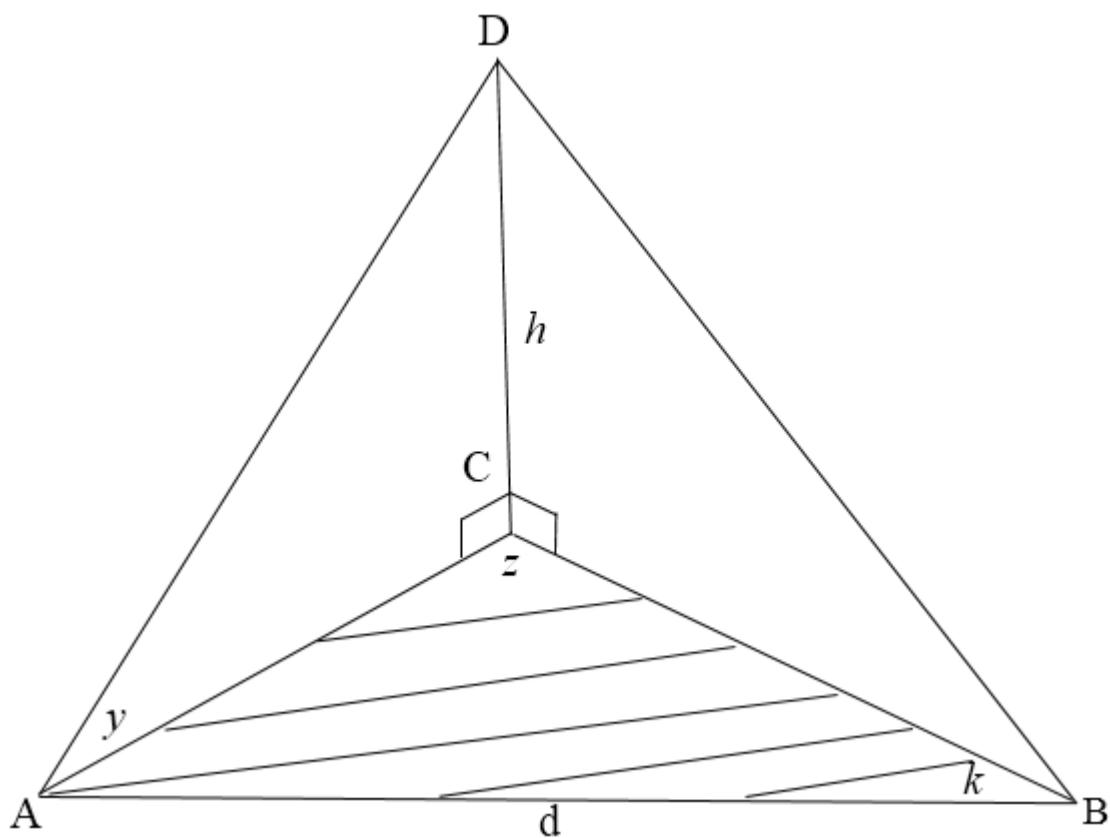
(1)

(2)

(2)

(6)

QUESTION/VRAAG 7



7.1

(2)

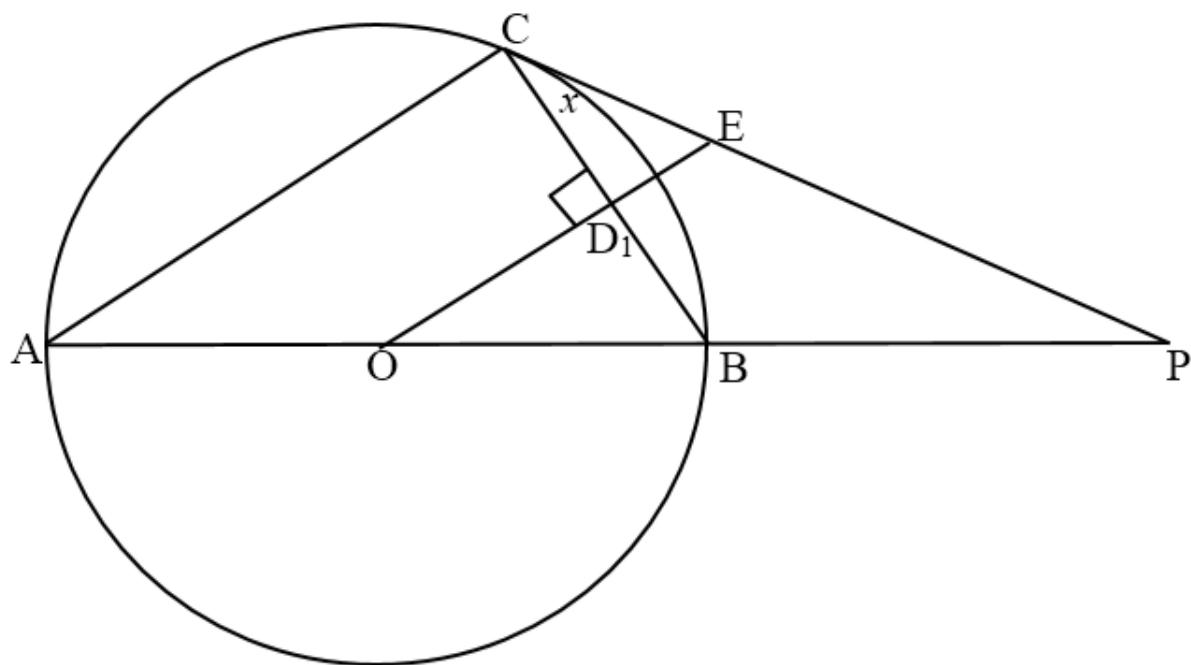
7.2

(2)

7.3		
		(1)
7.4		
		(2)

[7]

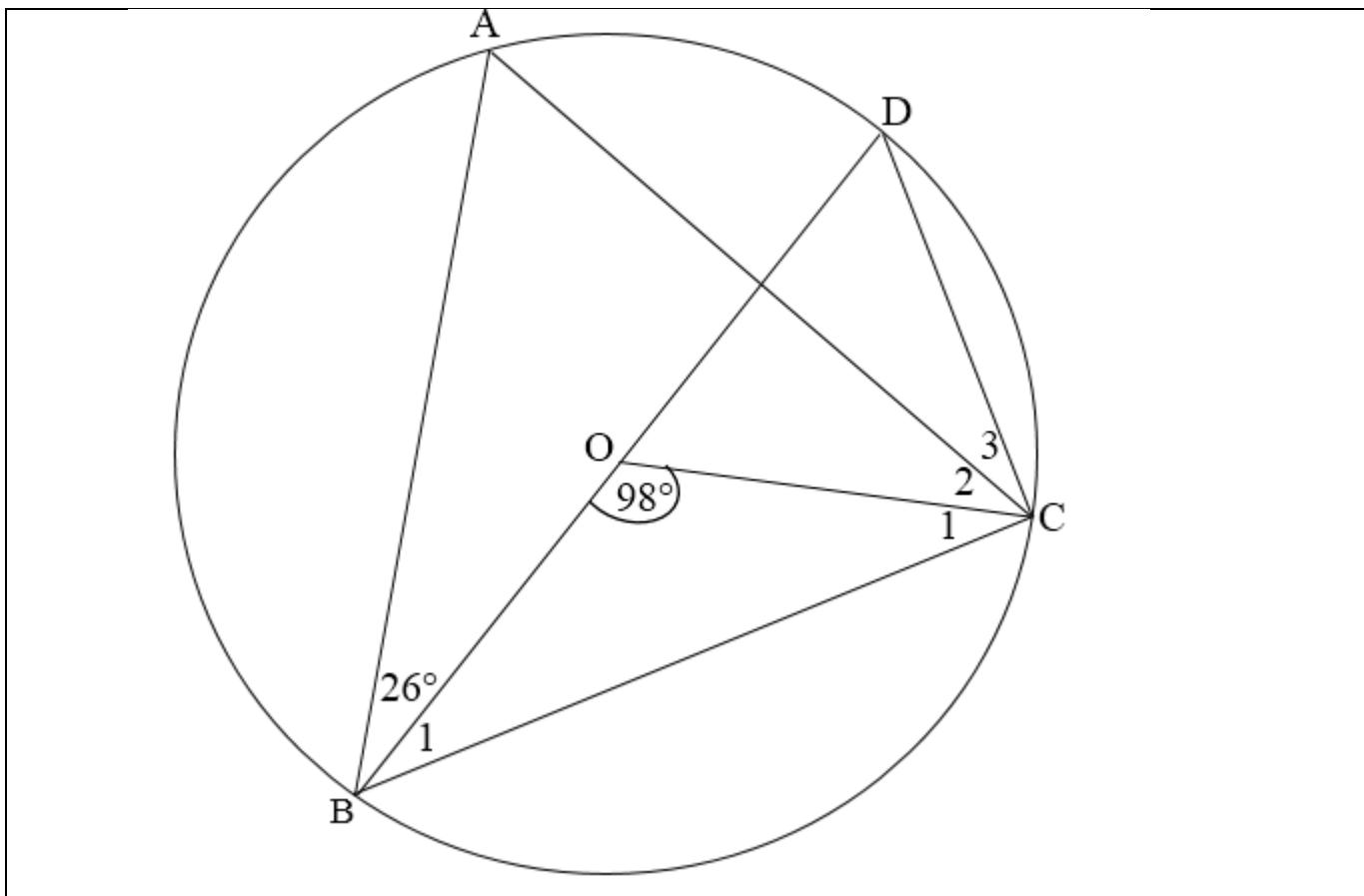
QUESTION/VRAAG 8



8.1		(1)
8.2		
8.3		
8.4		

[10]

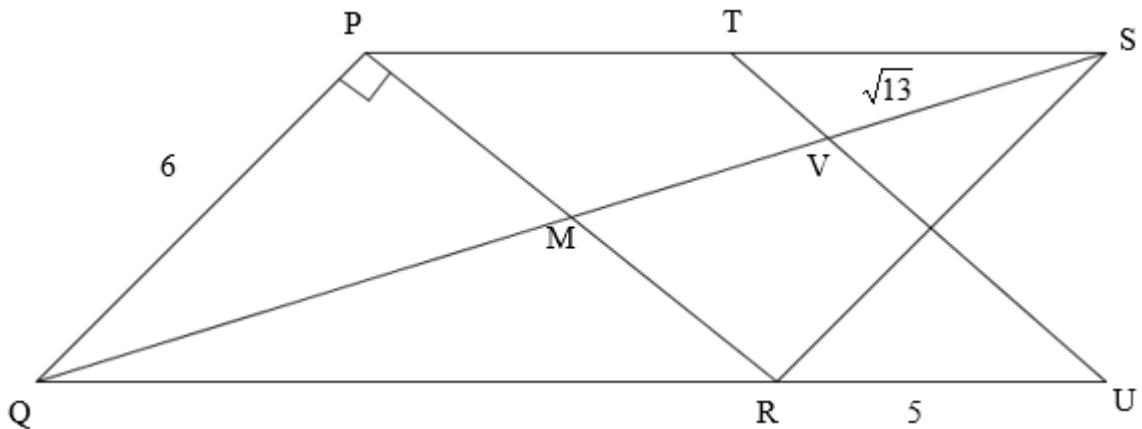
QUESTION/VRAAG 9



9.1		(2)
9.2		(3)
9.3		(3)

[8]

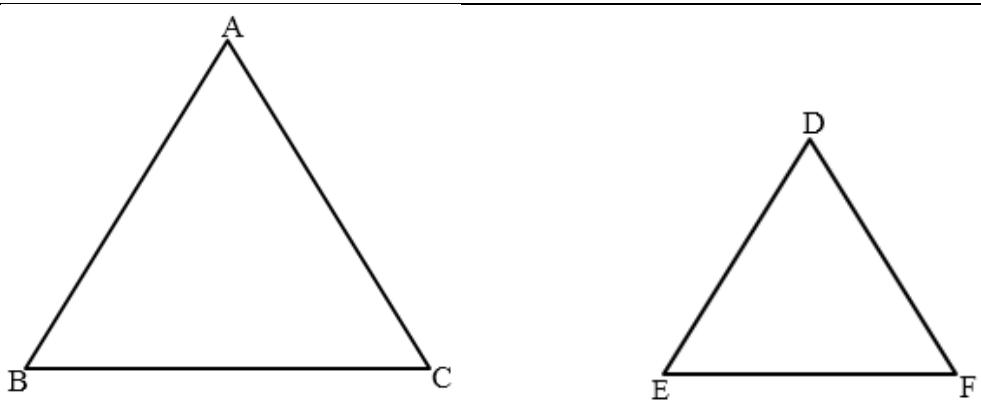
QUESTION/VRAAG 10



10.1	10.1.1		
			(3)
10.1.2			
			(4)
10.2			
			(2)

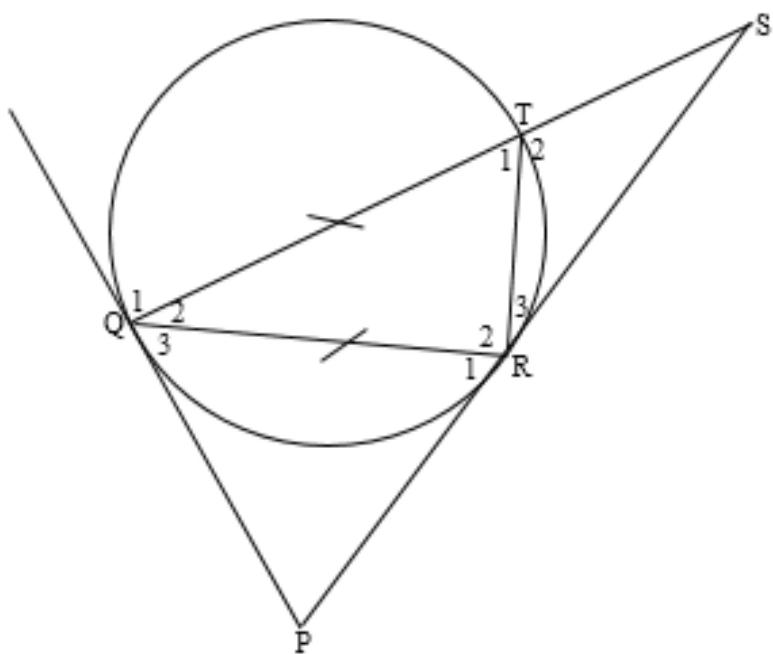
QUESTION/VRAAG 11

11.1



(7)

11.2



11.2.1

(3)

11.2.2

(2)

11.2.3

(3)

11.2.4

	11.2.5		
			(2)
	11.2.6		
			(3)

[23]

TOTAL/TOTAAL: 150**Additional Space/Addisionele Ruimte**

Additional Space/Additionele Ruimte

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GRADE/GRAAD 12

JUNE/JUNIE 2017

**MATHEMATICS P2/WISKUNDE V2
MEMORANDUM**

MARKS/PUNTE: 150

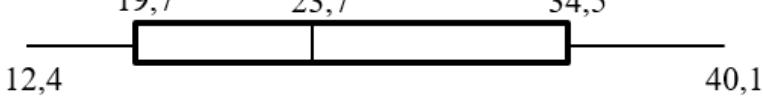
This memorandum consists of 12 pages.
Hierdie memorandum bestaan uit 12 bladsye.

QUESTION 1 / VRAAG 1

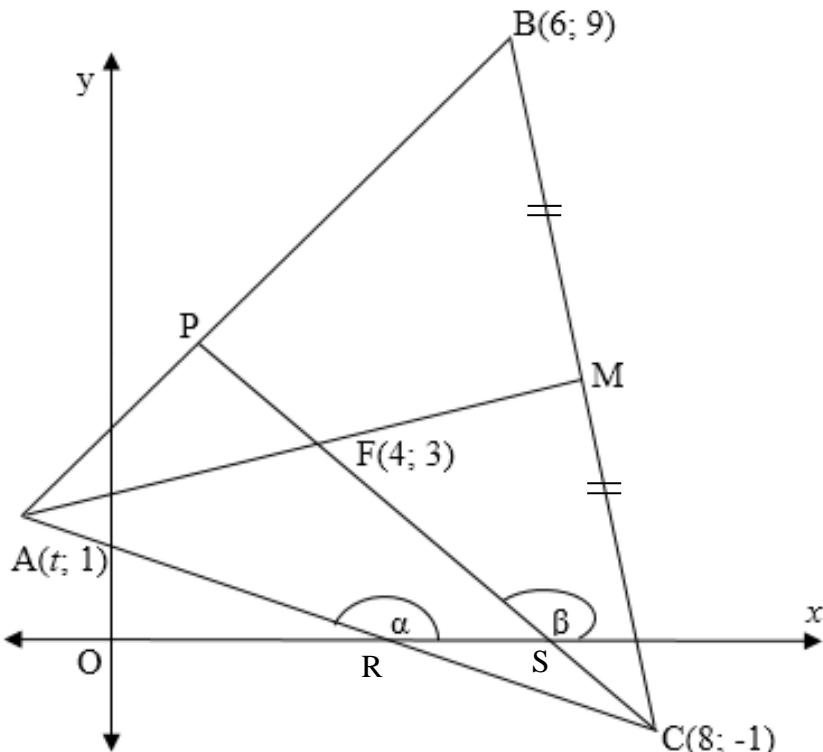
1.1	Percentages / <i>Persentasies</i>	Frequency / <i>Frekvensie</i>	Cumulative Frequency / <i>Kumulatiewe Frekvensie</i>	<ul style="list-style-type: none"> ✓ 3, 12 ✓ 24, 35, 44 ✓ 50 <p>(3)</p>		
	$30 \leq x < 40$	1	1			
	$40 \leq x < 50$	2	3			
	$50 \leq x < 60$	9	12			
	$60 \leq x < 70$	12	24			
	$70 \leq x < 80$	11	35			
	$80 \leq x < 90$	9	44			
1.2	Ogive					
					<ul style="list-style-type: none"> ✓ upper limits / <i>bo-limiete</i> ✓ cum f / <i>kum. f</i> ✓ shape / <i>vorm</i> ✓ grounded / <i>ge-anker</i> 	
1.3	Approx. 30 [accept between 28 – 32] Ongeveer 30 [aanvaar tussen 28 – 32]				<ul style="list-style-type: none"> ✓✓ answer/ indicated on graph. <i>antwoord / op grafiek aangedui</i> <p>(2)</p>	
					[9]	

QUESTION 2 / VRAAG 2

	12,4	15,1	18,9	19,7	19,7	20,0	
	20,9	23,7	23,8	31,1	33,6	34,5	
	34,9	36,5	40,1				
2.1	Minimum / <i>Minimum</i>			= 12,4			✓ min & max
	Lower quartile / <i>Onderste kwartiel</i> (Q_1)			= 19,7			✓ Q_1
	Median / <i>Mediaan</i>			(Q_2) = 23,7			✓ Q_2
	Upper quartile / <i>Boonste kwartiel</i> (Q_3)			= 34,5			✓ Q_3
	Maximum / <i>Maksimum</i>			= 40,1			
							(4)

2.2		✓ min / max ✓ Q ₁ / Q ₃ ✓ Q ₂ (3)
2.3	Skewed positively to the right. Skeef positief na regs	✓ positively skewed / positief skeef (1)
2.4	SD/SA = 8,36	✓✓ answer / antwoord (2)
2.5	A small standard deviation indicates that the data is clustered around the mean. OR/OF A large standard deviation indicates that the data is more spread out. <i>'n Klein standaardafwyking dui aan dat die data rondom die gemiddelde gegroepeer is. 'n Groot standaardafwyking dui aan dat die data meer versprei is.</i>	✓ answer / antwoord (1)

[11]

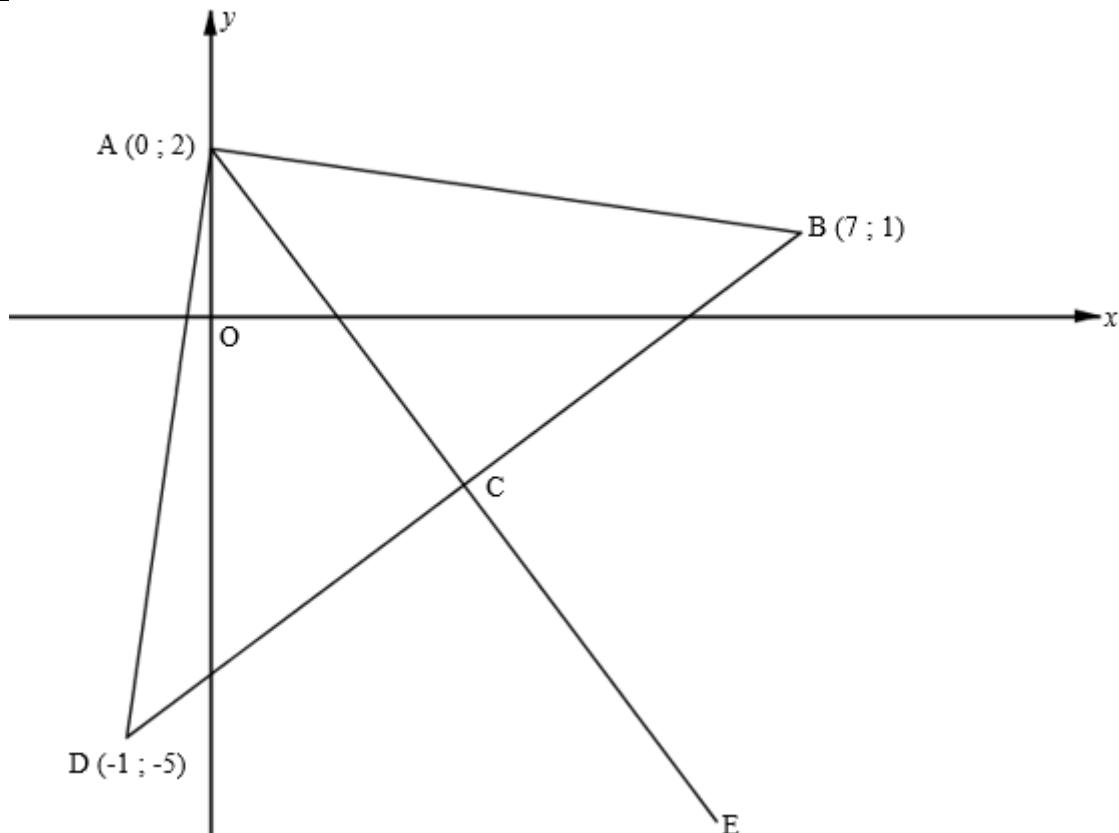
QUESTION 3 / VRAAG 3

3.1	$M = \left[\frac{6+8}{2}; \frac{9-1}{2} \right]$ $M = (7; 4)$	✓ x- value of M / x-waarde van M ✓ y- value of M / y-waarde van M (2)
3.2	$m_{FM} = \frac{4-3}{7-4} = \frac{1}{3}$ $y - y_1 = \frac{1}{3}(x - x_1)$ $m = \frac{1}{3}$ $y - 4 = \frac{1}{3}(x - 7)$ $M = (7; 4)$ $\therefore y = \frac{1}{3}x + \frac{5}{3}$	✓ substituting / vervanging ✓ value of m _{FM} / waarde van m _{FM} ✓ substituting M(7; 4) / vervanging M(7; 4) ✓ answer / antwoord (4)

3.3 $1 = \frac{1}{3}t + \frac{5}{3}$ $t = -2$ <p style="text-align: center;">OR / OF</p> $m_{AF} = m_{FM}$ $\frac{3-1}{4-t} = \frac{1}{3}$ $4-t = 6$ $t = -2$	<ul style="list-style-type: none"> ✓ substitution into line equation / vervanging in lyn vergelyking ✓ answer (as negative) / antwoord (as negatief) <p style="text-align: center;">OR / OF</p> <ul style="list-style-type: none"> ✓ substitution into grad eqn / vervanging in gradiënt vergelyking ✓ answer as negative / antwoord as negatief
3.4 $m_{PC} = \frac{3-(-1)}{4-8} = -1$ <div style="border: 1px solid black; padding: 5px; margin-top: 5px;"> ANSWER ONLY FULL MARKS/ SLEGS ANTWOORD </div>	<ul style="list-style-type: none"> ✓ substitution / vervanging ✓ answer / antwoord
3.5 $\tan \beta = -1$ $\beta = 135^\circ$	<ul style="list-style-type: none"> ✓ $\tan \beta = -1$ ✓ $\beta = 135^\circ$
3.6 $\tan \alpha = \frac{-2}{10} = -\frac{1}{5}$ $\therefore \alpha = 180^\circ - 11.31^\circ$ $= 168.69^\circ$ $A\hat{C}P = \alpha - \beta$ $= 33.69^\circ$	<ul style="list-style-type: none"> ✓ $\tan \alpha = -\frac{1}{5}$ ✓ $\alpha = 168.69^\circ$ ✓ $A\hat{C}P = \alpha - \beta$ ✓ answer / antwoord

[16]

QUESTION 4 / VRAAG 4



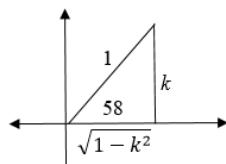
4.1 $C = \left[\frac{7-1}{2}; \frac{1-5}{2} \right]$ $= [3; -2]$	<div style="border: 1px solid black; padding: 2px;"> ANSWER ONLY / SLEGS ANTWOORD </div>	<ul style="list-style-type: none"> ✓ x-value / waarde ✓ y-value / waarde
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4.2	$CA^2 = (3 - 0)^2 + (2 + 2)^2$ $CA^2 = 25$ $CA = 5$ $CB^2 = (7 - 3)^2 + (1 + 2)^2$ $CB^2 = 25$ $CB = 5$ $\therefore CA = CB$	✓ substitution / substitusie ✓ answer for CA <i>antwoord vir CA</i> ✓ answer for CB <i>antwoord vir CB</i> (3)
4.3	$m_{AD} = \frac{2+5}{0+1}$ $= 7$ $m_{AB} = \frac{2-1}{0-7}$ $= -\frac{1}{7}$ $m_{AD} \times m_{AB} = 7 \times \left(-\frac{1}{7}\right) = -1$ $\therefore AD \perp AB \quad [m_{AD} \times m_{AB} = -1]$ $\therefore D\hat{A}B = 90^\circ$	✓ substitution ✓ $m_{AD} = 7$ ✓ substitution ✓ m_{AB} ✓ $m_{AD} \times m_{AB} = -1$ (5)
4.4	$(x - 3)^2 + (y + 2)^2 = 25$	✓ correct centre / <i>korrek middelpunt</i> ✓ correct / <i>korrekte r²</i> (2)
4.5	$m_{BC} = \frac{1 - (-2)}{7 - 3}$ $= \frac{3}{4}$	✓ substitution ✓ m_{BC} (2)
4.6	$m_{tan} = -\frac{4}{3}$ $y - 1 = -\frac{4}{3}(x - 7)$ $y = -\frac{4}{3}x + \frac{31}{3}$	✓ m_{tan} ✓ subst $m = -\frac{4}{3}$ and $B(7;1)$ verv. $m = -\frac{4}{3}$ en $B(7;1)$ ✓ answer / <i>antwoord</i> (3)
4.7	AE = DB [diameters of same circle] \therefore ABED is a rectangle [diagonals =]	✓ AE = DB ✓ reason ✓ reason (3)

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QUESTION 5 / VRAAG 5

5.1.1	$\sin 238^\circ = -\sin 58^\circ$ $= -k$	✓ reduction / reduksie ✓ answer / <i>antwoord</i> (2)
5.1.2	$\cos 58^\circ = \sin 32^\circ$ $= \sqrt{1 - k^2}$	✓ $\sin 32^\circ$ ✓ answer / <i>antwoord</i> (2)

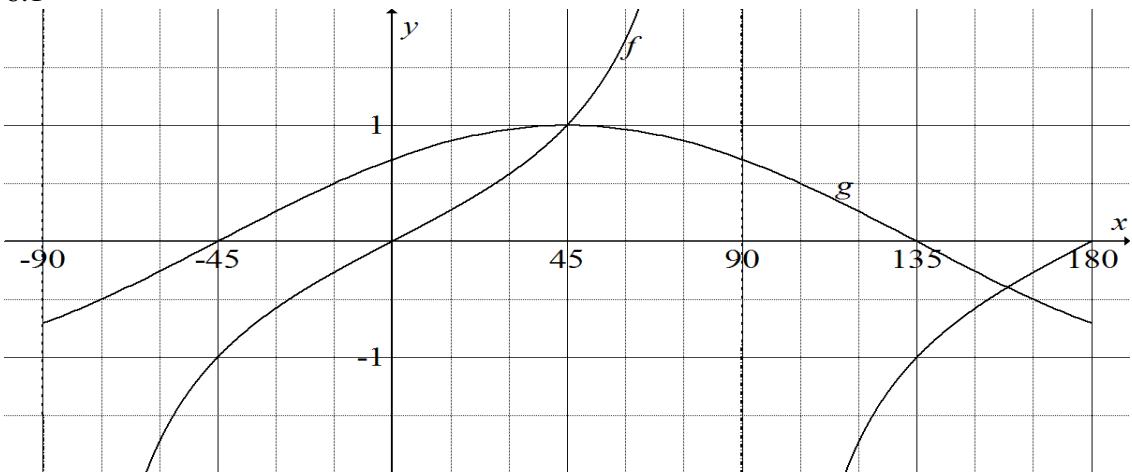


5.2	$ \begin{aligned} &= \frac{\tan(180^\circ - 30^\circ) \cdot \sin(360^\circ - 60^\circ) \cdot \sin 10^\circ}{\cos(180^\circ + 45^\circ) \cdot \sin(180^\circ - 45^\circ) \cdot \cos(90^\circ - 10^\circ)} \\ &= \frac{(-\tan 30^\circ)(-\sin 60^\circ) \sin 10^\circ}{(-\cos 45^\circ)(\sin 45^\circ) \sin 10^\circ} \\ &= \frac{\frac{1}{\sqrt{3}} \cdot \frac{\sqrt{3}}{2}}{-\frac{1}{\sqrt{2}} \cdot \frac{1}{\sqrt{2}}} \\ &= -1 \end{aligned} $	✓ - tan 30° ✓ - sin 60° ✓ - cos 45° ✓ sin 45° ✓ sin 10° ✓ simplification / vereenvoudiging ✓ answer / antwoord	(7)
5.3	$ \begin{aligned} \sin(\alpha + \beta) &= \cos [90^\circ - (\alpha + \beta)] \\ &= \cos[(90^\circ - \alpha) - \beta] \\ &= \cos(90^\circ - \alpha) \cos \beta - \sin(90^\circ - \alpha) \cos \beta \\ &= \sin \alpha \cos \beta - \cos \alpha \sin \beta \end{aligned} $	✓ cos [90° - (\alpha + \beta)] ✓ cos[(90° - \alpha) - \beta] ✓ cos(90° - \alpha) cos \beta - sin(90° - \alpha) cos \beta ✓ sin \alpha cos \beta - cos \alpha sin \beta	(4)
5.4	$ \begin{aligned} \frac{\cos 2x + 1}{\sin 2x \cdot \tan x} &= \frac{2 \cos^2 x - 1 + 1}{2 \sin x \cos x \cdot \frac{\sin x}{\cos x}} \\ &= \frac{2 \cos^2 x}{2 \sin^2 x} \\ &= \frac{1}{\tan^2 x} \end{aligned} $	✓ identity numerator identiteit teller ✓ identity denominator identiteit noemer ✓ $\frac{\sin x}{\cos x}$ ✓ $\frac{\cos^2 x}{\sin^2 x}$ simplification / vereenvoudiging	(4)
5.5.1	$ \begin{aligned} \frac{\sin x}{\cos x} &= 2 \sin x \\ \sin x &= 2 \sin x \cos x \\ \sin x - 2 \sin x \cos x &= 0 \\ \sin x(1 - 2 \cos x) &= 0 \\ \sin x = 0 \quad \text{or/of} \cos x = \frac{1}{2} \end{aligned} $	✓ identity / identiteit ($\frac{\sin x}{\cos x}$) ✓ simplification / vereenvoudiging ✓ factors / faktore	(3)
5.5.2	$ \begin{aligned} \sin x = 0 &\quad \text{or} \quad \cos x = \frac{1}{2} \\ x = 0^\circ + 360^\circ k, k \in \mathbb{Z} & \\ \text{OR} & \quad x = \pm 60^\circ + 360^\circ k \\ x = 180^\circ + 360^\circ k & \quad k \in \mathbb{Z} \end{aligned} $	✓ $x = 0^\circ$ ✓ $x = 180^\circ$ ✓ $x = \pm 60^\circ$ ✓ $360^\circ k, k \in \mathbb{Z}$	(4)

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QUESTION 6 / VRAAG 6

6.1



✓ Asymptotes / Asimptote (f)

✓ Shape / Vorm (g)

✓ $(45^\circ; 1)$ (f)✓ $(-45^\circ; 0)$ / $(135^\circ; 0)$ / x-intercepts (g)

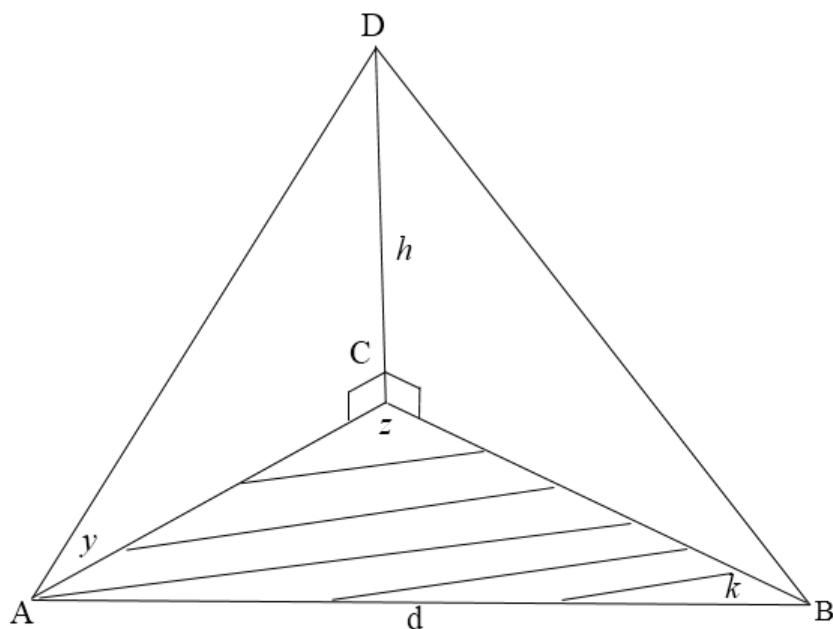
✓ Endpoints / Eindpunten (f)

✓ Endpoints / Eindpunten (g)

(6)

6.2.1	$x = -45^\circ$	✓✓ -45°
6.2.2	$(-90^\circ; 45^\circ]$ OR/OF $-90^\circ < x \leq 45^\circ$	✓ -90° and 45° ✓ correct inequalities
6.3	90°	✓ answer / antwoord

[11]

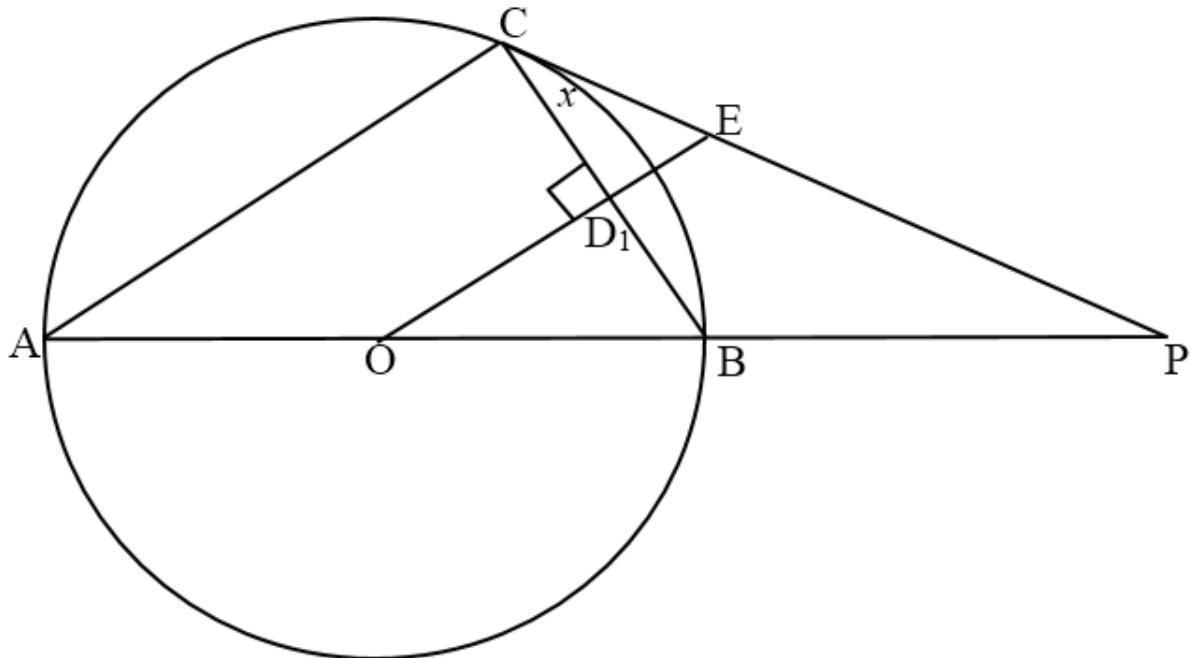
QUESTION 7 / VRAAG 7

7.1	In ΔABC $\frac{AC}{\sin k} = \frac{d}{\sin z}$ $\therefore AC = \frac{d \cdot \sin k}{\sin z}$	ANSWER ONLY/ SLEGS ANTWOORD	✓ proportion / verhouding ✓ answer / antwoord
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7.2	<p>In ΔADC</p> $\frac{AC}{\sin(90^\circ - y)} = \frac{h}{\sin y}$ $AC = \frac{h \cdot \cos y}{\sin y}$ $AC = \frac{h}{\tan y}$ <p>OR/OF</p> $\frac{AC}{h} = \frac{1}{\tan y}$ $AC = \frac{h}{\tan y}$	<ul style="list-style-type: none"> ✓ proportion / verhouding ✓ answer / antwoord
7.3	$h = \frac{AC \cdot \sin y}{\cos y}$ $h = \frac{d \sin k \cdot \sin y}{\cos y \cdot \sin z}$ $h = \frac{d \cdot \tan y \cdot \sin k}{\sin z}$ <p>OR/OF</p> $AC = \frac{h}{\tan y}$ $AC = \frac{d \cdot \sin k}{\sin z}$ $\therefore \frac{h}{\tan y} = \frac{d \cdot \sin k}{\sin z}$ $\therefore h = \frac{d \sin k \cdot \tan y}{\sin z}$	<ul style="list-style-type: none"> ✓ subst/verv. $AC = \frac{d \cdot \sin k}{\sin z}$ <p>OR/OF</p> <ul style="list-style-type: none"> ✓ equating AC / gelykstel aan AC
7.4	$\therefore h = \frac{d \sin k \cdot \tan y}{\sin z}$ $h = \frac{80 \cdot \sin 38^\circ \cdot \tan 40^\circ}{\sin 125}$ $= 50,45 \text{ m}$	<ul style="list-style-type: none"> ✓ substitution / vervanging ✓ answer / antwoord

[7]

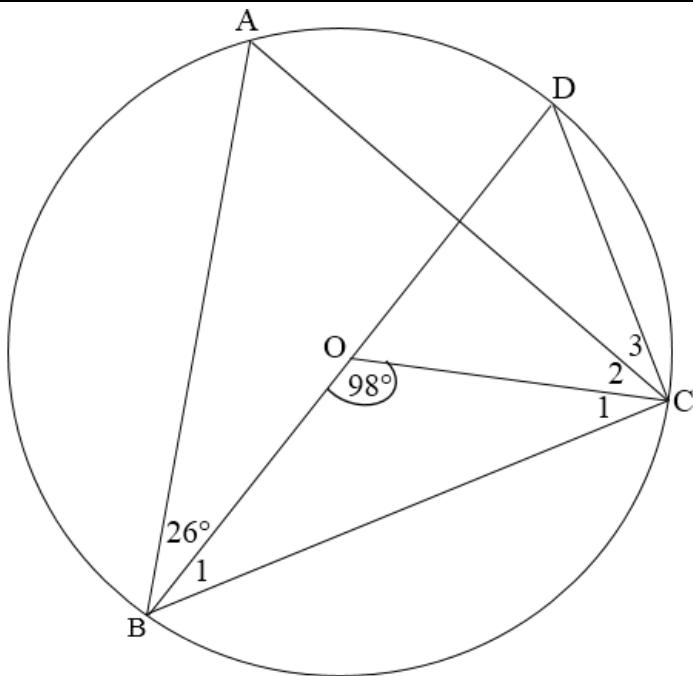
QUESTION 8 / VRAAG 8



8.1	Line from centre perpendicular to chord, bisects the chord. / <i>Lyn vanaf die middelpunt loodreg op die koord, halveer die koord.</i>	✓ answer / antwoord (1)
8.2.	$\hat{A}CB = 90^\circ$ [angle in semi-circle] / [hoek in semi-sirkel] $\hat{A}CB = \hat{D}_1$ [both = 90°] / [beide = 90°] $\therefore OE \parallel AC$ [corresp \angle 's equal] / [ooreenkomsige \angle 'e is gelyk]	✓ S ✓R ✓ R (3)
8.3	$\hat{A} = x$ [tan chord] / [raaklyn koord] $\hat{E}OB = x$ [corresp \angle 's; $AC \parallel OE$] / [ooreenkomsige \angle 'e; $AC \parallel OE$]	✓ S ✓R ✓ S ✓R (4)
8.4	$\hat{E}OB = \hat{E}CB$ [both = x] / [beide = x] $\therefore OBEC$ is cyclic quad [converse angles in same segment] $OBEC$ is 'n koordevierhoek [hoeke in dieselfde segment]	✓ S ✓ R (2)

[10]

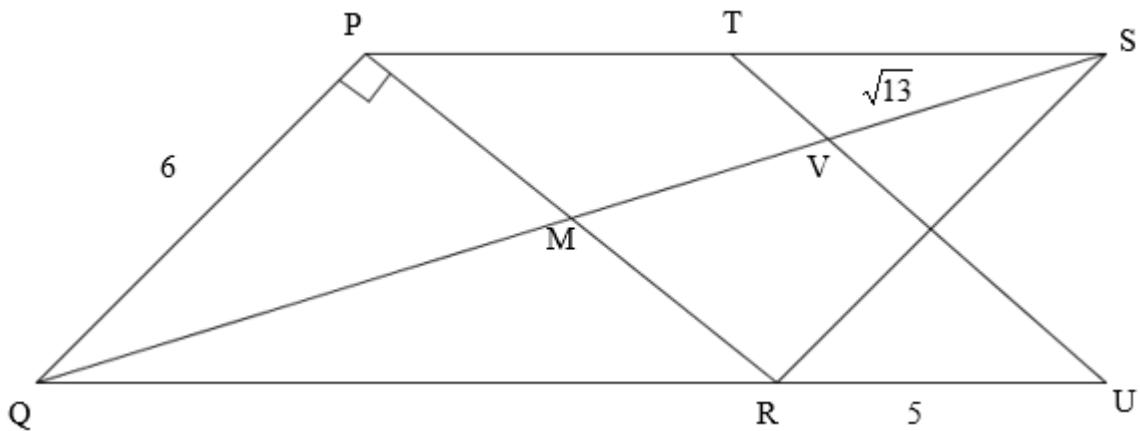
QUESTION 9 / VRAAG 9



9.1	$\hat{A} = 49^\circ$ [\angle at centre = 2 \angle at circumf.] / [Middelpunts \angle]	$\checkmark S \checkmark R$ (2)
9.2	$\hat{C}_1 = \hat{B}_1$ [angles opp equal sides] / [hoeke teenoor gelyke sye] $\hat{B}_1 = \frac{180^\circ - 98^\circ}{2}$ [angles of Δ] / [hoeke van Δ] $\hat{B}_1 = 41^\circ$	$\checkmark R$ $\checkmark R$ $\checkmark S$ (3)
9.3	$B\hat{C}D = 90^\circ$ [\angle 's in semi-circle] / [\angle^e in 'n semi-sirkel] $\hat{B}_2 = \hat{C}_3 = 26^\circ$ [\angle 's in same segment] / [\angle^e in dieselfde segment] $\hat{C}_2 = 23^\circ$	$\checkmark S/R$ $\checkmark S/R$ $\checkmark S$ (3)

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QUESTION 10 / VRAAG 10

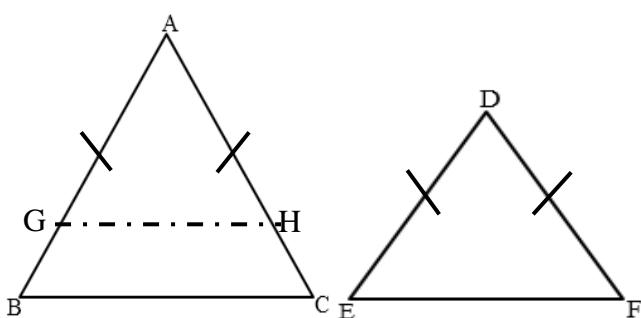


10.1.1	$QR^2 = PQ^2 + PR^2$ $= 6^2 + 8^2$ $\therefore QR = 10$ $\therefore \frac{UR}{RQ} = \frac{5}{10}$ $= \frac{1}{2}$	Pyth.Theo	\checkmark subst. in Pyth $\checkmark QR = 10$ $\checkmark \frac{UR}{RQ} = \frac{1}{2}$ (3)
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10.1.2	$PM = 4$ [diagonals bisect each other] $QM^2 = 6^2 + 4^2$ [Pyth. Theo] $QM = 2\sqrt{13}$ $MS = QM = 2\sqrt{13}$ [Diagonals bisect each other] $\therefore MV = \sqrt{13}$ $\therefore \frac{VM}{MQ} = \frac{\sqrt{13}}{2\sqrt{13}}$ $= \frac{1}{2}$	✓ R ✓ $QM = 2\sqrt{13}$ ✓ $MV = \sqrt{13}$ ✓ $\frac{VM}{MQ} = \frac{1}{2}$ (4)
10.2	$\frac{UR}{RQ} = \frac{VM}{MQ}$ $\left[\text{both} = \frac{1}{2} \right]$ $\therefore MR \parallel VU$ [line divides two sides of Δ in prop]	✓ S ✓ R (2)

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QUESTION 11 / VRAAG 11



11.1	<p>Constr/Konstr: On AB mark off $AG = DE$ / Merk $AG = DE$ af op AB On AC mark off $AH = DF$ / Merk $AH = DF$ af op AC Join GH. / Verbind GH</p> <p>Proof / Bewys: In ΔAGH & ΔDEF:</p> <ol style="list-style-type: none"> $AG = DE$ (constr) / (konstr.) $\hat{A} = \hat{D}$ (given) / (gegee) $AH = DF$ (constr) / (konstr.) $\therefore \Delta AGH \parallel \Delta DEF$ (SAS) / (SHS) $\therefore \hat{G}_1 = \hat{E}$ <p>But / Maar $\hat{B} = \hat{E}$ given/gegee $\therefore \hat{G}_1 = \hat{B}$ $\therefore GH \parallel BC$ (corresp angles equal) / (ooreenk. hoeke gelyk) $\therefore \frac{AB}{AG} = \frac{AC}{AH}$ $\therefore \frac{AB}{DE} = \frac{AC}{DF}$ ($AG = DE$, $AH = DF$) $\therefore \frac{AB}{DE} = \frac{AC}{DF} = \frac{BC}{EF}$</p>	✓ constr / konstr. ✓ S ✓ S/R ✓ S ✓ R ✓ S ✓ R (7)
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11.2		
11.2.1	$R_2 = x$ [tan chord] : [raaklyn koord] $T_1 = x$ [\angle 's opp equal sides] : [\angle 'e teenoor gelyke sye] $Q_3 = x$ [tan chord] : [raaklyn koord] $R_1 = x$ [tan from same point] : [raaklyne vanaf dieselfde punt]	\checkmark S/R \checkmark S/R \checkmark S/R \checkmark S/R \checkmark S/R (any three) / (enige drie) (3)
11.2.2	$Q_2 = 180^\circ - 2x$ [angles of Δ] : [hoeke van Δ]	\checkmark S \checkmark R (2)
11.2.3	$\hat{P} = 180^\circ - 2x$ [sum of angles of ΔPQR] $R_3 = Q_2 = 180^\circ - 2x$ [tan chord] : [raaklyn koord] $\therefore TR \parallel QP$ [corresp \angle 's =] : [ooreenkomsstige \angle 'e =]	\checkmark S \checkmark S/R \checkmark R (3)
11.2.4	In ΔSTR & ΔSRQ $\hat{S} = \hat{S}$ common / gemeen $\hat{R}_3 = \hat{Q}_2$ tan chord / raaklyn koord $\therefore \Delta STR \sim \Delta SRQ$ [AAA] / [HHH]	\checkmark S \checkmark S \checkmark R (3)
11.2.5	$\frac{ST}{SR} = \frac{SR}{SQ}$ $\Delta STR \sim \Delta SRQ$ $RS^2 = ST \cdot SQ$	\checkmark S \checkmark R (2)
11.2.6	$\frac{SP}{PR} = \frac{SQ}{TQ}$ [line \parallel to one side of a Δ] $= \frac{5}{3}$ $PQ = PR$ [tan from same point] $\frac{SP}{PQ} = \frac{5}{3}$	\checkmark S/R \checkmark R \checkmark value of $\frac{SP}{PQ} = \frac{5}{3}$ (3)

[23]

TOTAL/TOTAAL: 150